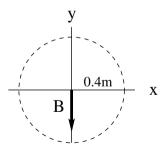


An infinitely long straight current of magnitude I=6A is directed into the plane (\otimes) and located a distance d=0.4m from the coordinate origin (somewhere on the dashed circle). The magnetic field \vec{B} generated by this current is in the negative y-direction as shown.

- (a) Find the magnitude B of the magnetic field.
- (b) Mark the location of the position of the current \otimes on the dashed circle.

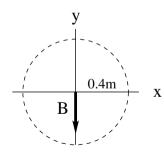




An infinitely long straight current of magnitude I=6A is directed into the plane (\otimes) and located a distance d=0.4m from the coordinate origin (somewhere on the dashed circle). The magnetic field \vec{B} generated by this current is in the negative y-direction as shown.

- (a) Find the magnitude B of the magnetic field.
- (b) Mark the location of the position of the current \otimes on the dashed circle.

(a)
$$B = \frac{\mu_0}{2\pi} \frac{I}{d} = 3\mu T$$
.





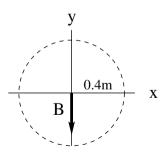
An infinitely long straight current of magnitude I=6A is directed into the plane (\otimes) and located a distance d=0.4m from the coordinate origin (somewhere on the dashed circle). The magnetic field \vec{B} generated by this current is in the negative y-direction as shown.

- (a) Find the magnitude B of the magnetic field.
- (b) Mark the location of the position of the current \otimes on the dashed circle.

Solution:

(a)
$$B = \frac{\mu_0}{2\pi} \frac{I}{d} = 3\mu T$$
.

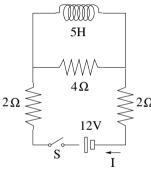
(b) Position of current \otimes is at y = 0, x = -0.4m.





In the circuit shown we close the switch S at time t=0. Find the current I through the battery and the voltage V_L across the inductor

- (a) immediately after the switch has been closed,
- (b) a very long time later.





In the circuit shown we close the switch S at time t=0. Find the current I through the battery and the voltage V_L across the inductor

- (a) immediately after the switch has been closed,
- (b) a very long time later.

2Ω S 12V I I

(a)
$$I = \frac{12V}{2\Omega + 4\Omega + 2\Omega} = 1.5A$$
, $V_L = (4\Omega)(1.5A) = 6V$.



In the circuit shown we close the switch S at time t=0. Find the current I through the battery and the voltage V_L across the inductor

- (a) immediately after the switch has been closed.
- (b) a very long time later.

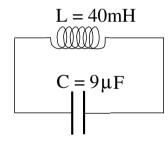
(a)
$$I=rac{12{
m V}}{2\Omega+4\Omega+2\Omega}=1.5{
m A}, \qquad V_L=(4\Omega)(1.5{
m A})=6{
m V}.$$
 (b) $I=rac{12{
m V}}{2\Omega+2\Omega}=3{
m A}, \qquad V_L=0.$

(b)
$$I = \frac{12V}{2\Omega + 2\Omega} = 3A$$
, $V_L = 0$



At time t=0 the capacitor is charged to $Q_{max}=3\mu C$ and the current is instantaneously zero.

- (a) How much energy is stored in the capacitor at time t=0?
- (b) At what time t_1 does the current reach its maximum value?
- (c) How much energy is stored in the inductor at time t_1 ?

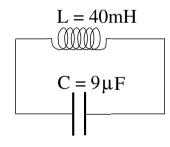




At time t=0 the capacitor is charged to $Q_{max}=3\mu C$ and the current is instantaneously zero.

- (a) How much energy is stored in the capacitor at time t=0?
- (b) At what time t_1 does the current reach its maximum value?
- (c) How much energy is stored in the inductor at time t_1 ?

(a)
$$U_C = \frac{Q_{max}^2}{2C} = 0.5 \mu J.$$





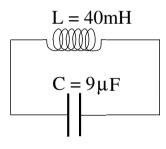
At time t=0 the capacitor is charged to $Q_{max}=3\mu C$ and the current is instantaneously zero.

- (a) How much energy is stored in the capacitor at time t=0?
- (b) At what time t_1 does the current reach its maximum value?
- (c) How much energy is stored in the inductor at time t_1 ?

(a)
$$U_C = \frac{Q_{max}^2}{2C} = 0.5 \mu J.$$

(a)
$$U_C=rac{Q_{max}^2}{2C}=0.5\mu J.$$

(b) $T=rac{2\pi}{\omega}=2\pi\sqrt{LC}=3.77 {
m ms}, \qquad t_1=rac{T}{4}=0.942 {
m ms}.$





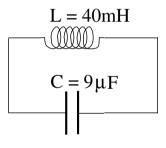
At time t=0 the capacitor is charged to $Q_{max}=3\mu C$ and the current is instantaneously zero.

- (a) How much energy is stored in the capacitor at time t=0?
- (b) At what time t_1 does the current reach its maximum value?
- (c) How much energy is stored in the inductor at time t_1 ?

(a)
$$U_C = \frac{Q_{max}^2}{2C} = 0.5 \mu J.$$

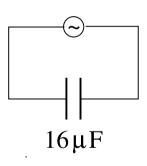
(b)
$$T=rac{2\pi}{\omega}=2\pi\sqrt{LC}=3.77 ext{ms}, \qquad t_1=rac{T}{4}=0.942 ext{ms}.$$

(c)
$$U_L = U_C = 0.5 \mu J$$
 (energy conservation.)





- (a) What is the maximum value I_{max} of the current?
- (b) What is the emf $\mathcal{E}(t)$ at t = 0.01s?
- (c) What is the current I(t) at t=0.01s?

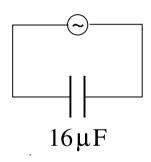




Consider the circuit shown. The ac voltage supplied is $\mathcal{E} = \mathcal{E}_{max} \cos(\omega t)$ with $\mathcal{E}_{max} = 170$ V and $\omega = 377$ rad/s.

- (a) What is the maximum value I_{max} of the current?
- (b) What is the emf $\mathcal{E}(t)$ at t = 0.01s?
- (c) What is the current I(t) at t=0.01s?

(a)
$$I_{max} = \frac{\mathcal{E}_{max}}{X_C} = \mathcal{E}_{max}\omega C = 1.03$$
A.





Consider the circuit shown. The ac voltage supplied is $\mathcal{E} = \mathcal{E}_{max} \cos(\omega t)$ with $\mathcal{E}_{max} = 170$ V and $\omega = 377$ rad/s.

- (a) What is the maximum value I_{max} of the current?
- (b) What is the emf $\mathcal{E}(t)$ at t = 0.01s?
- (c) What is the current I(t) at t = 0.01s?

16 u F

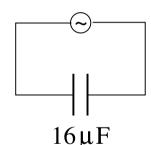
(a)
$$I_{max} = \frac{\mathcal{E}_{max}}{X_C} = \mathcal{E}_{max}\omega C = 1.03$$
A.

(b)
$$\mathcal{E} = (170 \text{V}) \cos(3.77 \text{rad}) = (170 \text{V}) (-0.809) = -138 \text{V}.$$



Consider the circuit shown. The ac voltage supplied is $\mathcal{E} = \mathcal{E}_{max} \cos(\omega t)$ with $\mathcal{E}_{max} = 170$ V and $\omega = 377$ rad/s.

- (a) What is the maximum value I_{max} of the current?
- (b) What is the emf $\mathcal{E}(t)$ at t = 0.01s?
- (c) What is the current I(t) at t = 0.01s?



(a)
$$I_{max} = \frac{\mathcal{E}_{max}}{X_C} = \mathcal{E}_{max}\omega C = 1.03$$
A.

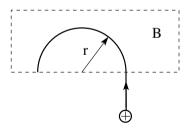
(b)
$$\mathcal{E} = (170 \text{V}) \cos(3.77 \text{rad}) = (170 \text{V})(-0.809) = -138 \text{V}.$$

(c)
$$I = \mathcal{E}_{max}\omega C \cos(3.77\text{rad} + \pi/2) = (1.03\text{A})(0.588) = 0.605\text{A}.$$



A proton ($m=1.67\times 10^{-27}$ kg, $q=1.60\times 10^{-19}$ C) with velocity $v=3.7\times 10^4$ m/s enters a region of magnetic field B directed perpendicular to the plane of the sheet. The field bends the path of the proton into a semicircle of radius r=19cm as shown.

