

[mex221] Momentum conservation

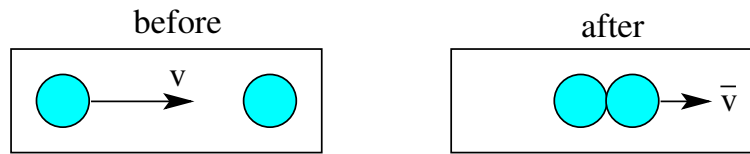
Two particles with equal masses m as measured when at rest are undergoing an inelastic collision as shown in the lab frame S . Conservation of total momentum implies

$$m(v)\mathbf{v} + m(0)0 = M(\bar{v})\bar{\mathbf{v}},$$

where $v = 2\bar{v}/(1 + \bar{v}^2/c^2)$. Use the requirement that the total momentum is also conserved in frame S' that moves with relative velocity \mathbf{u} perpendicular to \mathbf{v} to infer the relation

$$m(v')\mathbf{u} + m(u)\mathbf{u} = M(\bar{v}')\mathbf{u},$$

where $v' = \sqrt{v^2 + u^2(1 - v^2/c^2)}$ and $\bar{v}' = \sqrt{\bar{v}^2 + u^2(1 - \bar{v}^2/c^2)}$. In the limit $u \rightarrow 0$, this becomes a relativistic relation between individual masses and composite mass.



Solution: