

**[mex194] Determine canonicity and generating functions III**

Consider the following transformation from a set of canonical coordinates  $(q, p)$  to a new set of coordinates  $(Q, P)$ :

$$Q = \ln p, \quad P = -qp.$$

(a) Verify that this transformation is canonical by investigating its Jacobian determinant. (b) Determine the generating function  $F_1(q, Q)$  by integration of the total differential  $dF_1$ . (c) Determine the generating function  $F_2(q, P)$  by integration of the total differential  $dF_2$ . (d) Determine the generating function  $F_2(q, P)$  from  $F_1(q, Q)$  via Legendre transform.

**Solution:**