- (a) Find the force necessary to keep the proton moving on the circle
- (b) Find the direction $(\odot \text{ or } \otimes)$ and the magnitude of the magnetic field B that provides this force.
- (c) Find the time t it takes the proton to complete the semicircular motion.

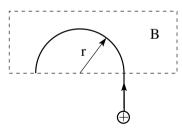




A proton ($m=1.67\times 10^{-27}$ kg, $q=1.60\times 10^{-19}$ C) with velocity $v=3.7\times 10^4$ m/s enters a region of magnetic field B directed perpendicular to the plane of the sheet. The field bends the path of the proton into a semicircle of radius r=19cm as shown.

- (a) Find the force necessary to keep the proton moving on the circle
- (b) Find the direction $(\odot \text{ or } \otimes)$ and the magnitude of the magnetic field B that provides this force.
- (c) Find the time t it takes the proton to complete the semicircular motion.

(a)
$$F = \frac{mv^2}{r} = 1.20 \times 10^{-17} \text{N}.$$





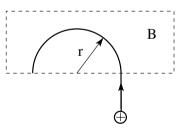
A proton ($m = 1.67 \times 10^{-27}$ kg, $q = 1.60 \times 10^{-19}$ C) with velocity $v = 3.7 \times 10^4$ m/s enters a region of magnetic field B directed perpendicular to the plane of the sheet. The field bends the path of the proton into a semicircle of radius r = 19cm as shown.

- (a) Find the force necessary to keep the proton moving on the circle
- (b) Find the direction $(\odot \text{ or } \otimes)$ and the magnitude of the magnetic field B that provides this force.
- (c) Find the time t it takes the proton to complete the semicircular motion.

(a)
$$F = \frac{mv^2}{r} = 1.20 \times 10^{-17} \text{N}$$

(a)
$$F = \frac{mv^2}{r} = 1.20 \times 10^{-17} \text{N}.$$

(b) $F = qvB \implies B = \frac{F}{qv} = 2.03 \times 10^{-3} \text{T}.$



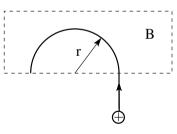


A proton ($m=1.67\times 10^{-27}$ kg, $q=1.60\times 10^{-19}$ C) with velocity $v=3.7\times 10^4$ m/s enters a region of magnetic field B directed perpendicular to the plane of the sheet. The field bends the path of the proton into a semicircle of radius r=19cm as shown.

- (a) Find the force necessary to keep the proton moving on the circle
- (b) Find the direction $(\odot \text{ or } \otimes)$ and the magnitude of the magnetic field B that provides this force.
- (c) Find the time t it takes the proton to complete the semicircular motion.

(a)
$$F = \frac{mv^2}{r} = 1.20 \times 10^{-17} \text{N}.$$

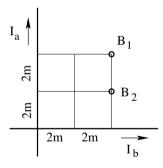
(c)
$$vt = \pi r$$
 $\Rightarrow t = \frac{\pi r}{v} = 1.61 \times 10^{-5} \text{s}.$





Consider two infinitely long, straight wires with currents of equal magnitude $I_1 = I_2 = 5$ A in the directions shown.

Find the direction (in/out) and the magnitude of the magnetic fields ${\bf B}_1$ and ${\bf B}_2$ at the points marked in the graph.

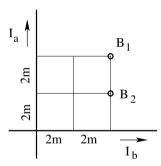




Consider two infinitely long, straight wires with currents of equal magnitude $I_1 = I_2 = 5$ A in the directions shown.

Find the direction (in/out) and the magnitude of the magnetic fields \mathbf{B}_1 and \mathbf{B}_2 at the points marked in the graph.

•
$$B_1=rac{\mu_0}{2\pi}\left(rac{5A}{4m}-rac{5A}{4m}
ight)=0$$
 (no direction).



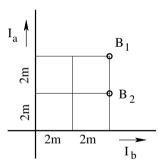


Consider two infinitely long, straight wires with currents of equal magnitude $I_1 = I_2 = 5$ A in the directions shown.

Find the direction (in/out) and the magnitude of the magnetic fields \mathbf{B}_1 and \mathbf{B}_2 at the points marked in the graph.

•
$$B_1=rac{\mu_0}{2\pi}\left(rac{5{
m A}}{4{
m m}}-rac{5{
m A}}{4{
m m}}
ight)=0$$
 (no direction).

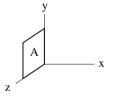
•
$$B_2=rac{\mu_0}{2\pi}\left(rac{5A}{2m}-rac{5A}{4m}
ight)=0.25\mu T$$
 (out of plane).

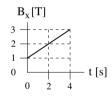




A conducting loop in the shape of a square with area $A=4\mathrm{m}^2$ and resistance $R=5\Omega$ is placed in the yz-plane as shown. A time-dependent magnetic field $\mathbf{B}=B_x\hat{\mathbf{i}}$ is present. The dependence of B_x on time is shown graphically.

- (a) Find the magnetic flux Φ_B through the loop at time t=0.
- (b) Find magnitude and direction (cw/ccw) of the induced current I at time t=2s.

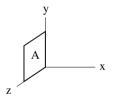


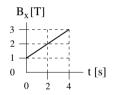




A conducting loop in the shape of a square with area $A=4\mathrm{m}^2$ and resistance $R=5\Omega$ is placed in the yz-plane as shown. A time-dependent magnetic field $\mathbf{B}=B_x\hat{\mathbf{i}}$ is present. The dependence of B_x on time is shown graphically.

- (a) Find the magnetic flux Φ_B through the loop at time t=0.
- (b) Find magnitude and direction (cw/ccw) of the induced current I at time t=2s.





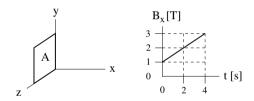
Choice of area vector: $\odot/\otimes \quad \Rightarrow$ positive direction = ccw/cw.

(a)
$$\Phi_B = \pm (1T)(4m^2) = \pm 4Tm^2$$
.



A conducting loop in the shape of a square with area $A=4\mathrm{m}^2$ and resistance $R=5\Omega$ is placed in the yz-plane as shown. A time-dependent magnetic field ${\bf B}=B_x{\bf \hat{i}}$ is present. The dependence of B_x on time is shown graphically.

- (a) Find the magnetic flux Φ_B through the loop at time t=0.
- (b) Find magnitude and direction (cw/ccw) of the induced current I at time t=2s.



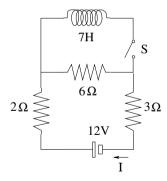
Choice of area vector: \odot/\otimes \Rightarrow positive direction = ccw/cw.

(a)
$$\Phi_R = \pm (1T)(4m^2) = \pm 4Tm^2$$
.

(a)
$$\Phi_B = \pm (1T)(4m^2) = \pm 4Tm^2$$
.
(b) $\frac{d\Phi_B}{dt} = \pm (0.5T/s)(4m^2) = \pm 2V$ $\Rightarrow \mathcal{E} = -\frac{d\Phi_B}{dt} = \mp 2V$.
 $\Rightarrow I = \frac{\mathcal{E}}{R} = \mp \frac{2V}{5O} = \mp 0.4A$ (cw).



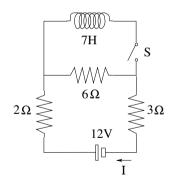
- (a) while the switch is open,
- (b) immediately after the switch has been closed,
- (c) a very long time later.





- (a) while the switch is open,
- (b) immediately after the switch has been closed,
- (c) a very long time later.

(a)
$$I = \frac{12V}{2\Omega + 3\Omega + 6\Omega} = 1.09A$$

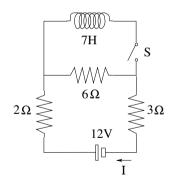




- (a) while the switch is open,
- (b) immediately after the switch has been closed,
- (c) a very long time later.

(a)
$$I = \frac{12V}{2O + 3O + 6O} = 1.09A$$

(b)
$$I = \frac{12V}{2O + 3O + 6O} = 1.09A$$
.



