

**[mex21] Gauge invariance of Lagrange equations**

A dynamical system with  $n$  degrees of freedom is specified by some Lagrangian  $L(q_1, \dots, q_n, \dot{q}_1, \dots, \dot{q}_n, t)$ . Show by direct substitution that the Lagrangian

$$L' = L + \frac{d}{dt}F(q_1, \dots, q_n, t)$$

yields the same Lagrange equations if  $F$  is an arbitrary differentiable function of its arguments.

**Solution:**