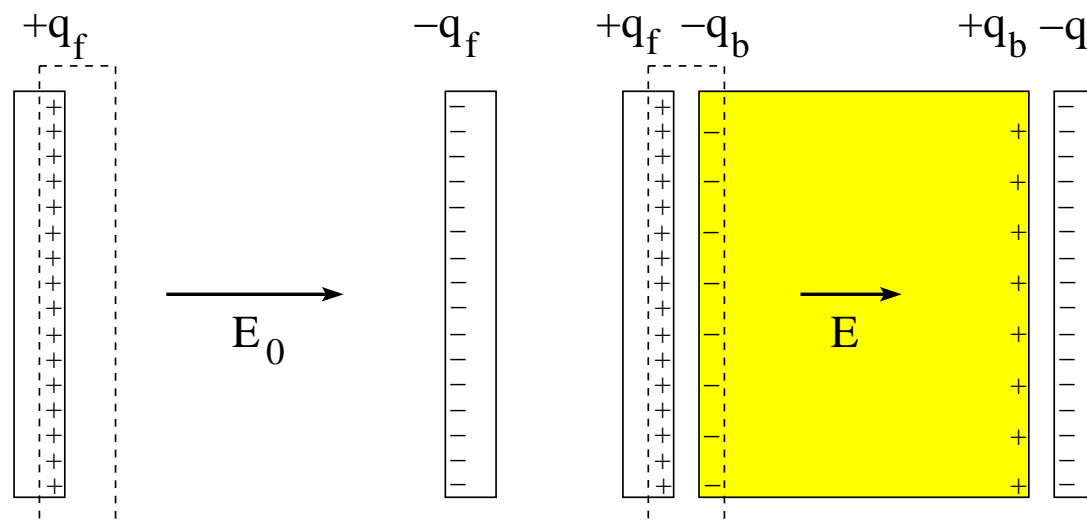


# Parallel-Plate Capacitor with Dielectric (1)



The polarization produces a bound charge on the surface of the dielectric.



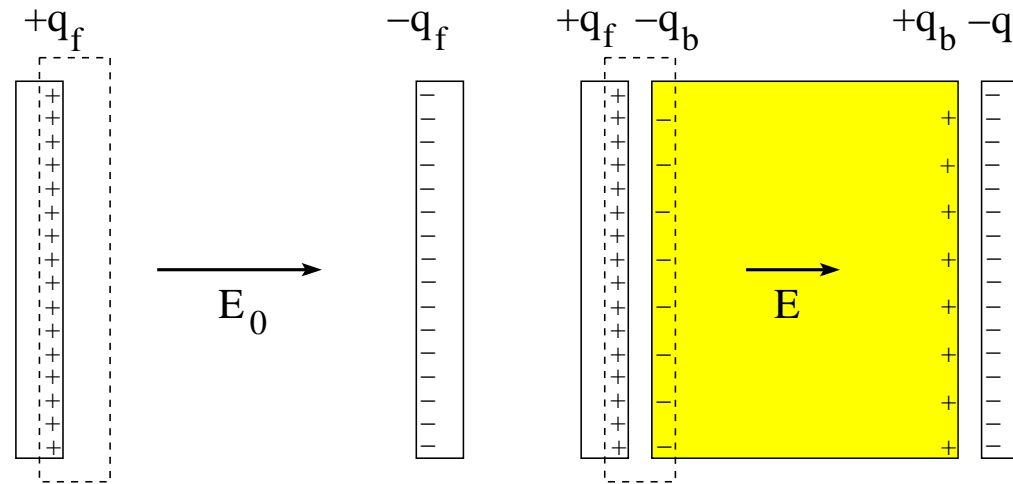
The bound surface charge has the effect of reducing the electric field between the plates from  $\vec{E}_0$  to  $\vec{E}$ .

- $A$ : area of plates
- $d$ : separation between plates
- $\pm q_f$ : free charge on plate
- $\pm q_b$ : bound charge on surface of dielectric
- $\vec{E}_0$ : electric field in vacuum
- $\vec{E}$ : electric field in dielectric

# Parallel-Plate Capacitor with Dielectric (2)



Use Gauss' law to determine the electric fields  $\vec{E}_0$  and  $\vec{E}$ .



- Field in vacuum:  $E_0 A = \frac{q_f}{\epsilon_0} \Rightarrow E_0 = \frac{q_f}{\epsilon_0 A}$
- Field in dielectric:  $E A = \frac{q_f - q_b}{\epsilon_0} \Rightarrow E = \frac{q_f - q_b}{\epsilon_0 A} < E_0$
- Voltage:  $V_0 = E_0 d$  (vacuum),  $V = E d = \frac{V_0}{\kappa} < V_0$  (dielectric)

Dielectric constant:  $\kappa \equiv \frac{E_0}{E} = \frac{q_f}{q_f - q_b} > 1$ . Permittivity of dielectric:  $\epsilon = \kappa \epsilon_0$ .