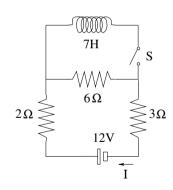


- (a) while the switch is open,
- (b) immediately after the switch has been closed,
- (c) a very long time later.

(a)
$$I = \frac{12V}{2O + 3O + 6O} = 1.09A$$

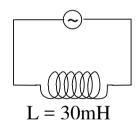
(b)
$$I = \frac{12V}{2\Omega + 3\Omega + 6\Omega} = 1.09A$$

(c)
$$I = \frac{12V}{2O + 3O} = 2.4A$$





- (a) What is the maximum value I_{max} of the current?
- (b) What is the emf ${\cal E}$ at t=0.02s?
- (c) What is the current I at t = 0.02s?



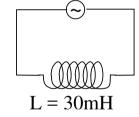


- (a) What is the maximum value I_{max} of the current?
- (b) What is the emf \mathcal{E} at t=0.02s?
- (c) What is the current I at t = 0.02s?

(a)
$$I_{max}=rac{\mathcal{E}_{max}}{X_L}=rac{\mathcal{E}_{max}}{\omega L}=rac{170 \mathrm{V}}{11.3\Omega}=15.0\mathrm{A}.$$



- (a) What is the maximum value I_{max} of the current?
- (b) What is the emf \mathcal{E} at t = 0.02s?
- (c) What is the current I at t = 0.02s?

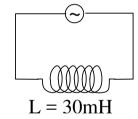


(a)
$$I_{max}=rac{\mathcal{E}_{max}}{X_L}=rac{\mathcal{E}_{max}}{\omega L}=rac{170 \mathrm{V}}{11.3\Omega}=15.0\mathrm{A}.$$

(b)
$$\mathcal{E} = \mathcal{E}_{max} \cos(7.54 \text{rad}) = (170 \text{V})(0.309) = 52.5 \text{V}.$$



- (a) What is the maximum value I_{max} of the current?
- (b) What is the emf \mathcal{E} at t=0.02s?
- (c) What is the current I at t = 0.02s?



(a)
$$I_{max} = \frac{\mathcal{E}_{max}}{X_L} = \frac{\mathcal{E}_{max}}{\omega L} = \frac{170 \text{V}}{11.3 \Omega} = 15.0 \text{A}.$$

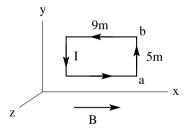
(b)
$$\mathcal{E} = \mathcal{E}_{max} \cos(7.54 \text{rad}) = (170 \text{V})(0.309) = 52.5 \text{V}.$$

(c)
$$I = I_{max} \cos(7.54 \text{rad} - \pi/2) = (15.0 \text{A})(0.951) = 14.3 \text{A}.$$



Consider a rectangular conducting loop in the xy-plane with a counterclockwise current I=7A in a uniform magnetic field $\vec{B}=3T\hat{\imath}$.

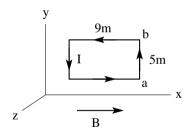
- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F} (magnitude and direction) acting on the side ab of the rectangle.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.





Consider a rectangular conducting loop in the xy-plane with a counterclockwise current I=7A in a uniform magnetic field $\vec{B}=3T\hat{\imath}$.

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F} (magnitude and direction) acting on the side ab of the rectangle.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

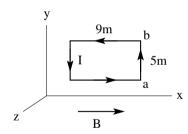


(a)
$$\vec{\mu} = (7A)(45m^2)\hat{k} = 315Am^2\hat{k}$$
.



Consider a rectangular conducting loop in the xy-plane with a counterclockwise current I=7A in a uniform magnetic field $\vec{B}=3T\hat{\imath}$.

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F} (magnitude and direction) acting on the side ab of the rectangle.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.



(a)
$$\vec{\mu} = (7A)(45m^2)\hat{k} = 315Am^2\hat{k}$$
.

(b)
$$\vec{F} = I\vec{L} \times \vec{B} = (7A)(5m\hat{j}) \times (3T\hat{i}) = -105N\hat{k}$$
.



Consider a rectangular conducting loop in the xy-plane with a counterclockwise current I=7A in a uniform magnetic field $\vec{B}=3$ T \hat{i} .

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F} (magnitude and direction) acting on the side ab of the rectangle.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

$\frac{9m}{1}$ $\frac{5m}{a}$

(a)
$$\vec{\mu} = (7A)(45m^2)\hat{k} = 315Am^2\hat{k}$$
.

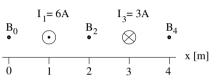
(b)
$$\vec{F} = I\vec{L} \times \vec{B} = (7A)(5m\hat{j}) \times (3T\hat{i}) = -105N\hat{k}$$
.

(c)
$$\vec{\tau} = \vec{\mu} \times \vec{B} = (315 \text{Am}^2 \hat{k}) \times (31 \hat{i}) = 945 \text{Nm} \hat{j}$$



Consider two very long, straight wires with currents $I_1 = 6A$ at x = 1m and $I_3 = 3A$ at x = 3m in the directions shown. Find magnitude and direction (up/down) of the magnetic field

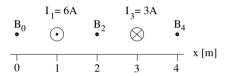
- (a) B_0 at x = 0,
- (b) B_2 at x = 2m,
- (c) B_4 at x = 4m.





Consider two very long, straight wires with currents $I_1 = 6A$ at x = 1m and $I_3 = 3A$ at x = 3m in the directions shown. Find magnitude and direction (up/down) of the magnetic field

- (a) B_0 at x = 0,
- (b) B_2 at x = 2m,
- (c) B_4 at x = 4m.

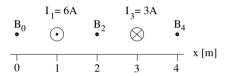


(a)
$$B_0=-rac{\mu_0(6{
m A})}{2\pi(1{
m m})}+rac{\mu_0(3{
m A})}{2\pi(3{
m m})}=-1.2\mu{
m T}+0.2\mu{
m T}=-1.0\mu{
m T}$$
 (down),



Consider two very long, straight wires with currents $I_1 = 6A$ at x = 1m and $I_3 = 3A$ at x = 3m in the directions shown. Find magnitude and direction (up/down) of the magnetic field

- (a) B_0 at x = 0,
- (b) B_2 at x = 2m,
- (c) B_4 at x = 4m.



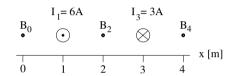
(a)
$$B_0=-rac{\mu_0(6{
m A})}{2\pi(1{
m m})}+rac{\mu_0(3{
m A})}{2\pi(3{
m m})}=-1.2\mu{
m T}+0.2\mu{
m T}=-1.0\mu{
m T}$$
 (down),

(b)
$$B_2=rac{\mu_0(6{
m A})}{2\pi(1{
m m})}+rac{\mu_0(3{
m A})}{2\pi(1{
m m})}=1.2\mu{
m T}+0.6\mu{
m T}=1.8\mu{
m T}$$
 (up),



Consider two very long, straight wires with currents $I_1 = 6A$ at x = 1m and $I_3 = 3A$ at x = 3m in the directions shown. Find magnitude and direction (up/down) of the magnetic field

- (a) B_0 at x = 0,
- (b) B_2 at x = 2m,
- (c) B_4 at x = 4m.



(a)
$$B_0 = -\frac{\mu_0(6\mathrm{A})}{2\pi(1\mathrm{m})} + \frac{\mu_0(3\mathrm{A})}{2\pi(3\mathrm{m})} = -1.2\mu\mathrm{T} + 0.2\mu\mathrm{T} = -1.0\mu\mathrm{T}$$
 (down),

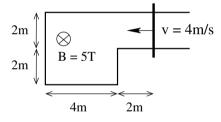
(b)
$$B_2=rac{\mu_0(6{
m A})}{2\pi(1{
m m})}+rac{\mu_0(3{
m A})}{2\pi(1{
m m})}=1.2\mu{
m T}+0.6\mu{
m T}=1.8\mu{
m T}$$
 (up),

(c)
$$B_4=rac{\mu_0(6{\rm A})}{2\pi(3{\rm m})}-rac{\mu_0(3{\rm A})}{2\pi(1{\rm m})}=0.4\mu{\rm T}-0.6\mu{\rm T}=-0.2\mu{\rm T}$$
 (down).



A conducting frame with a moving conducting rod is located in a uniform magnetic field as shown.

