

**[mex177] Stability of sleeping top**

A symmetric top (with principal moments of inertia  $I_{\perp}, I_3$ ) is standing in an upright position ( $\theta = 0$ ) and rotating with angular velocity  $\omega_3$  about the symmetry axis. This motion is only stable under small perturbations if  $\omega_3$  exceeds a critical value  $\omega_c$ . Find  $\omega_c$ .

**Solution:**