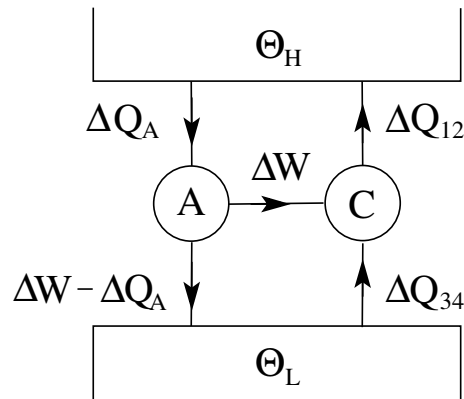


## Maximum efficiency [tln12]

Is it possible to construct a heat engine  $A$  which is more efficient than the Carnot engine  $C$ ?

Use engine  $A$  to drive engine  $C$  in the reverse i.e. as a refrigerator.



Heat transfers:  $\Delta Q_A > 0$ ,  $\Delta Q_{12} < 0$ ,  $\Delta Q_{34} > 0$ .

Work performance:  $\Delta W = \Delta W_{out}^{(A)} = \Delta W_{in}^{(C)} > 0$ .

Efficiencies:  $\eta_A = \frac{\Delta W}{\Delta Q_A}$ ,  $\eta_C = \frac{\Delta W}{|\Delta Q_{12}|}$

Since engine  $C$  operates reversibly,  $\eta_C$  is the same in the forward and reverse directions. Note:  $\eta_C$  is not an *efficiency* in the reverse mode.

$\eta_A > \eta_C$  would imply  $\Delta Q_A < |\Delta Q_{12}|$ .

The two engines combined would then cause heat to flow from low to high temperature without work input, which is a violation of the second law.

Conclusions:

- Engine  $A$  cannot be more efficient than engine  $C$ .
- All Carnot engines operating between  $\Theta_H$  and  $\Theta_L$  must have the same efficiency.