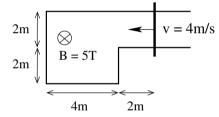
- (a) Find the magnetic flux Φ_B through the frame at the instant shown.
- (b) Find the induced emf ${\cal E}$ at the instant shown.
- (c) Find the direction (cw/ccw) of the induced current.





A conducting frame with a moving conducting rod is located in a uniform magnetic field as shown.

- (a) Find the magnetic flux Φ_B through the frame at the instant shown.
- (b) Find the induced emf ${\cal E}$ at the instant shown.
- (c) Find the direction (cw/ccw) of the induced current.

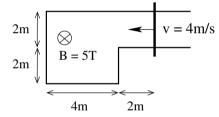


(a)
$$\Phi_B = \vec{A} \cdot \vec{B} = \pm (20 \text{m}^2)(5\text{T}) = \pm 100 \text{Wb}.$$



A conducting frame with a moving conducting rod is located in a uniform magnetic field as shown.

- (a) Find the magnetic flux Φ_B through the frame at the instant shown.
- (b) Find the induced emf $\boldsymbol{\mathcal{E}}$ at the instant shown.
- (c) Find the direction (cw/ccw) of the induced current.



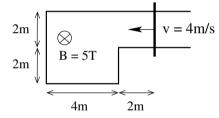
(a)
$$\Phi_B = \vec{A} \cdot \vec{B} = \pm (20 \text{m}^2)(5\text{T}) = \pm 100 \text{Wb}.$$

(b)
$$\mathcal{E} = -\frac{d\Phi_B}{dt} = \pm (5T)(2m)(4m/s) = \pm 40V.$$



A conducting frame with a moving conducting rod is located in a uniform magnetic field as shown.

- (a) Find the magnetic flux Φ_B through the frame at the instant shown.
- (b) Find the induced emf $\boldsymbol{\mathcal{E}}$ at the instant shown.
- (c) Find the direction (cw/ccw) of the induced current.



Solution:

(a)
$$\Phi_B = \vec{A} \cdot \vec{B} = \pm (20 \text{m}^2)(5\text{T}) = \pm 100 \text{Wb}.$$

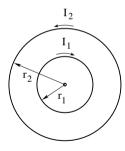
(b)
$$\mathcal{E} = -\frac{d\Phi_B}{dt} = \pm (5T)(2m)(4m/s) = \pm 40V.$$

(c) clockwise.



Consider two circular currents $I_1 = 3A$ at radius $r_1 = 2m$ and $I_2 = 5A$ at radius $r_2 = 4m$ in the directions shown.

- (a) Find magnitude B and direction (\odot, \otimes) of the resultant magnetic field at the center.
- (b) Find magnitude μ and direction (\odot, \otimes) of the magnetic dipole moment generated by the two currents.



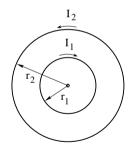


Consider two circular currents $I_1 = 3A$ at radius $r_1 = 2m$ and $I_2 = 5A$ at radius $r_2 = 4m$ in the directions shown.

- (a) Find magnitude B and direction (\odot, \otimes) of the resultant magnetic field at the center.
- (b) Find magnitude μ and direction (\odot, \otimes) of the magnetic dipole moment generated by the two currents.

(a)
$$B = \frac{\mu_0(3A)}{2(2m)} - \frac{\mu_0(5A)}{2(4m)} = (9.42 - 7.85) \times 10^{-7} T$$

 $\Rightarrow B = 1.57 \times 10^{-7} T \otimes$





Consider two circular currents $I_1 = 3A$ at radius $r_1 = 2m$ and $I_2 = 5A$ at radius $r_2 = 4m$ in the directions shown.

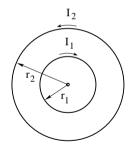
- (a) Find magnitude B and direction (\odot, \otimes) of the resultant magnetic field at the center.
- (b) Find magnitude μ and direction (\odot, \otimes) of the magnetic dipole moment generated by the two currents.

(a)
$$B = \frac{\mu_0(3A)}{2(2m)} - \frac{\mu_0(5A)}{2(4m)} = (9.42 - 7.85) \times 10^{-7} T$$

 $\Rightarrow B = 1.57 \times 10^{-7} T \otimes$

(b)
$$\mu = \pi (4m)^2 (5A) - \pi (2m)^2 (3A) = (251 - 38) Am^2$$

 $\Rightarrow \mu = 213 Am^2 \quad \odot$





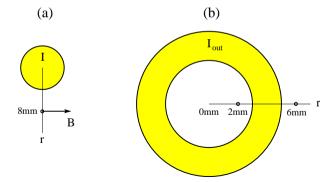
(a) Consider a solid wire of radius R = 3mm.

Find magnitude I and direction (in/out) that produces a magnetic field $B = 7\mu T$ at radius r = 8mm.

(b) Consider a hollow cable with inner radius $R_{int} = 3$ mm and outer radius $R_{ext} = 5$ mm.

A current $I_{out} = 0.9$ A is directed out of the plane.

Find direction (up/down) and magnitude B_2 , B_6 of the magnetic field at radius $r_2 = 2$ mm and $r_6 = 6$ mm, respectively.





(a) Consider a solid wire of radius R = 3mm.

Find magnitude I and direction (in/out) that produces a magnetic field $B = 7\mu T$ at radius r = 8mm.

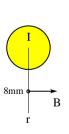
(b) Consider a hollow cable with inner radius $R_{int} = 3$ mm and outer radius $R_{ext} = 5$ mm.

A current $I_{out} = 0.9$ A is directed out of the plane.

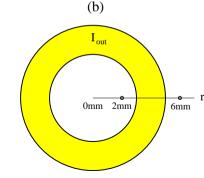
Find direction (up/down) and magnitude B_2 , B_6 of the magnetic field at radius $r_2 = 2$ mm and $r_6 = 6$ mm, respectively.

Solution:

(a)
$$7\mu T = \frac{\mu_0 I}{2\pi (8 \text{mm})} \quad \Rightarrow I = 0.28 A$$
 (out).



(a)





(a) Consider a solid wire of radius R = 3mm.

Find magnitude I and direction (in/out) that produces a magnetic field $B = 7\mu T$ at radius r = 8mm.

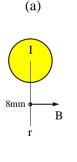
(b) Consider a hollow cable with inner radius $R_{int} = 3$ mm and outer radius $R_{ext} = 5$ mm.

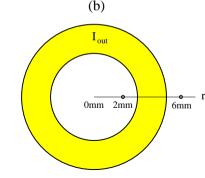
A current $I_{out} = 0.9$ A is directed out of the plane.

Find direction (up/down) and magnitude B_2 , B_6 of the magnetic field at radius $r_2 = 2$ mm and $r_6 = 6$ mm, respectively.

(a)
$$7\mu T = \frac{\mu_0 I}{2\pi (8 \text{mm})} \implies I = 0.28 \text{A}$$
 (out).

(a)
$$7\mu T = \frac{\mu_0 I}{2\pi (8 \text{mm})} \Rightarrow I = 0.28 \text{A}$$
 (out).
(b) $B_2 = 0$, $B_6 = \frac{\mu_0 (0.9 \text{A})}{2\pi (6 \text{mm})} = 30 \mu \text{T}$ (up).





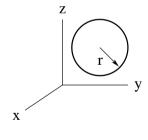


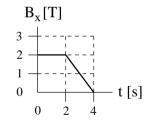
A circular wire of radius r=2.5m and resistance $R=4.8\Omega$ is placed in the yz-plane as shown.

A time-dependent magnetic field $\mathbf{B} = B_x \hat{\mathbf{i}}$ is present.

The dependence of B_x on time is shown graphically.

- (a) Find the magnitude $|\Phi_B^{(1)}|$ and $|\Phi_B^{(3)}|$ of the magnetic flux through the cicle at times t=1s and t=3s, respectively.
- (b) Find magnitude I_1 , I_3 and direction (cw/ccw) of the induced current at times t=1s and t=3s, respectively.







A circular wire of radius r=2.5m and resistance $R=4.8\Omega$ is placed in the yz-plane as shown.

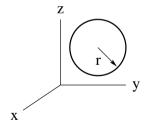
A time-dependent magnetic field $\mathbf{B} = B_x \hat{\mathbf{i}}$ is present.

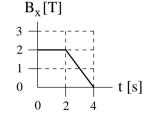
The dependence of B_x on time is shown graphically.

- (a) Find the magnitude $|\Phi_B^{(1)}|$ and $|\Phi_B^{(3)}|$ of the magnetic flux through the cicle at times t=1s and t=3s, respectively.
- (b) Find magnitude I_1 , I_3 and direction (cw/ccw) of the induced current at times t=1s and t=3s, respectively.

(a)
$$|\Phi_B^{(1)}| = \pi (2.5\text{m})^2 (2\text{T}) = 39.3 \,\text{Wb},$$

 $|\Phi_B^{(3)}| = \pi (2.5\text{m})^2 (1\text{T}) = 19.6 \,\text{Wb}.$







A circular wire of radius r=2.5m and resistance $R=4.8\Omega$ is placed in the yz-plane as shown.

A time-dependent magnetic field $\mathbf{B} = B_x \hat{\mathbf{i}}$ is present.

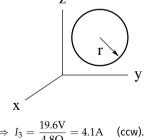
The dependence of B_x on time is shown graphically.

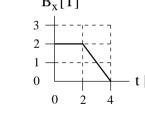
- (a) Find the magnitude $|\Phi_B^{(1)}|$ and $|\Phi_B^{(3)}|$ of the magnetic flux through the cicle at times t=1s and t=3s, respectively.
- (b) Find magnitude I_1 , I_3 and direction (cw/ccw) of the induced current at times t=1s and t=3s, respectively.

(a)
$$|\Phi_B^{(1)}| = \pi (2.5\text{m})^2 (2\text{T}) = 39.3 \,\text{Wb},$$
 $|\Phi_B^{(3)}| = \pi (2.5\text{m})^2 (1\text{T}) = 19.6 \,\text{Wb}.$

(b)
$$\left| \frac{d\Phi_B^{(1)}}{dt} \right| = 0 \quad \Rightarrow I_1 = 0,$$

$$\left| rac{d\Phi_B^{(3)}}{dt}
ight| = |\pi (2.5 {
m m})^2 (-1 {
m T/s})| = 19.6 {
m V} \qquad \Rightarrow \ I_3 = rac{19.6 {
m V}}{4.8 \Omega} = 4.1 {
m A} \quad \mbox{(ccw)}.$$

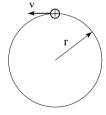






A proton ($m=1.67\times 10^{-27}$ kg, $q=1.60\times 10^{-19}$ C) with velocity $v=3.7\times 10^4$ m/s moves on a circle of radius r=0.49m in a counterclockwise direction.

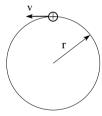
- (a) Find the centripetal force ${\it F}$ needed to keep the proton on the circle.
- (b) Find direction (\odot or \otimes) and magnitude of the field **B** that provides the centripetal force F.
- (c) Find the electric current \boldsymbol{I} produced by the rotating proton.





A proton ($m=1.67\times 10^{-27}$ kg, $q=1.60\times 10^{-19}$ C) with velocity $v=3.7\times 10^4$ m/s moves on a circle of radius r=0.49m in a counterclockwise direction.

- (a) Find the centripetal force F needed to keep the proton on the circle.
- (b) Find direction (\odot or \otimes) and magnitude of the field **B** that provides the centripetal force *F*.
- (c) Find the electric current \boldsymbol{I} produced by the rotating proton.

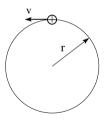


(a)
$$F = \frac{mv^2}{r} = \frac{(1.67 \times 10^{-27} \text{kg})(3.7 \times 10^4 \text{m/s})^2}{0.49 \text{m}} = 4.67 \times 10^{-18} \text{N}.$$



A proton ($m=1.67\times 10^{-27}$ kg, $q=1.60\times 10^{-19}$ C) with velocity $v=3.7\times 10^4$ m/s moves on a circle of radius r = 0.49m in a counterclockwise direction.

- (a) Find the centripetal force F needed to keep the proton on the circle.
- (b) Find direction (\odot or \otimes) and magnitude of the field **B** that provides the centripetal force F.
- (c) Find the electric current *I* produced by the rotating proton.



(a)
$$F = \frac{mv^2}{r} = \frac{(1.67 \times 10^{-27} \text{kg})(3.7 \times 10^4 \text{m/s})^2}{0.49 \text{m}} = 4.67 \times 10^{-18} \text{N}.$$

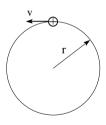
(b) $F = qvB \implies B = \frac{F}{qv} = \frac{4.67 \times 10^{-18} \text{N}}{(1.60 \times 10^{-19} \text{C})(3.7 \times 10^4 \text{m/s})} = 0.788 \text{mT} \otimes (\text{in}).$

(b)
$$F = qvB \implies B = \frac{F}{qv} = \frac{4.67 \times 10^{-18} \text{N}}{(1.60 \times 10^{-19} \text{C})(3.7 \times 10^4 \text{m/s})} = 0.788 \text{mT} \otimes (\text{in})$$



A proton ($m=1.67\times 10^{-27}$ kg, $q=1.60\times 10^{-19}$ C) with velocity $v=3.7\times 10^4$ m/s moves on a circle of radius r = 0.49m in a counterclockwise direction.

- (a) Find the centripetal force F needed to keep the proton on the circle.
- (b) Find direction (\odot or \otimes) and magnitude of the field **B** that provides the centripetal force F.
- (c) Find the electric current *I* produced by the rotating proton.



(a)
$$F = \frac{mv^2}{r} = \frac{(1.67 \times 10^{-27} \text{kg})(3.7 \times 10^4 \text{m/s})^2}{0.49 \text{m}} = 4.67 \times 10^{-18} \text{N}.$$

(b) $F = qvB \quad \Rightarrow B = \frac{F}{qv} = \frac{4.67 \times 10^{-18} \text{N}}{(1.60 \times 10^{-19} \text{C})(3.7 \times 10^4 \text{m/s})} = 0.788 \text{mT} \quad \otimes \text{(in)}.$
(c) $I = \frac{q}{\tau}, \quad \tau = \frac{2\pi r}{v} \quad \Rightarrow I = \frac{qv}{2\pi r} = 1.92 \times 10^{-15} \text{A}.$

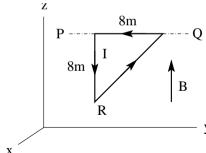
(b)
$$F = qvB \implies B = \frac{F}{qv} = \frac{4.67 \times 10^{-18} \text{N}}{(1.60 \times 10^{-19} \text{C})(3.7 \times 10^4 \text{m/s})} = 0.788 \text{mT} \otimes (\text{in})$$

(c)
$$I = \frac{q}{\tau}$$
, $\tau = \frac{2\pi r}{v}$ $\Rightarrow I = \frac{qv}{2\pi r} = 1.92 \times 10^{-15} \text{A}$



A triangular conducting loop in the yz-plane with a counterclockwise current I=3A is free to rotate about the axis PQ. A uniform magnetic field $\vec{B}=0.5T\hat{k}$ is present. (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the triangle.

- (b) Find the magnetic torque $\vec{\tau}$ (magnitude and direction) acting on the triangle.
- (c) Find the magnetic force \vec{F}_H (magnitude and direction) acting on the long side (hypotenuse) of the triangle.
- (d) Find the force \vec{F}_R (magnitude and direction) that must be applied to the corner R to keep the triangle from rotating.

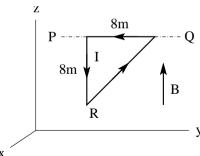




A triangular conducting loop in the yz-plane with a counterclockwise current I=3A is free to rotate about the axis PQ. A uniform magnetic field $\vec{B}=0.5T\hat{k}$ is present. (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the triangle.

- (b) Find the magnetic torque $\vec{\tau}$ (magnitude and direction) acting on the triangle.
- (c) Find the magnetic force \vec{F}_H (magnitude and direction) acting on the long side (hypotenuse) of the triangle.
- (d) Find the force \vec{F}_R (magnitude and direction) that must be applied to the corner R to keep the triangle from rotating.

(a)
$$\vec{\mu} = (3A)(32m^2)\hat{i} = 96Am^2\hat{i}$$
.

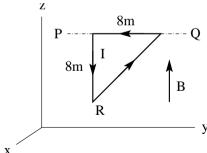




A triangular conducting loop in the yz-plane with a counterclockwise current I=3A is free to rotate about the axis PQ. A uniform magnetic field $\vec{B}=0.5T\hat{k}$ is present. (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the triangle.

- (b) Find the magnetic torque $\vec{\tau}$ (magnitude and direction) acting on the triangle.
- (c) Find the magnetic force \vec{F}_H (magnitude and direction) acting on the long side (hypotenuse) of the triangle.
- (d) Find the force \vec{F}_R (magnitude and direction) that must be applied to the corner R to keep the triangle from rotating.

- (a) $\vec{\mu} = (3A)(32m^2)\hat{i} = 96Am^2\hat{i}$.
- (b) $\vec{\tau} = \vec{\mu} \times \vec{B} = (96 \text{Am}^2 \hat{i}) \times (0.5 \text{T} \hat{k}) = -48 \text{Nm} \hat{j}$.

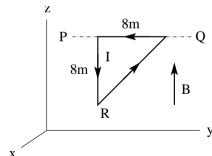




A triangular conducting loop in the yz-plane with a counterclockwise current I=3A is free to rotate about the axis PQ. A uniform magnetic field $\vec{B}=0.5T\hat{k}$ is present. (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the triangle.

- (b) Find the magnetic torque $\vec{\tau}$ (magnitude and direction) acting on the triangle.
- (c) Find the magnetic force \vec{F}_H (magnitude and direction) acting on the long side (hypotenuse) of the triangle.
- (d) Find the force \vec{F}_R (magnitude and direction) that must be applied to the corner R to keep the triangle from rotating.

- (a) $\vec{\mu} = (3A)(32m^2)\hat{i} = 96Am^2\hat{i}$.
- (b) $\vec{\tau} = \vec{\mu} \times \vec{B} = (96 \text{Am}^2 \hat{\imath}) \times (0.5 \text{T} \hat{k}) = -48 \text{Nm} \hat{\jmath}$.
- (c) $F_H = (3A)(8\sqrt{2}m)(0.5T)(\sin 45^\circ) = 12N$ \odot .

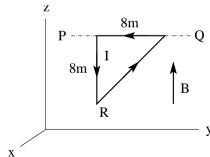




A triangular conducting loop in the yz-plane with a counterclockwise current I=3A is free to rotate about the axis PQ. A uniform magnetic field $\vec{B}=0.5T\hat{k}$ is present. (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the triangle.

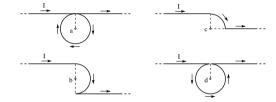
- (b) Find the magnetic torque $\vec{\tau}$ (magnitude and direction) acting on the triangle.
- (c) Find the magnetic force \vec{F}_H (magnitude and direction) acting on the long side (hypotenuse) of the triangle.
- (d) Find the force \vec{F}_R (magnitude and direction) that must be applied to the corner R to keep the triangle from rotating.

- (a) $\vec{\mu} = (3A)(32m^2)\hat{i} = 96Am^2\hat{i}$.
- (b) $\vec{\tau} = \vec{\mu} \times \vec{B} = (96\text{Am}^2\hat{i}) \times (0.5\text{T}\hat{k}) = -48\text{Nm}\hat{j}$.
- (c) $F_H = (3A)(8\sqrt{2}m)(0.5T)(\sin 45^\circ) = 12N$ \odot .
- (d) $(-8\text{m}\hat{k}) \times \vec{F}_R = -\vec{\tau} = 48\text{Nm}\hat{j}$ $\Rightarrow \vec{F}_R = -6\text{N}\hat{i}$.



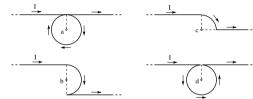


Two semi-infinite straight wires are connected to a curved wire in the form of a full circle, quarter circle, or half circle of radius R=1m in four different configurations. A current I=1A flows in the directions shown. Find magnitude B_a, B_b, B_c, B_d and direction (\odot/\otimes) of the magnetic field thus generated at the points a, b, c, d.





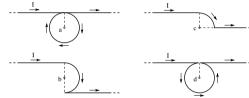
Two semi-infinite straight wires are connected to a curved wire in the form of a full circle, quarter circle, or half circle of radius R=1m in four different configurations. A current I=1A flows in the directions shown. Find magnitude B_a, B_b, B_c, B_d and direction (\odot/\otimes) of the magnetic field thus generated at the points a, b, c, d.



$$B_a = \left| \frac{\mu_0 I}{4\pi R} + \frac{\mu_0 I}{2R} + \frac{\mu_0 I}{4\pi R} \right| = |100 \text{nT} + 628 \text{nT} + 100 \text{nT}| = 828 \text{nT} \otimes 100 \text{nT}$$



Two semi-infinite straight wires are connected to a curved wire in the form of a full circle, quarter circle, or half circle of radius R=1m in four different configurations. A current I=1A flows in the directions shown. Find magnitude B_a, B_b, B_c, B_d and direction (\odot/\otimes) of the magnetic field thus generated at the points a, b, c, d.

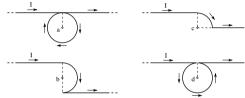


$$B_a = \left| \frac{\mu_0 I}{4\pi R} + \frac{\mu_0 I}{2R} + \frac{\mu_0 I}{4\pi R} \right| = |100 \text{nT} + 628 \text{nT} + 100 \text{nT}| = 828 \text{nT} \quad \otimes$$

$$B_b = \left| \frac{\mu_0 I}{4\pi R} + \frac{\mu_0 I}{4R} - \frac{\mu_0 I}{4\pi R} \right| = |100 \text{nT} + 314 \text{nT} - 100 \text{nT}| = 314 \text{nT} \quad \otimes$$



Two semi-infinite straight wires are connected to a curved wire in the form of a full circle, quarter circle, or half circle of radius R=1m in four different configurations. A current I=1A flows in the directions shown. Find magnitude B_a , B_b , B_c , B_d and direction (\odot/\otimes) of the magnetic field thus generated at the points a, b, c, d.



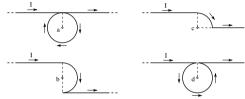
$$B_{a} = \left| \frac{\mu_{0}I}{4\pi R} + \frac{\mu_{0}I}{2R} + \frac{\mu_{0}I}{4\pi R} \right| = |100\text{nT} + 628\text{nT} + 100\text{nT}| = 828\text{nT} \quad \otimes$$

$$B_{b} = \left| \frac{\mu_{0}I}{4\pi R} + \frac{\mu_{0}I}{4R} - \frac{\mu_{0}I}{4\pi R} \right| = |100\text{nT} + 314\text{nT} - 100\text{nT}| = 314\text{nT} \quad \otimes$$

$$B_{c} = \left| \frac{\mu_{0}I}{4\pi R} + \frac{\mu_{0}I}{8R} + 0 \right| = |100\text{nT} + 157\text{nT}| = 257\text{nT} \quad \otimes$$



Two semi-infinite straight wires are connected to a curved wire in the form of a full circle, quarter circle, or half circle of radius R=1m in four different configurations. A current I=1A flows in the directions shown. Find magnitude B_a, B_b, B_c, B_d and direction (\odot/\otimes) of the magnetic field thus generated at the points a, b, c, d.



$$B_{a} = \left| \frac{\mu_{0}I}{4\pi R} + \frac{\mu_{0}I}{2R} + \frac{\mu_{0}I}{4\pi R} \right| = |100\text{nT} + 628\text{nT} + 100\text{nT}| = 828\text{nT} \quad \otimes$$

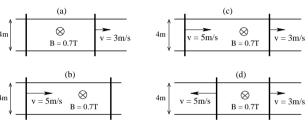
$$B_{b} = \left| \frac{\mu_{0}I}{4\pi R} + \frac{\mu_{0}I}{4R} - \frac{\mu_{0}I}{4\pi R} \right| = |100\text{nT} + 314\text{nT} - 100\text{nT}| = 314\text{nT} \quad \otimes$$

$$B_{c} = \left| \frac{\mu_{0}I}{4\pi R} + \frac{\mu_{0}I}{8R} + 0 \right| = |100\text{nT} + 157\text{nT}| = 257\text{nT} \quad \otimes$$

$$B_{d} = \left| \frac{\mu_{0}I}{4\pi R} - \frac{\mu_{0}I}{2R} + \frac{\mu_{0}I}{4\pi R} \right| = |100\text{nT} - 628\text{nT} + 100\text{nT}| = 428\text{nT} \quad \odot$$

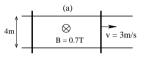


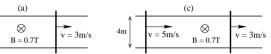
A pair of rails are connected by two mobile rods. A uniform magnetic field B directed into the plane is present. In the situations (a), (b), (c), (d), one or both rods move at constant velocity as shown. The resistance of the conducting loop is $R=0.2\Omega$ in each case. Find magnitude I and direction (cw/ccw) of the induced current in each case.

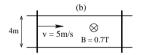


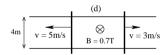


A pair of rails are connected by two mobile rods. A uniform magnetic field B directed into the plane is present. In the situations (a), (b), (c), (d), one or both rods move at constant velocity as shown. The resistance of the conducting loop is $R = 0.2\Omega$ in each case. Find magnitude I and direction (cw/ccw) of the induced current in each case.





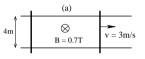


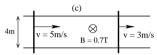


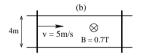
(a)
$$|\mathcal{E}| = (3\text{m/s})(0.7\text{T})(4\text{m}) = 8.4\text{V}, \qquad I = \frac{8.4\text{V}}{0.2\Omega} = 42\text{A}$$

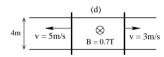


A pair of rails are connected by two mobile rods. A uniform magnetic field B directed into the plane is present. In the situations (a), (b), (c), (d), one or both rods move at constant velocity as shown. The resistance of the conducting loop is $R = 0.2\Omega$ in each case. Find magnitude I and direction (cw/ccw) of the induced current in each case.









(a)
$$|\mathcal{E}| = (3\text{m/s})(0.7\text{T})(4\text{m}) = 8.4\text{V}$$
,

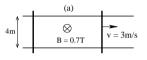
(a)
$$|\mathcal{E}| = (3\text{m/s})(0.7\text{T})(4\text{m}) = 8.4\text{V}, \qquad I = \frac{8.4\text{V}}{0.2\Omega} = 42\text{A}$$
 ccv
(b) $|\mathcal{E}| = (5\text{m/s})(0.7\text{T})(4\text{m}) = 14\text{V}, \qquad I = \frac{14\text{V}}{0.2\Omega} = 70\text{A}$ cw

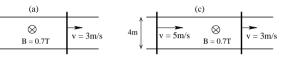
(b)
$$|\mathcal{E}| = (5\text{m/s})(0.7\text{T})(4\text{m}) = 14$$

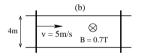
$$I = \frac{14V}{0.2\Omega} = 70A \qquad \text{cw}$$



A pair of rails are connected by two mobile rods. A uniform magnetic field B directed into the plane is present. In the situations (a), (b), (c), (d), one or both rods move at constant velocity as shown. The resistance of the conducting loop is $R = 0.2\Omega$ in each case. Find magnitude I and direction (cw/ccw) of the induced current in each case.







$$4m \oint \underbrace{v = 5m/s}_{V = 0.7T} \underbrace{\begin{pmatrix} (d) \\ (d) \\ (d) \\ (d) \\ (d) \\ (d) \\ (v = 3m/s) \\ (d) \\ (d) \\ (d) \\ (e) \\ ($$

(a)
$$|\mathcal{E}| = (3\text{m/s})(0.7\text{T})(4\text{m}) = 8.4\text{V}, \qquad I = \frac{8.4\text{V}}{0.2\Omega} = 42\text{A}$$

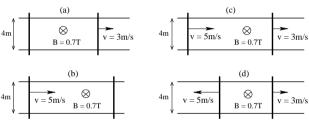
(b)
$$|\mathcal{E}| = (5\text{m/s})(0.7\text{T})(4\text{m}) = 14\text{V}, \qquad I = \frac{14\text{V}}{0.2\Omega} = 70\text{A}$$
 cw

(a)
$$|\mathcal{E}| = (3\text{m/s})(0.7\text{T})(4\text{m}) = 8.4\text{V}, \qquad I = \frac{8.4\text{V}}{0.2\Omega} = 42\text{A} \qquad \text{ccw}$$

(b) $|\mathcal{E}| = (5\text{m/s})(0.7\text{T})(4\text{m}) = 14\text{V}, \qquad I = \frac{14\text{V}}{0.2\Omega} = 70\text{A} \qquad \text{cw}$
(c) $|\mathcal{E}| = (5\text{m/s} - 3\text{m/s})(0.7\text{T})(4\text{m}) = 5.6\text{V}, \qquad I = \frac{5.6\text{V}}{0.2\Omega} = 28\text{A} \qquad \text{cw}$



A pair of rails are connected by two mobile rods. A uniform magnetic field B directed into the plane is present. In the situations (a), (b), (c), (d), one or both rods move at constant velocity as shown. The resistance of the conducting loop is $R=0.2\Omega$ in each case. Find magnitude I and direction (cw/ccw) of the induced current in each case.



(a)
$$|\mathcal{E}| = (3\text{m/s})(0.7\text{T})(4\text{m}) = 8.4\text{V}, \qquad I = \frac{8.4\text{V}}{0.2\Omega} = 42\text{A}$$
 ccw
(b) $|\mathcal{E}| = (5\text{m/s})(0.7\text{T})(4\text{m}) = 14\text{V}, \qquad I = \frac{14\text{V}}{0.2\Omega} = 70\text{A}$ cw

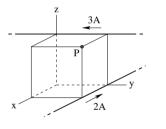
b)
$$|\mathcal{E}| = (5\text{m/s})(0.7\text{T})(4\text{m}) = 14\text{V}, \qquad I = \frac{14\text{V}}{0.2\Omega} = 70\text{A}$$
 cv

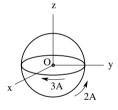
(c)
$$|\mathcal{E}| = (5\text{m/s} - 3\text{m/s})(0.7\text{T})(4\text{m}) = 5.6\text{V}, \qquad I = \frac{5.6\text{V}}{0.2\Omega} = 28\text{A}$$
 cw
(d) $|\mathcal{E}| = (5\text{m/s} + 3\text{m/s})(0.7\text{T})(4\text{m}) = 22.4\text{V}, \qquad I = \frac{22.4\text{V}}{0.2\Omega} = 112\text{A}$

(d)
$$|\mathcal{E}| = (5\text{m/s} + 3\text{m/s})(0.7\text{T})(4\text{m}) = 22.4\text{V}, \qquad I = \frac{22.4\text{V}}{0.2\Omega} = 112\text{A}$$
 ccv



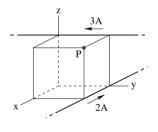
- (a) Two very long straight wires carry currents as shown. A cube with edges of length 8cm serves as scaffold. Find the magnetic field at point P in the form $\mathbf{B} = B_x \hat{\mathbf{i}} + B_y \hat{\mathbf{j}} + B_z \hat{\mathbf{k}}$ with B_x, B_y, B_z in SI units.
- (b) Two circular currents of radius 5cm, one in the xy-lane and the other in the yz-plane, carry currents as shown. Both circles are centered at point O. Find the magnetic field at point O in the form $\mathbf{B} = B_x \hat{\mathbf{i}} + B_y \hat{\mathbf{j}} + B_z \hat{\mathbf{k}}$ with B_x , B_y , B_z in SI units.

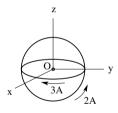






- (a) Two very long straight wires carry currents as shown. A cube with edges of length 8cm serves as scaffold. Find the magnetic field at point P in the form $\mathbf{B} = B_x \hat{\mathbf{i}} + B_y \hat{\mathbf{j}} + B_z \hat{\mathbf{k}}$ with B_x, B_y, B_z in SI units.
- (b) Two circular currents of radius 5cm, one in the xy-lane and the other in the yz-plane, carry currents as shown. Both circles are centered at point O. Find the magnetic field at point O in the form $\mathbf{B} = B_x \hat{\mathbf{i}} + B_y \hat{\mathbf{j}} + B_z \hat{\mathbf{k}}$ with B_x , B_y , B_z in SI units.

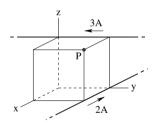


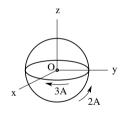


(a)
$$B_x = 0$$
, $B_y = \frac{\mu_0(2A)}{2\pi(0.08m)} = 5\mu T$, $B_z = \frac{\mu_0(3A)}{2\pi(0.08m)} = 7.5\mu T$.



- (a) Two very long straight wires carry currents as shown. A cube with edges of length 8cm serves as scaffold. Find the magnetic field at point P in the form $\mathbf{B} = B_x \hat{\mathbf{i}} + B_y \hat{\mathbf{j}} + B_z \hat{\mathbf{k}}$ with B_x, B_y, B_z in SI units.
- (b) Two circular currents of radius 5cm, one in the xy-lane and the other in the yz-plane, carry currents as shown. Both circles are centered at point O. Find the magnetic field at point O in the form $\mathbf{B} = B_x \hat{\mathbf{i}} + B_y \hat{\mathbf{j}} + B_z \hat{\mathbf{k}}$ with B_x , B_y , B_z in SI units.





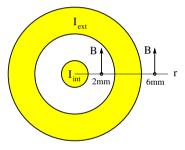
(a)
$$B_x = 0$$
, $B_y = \frac{\mu_0(2A)}{2\pi(0.08m)} = 5\mu T$, $B_z = \frac{\mu_0(3A)}{2\pi(0.08m)} = 7.5\mu T$.
(b) $B_x = \frac{\mu_0(2A)}{2(0.05m)} = 25.1\mu T$, $B_y = 0$, $B_z = -\frac{\mu_0(3A)}{2(0.05m)} = -37.7\mu T$.

b)
$$B_x = \frac{\mu_0(2A)}{2(0.05m)} = 25.1\mu\text{T}$$
, $B_y = 0$, $B_z = -\frac{\mu_0(3A)}{2(0.05m)} = -37.7\mu\text{T}$.



The coaxial cable shown has surfaces at radii 1mm, 3mm, and 5mm. The magnetic field is the same at radii 2mm and 6mm, namely $B=7\mu{\rm T}$ in the direction shown.

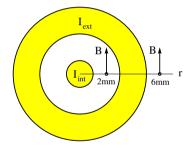
- (a) Find magnitude (in SI units) and direction (in/out) of the current $I_{\rm int}$ flowing through the inner conductor.
- (b) Find magnitude (in SI units) and direction (in/out) of the current $I_{\rm ext}$ flowing through the outer conductor.





The coaxial cable shown has surfaces at radii 1mm, 3mm, and 5mm. The magnetic field is the same at radii 2mm and 6mm, namely $B=7\mu {\rm T}$ in the direction shown.

- (a) Find magnitude (in SI units) and direction (in/out) of the current $I_{\rm int}$ flowing through the inner conductor.
- (b) Find magnitude (in SI units) and direction (in/out) of the current $I_{\rm ext}$ flowing through the outer conductor.

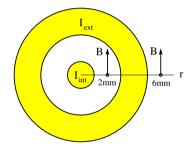


(a)
$$(7\mu T)(2\pi)(0.002m) = \mu_0 I_{int} \Rightarrow I_{int} = 0.07A$$
 (out)



The coaxial cable shown has surfaces at radii 1mm, 3mm, and 5mm. The magnetic field is the same at radii 2mm and 6mm, namely $B=7\mu {\rm T}$ in the direction shown.

- (a) Find magnitude (in SI units) and direction (in/out) of the current $I_{\rm int}$ flowing through the inner conductor.
- (b) Find magnitude (in SI units) and direction (in/out) of the current $I_{\rm ext}$ flowing through the outer conductor.



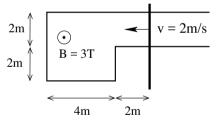
(a)
$$(7\mu T)(2\pi)(0.002m) = \mu_0 I_{int} \Rightarrow I_{int} = 0.07A$$
 (out)

(b)
$$(7\mu T)(2\pi)(0.006m) = \mu_0(I_{int}+I_{ext}) \Rightarrow I_{int}+I_{ext}=0.21A$$
 (out) $\Rightarrow I_{ext}=0.14A$ (out)



A conducting frame with a moving conducting rod is located in a uniform magnetic field as shown. The rod moves at constant velocity.

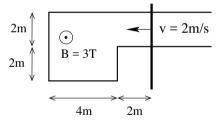
- (a) Find the magnetic flux Φ_B through the frame and the induced emf $\mathcal E$ around the frame at the instant shown.
- (b) Find the magnetic flux Φ_B through the frame and the induced emf $\mathcal E$ around the frame two seconds later. Write magnitudes only (in SI units), no directions.





A conducting frame with a moving conducting rod is located in a uniform magnetic field as shown. The rod moves at constant velocity.

- (a) Find the magnetic flux Φ_B through the frame and the induced emf $\mathcal E$ around the frame at the instant shown.
- (b) Find the magnetic flux Φ_B through the frame and the induced emf \mathcal{E} around the frame two seconds later. Write magnitudes only (in SI units), no directions.

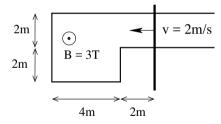


(a)
$$\Phi_B = (20\text{m}^2)(3\text{T}) = 60\text{Wb}$$
, $\mathcal{E} = (2\text{m/s})(3\text{T})(2\text{m}) = 12\text{V}$.



A conducting frame with a moving conducting rod is located in a uniform magnetic field as shown. The rod moves at constant velocity.

- (a) Find the magnetic flux Φ_B through the frame and the induced emf $\mathcal E$ around the frame at the instant shown.
- (b) Find the magnetic flux Φ_B through the frame and the induced emf \mathcal{E} around the frame two seconds later. Write magnitudes only (in SI units), no directions.



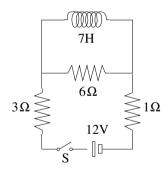
(a)
$$\Phi_B = (20m^2)(3T) = 60Wb$$
, $\mathcal{E} = (2m/s)(3T)(2m) = 12V$.

(b)
$$\Phi_B = (8m^2)(3T) = 24Wb$$
, $\mathcal{E} = (2m/s)(3T)(4m) = 24V$.



In the circuit shown we close the switch S at time t=0. Find the current I_L through the inductor and the voltage V_6 across the 6Ω -resistor

- (a) immediately after the switch has been closed,
- (b) a very long time later.

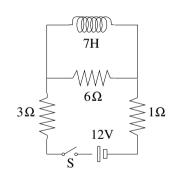




In the circuit shown we close the switch S at time t=0. Find the current I_L through the inductor and the voltage V_6 across the 6Ω -resistor

- (a) immediately after the switch has been closed,
- (b) a very long time later.

(a)
$$I_L=0$$
, $I_6=rac{12 {
m V}}{10\Omega}=1.2{
m A}$, $V_6=(6\Omega)(1.2{
m A})=7.2{
m V}$.



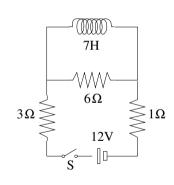


In the circuit shown we close the switch S at time t=0. Find the current I_L through the inductor and the voltage V_6 across the 6Ω -resistor

- (a) immediately after the switch has been closed,
- (b) a very long time later.

(a)
$$I_L=0$$
, $I_6=\frac{12 V}{10 \Omega}=1.2 A$, $V_6=(6 \Omega)(1.2 A)=7.2 V$.

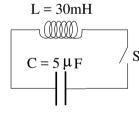
(b)
$$I_L = \frac{12V}{4\Omega} = 3A$$
, $V_6 = 0$.





At time t=0 the capacitor is charged to $Q_{max}=4\mu {\rm C}$ and the switch is being closed. The charge on the capacitor begins to decrease and the current through the inductor begins to increase.

- (a) At what time t_1 is the capacitor discharged for the first time?
- (b) At what time t_2 has the current through the inductor returned to zero for the first time?
- (c) What is the maximum energy stored in the capacitor at any time?
- (d) What is the maximum energy stored in the inductor at any time?

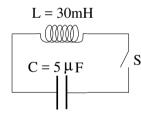




At time t=0 the capacitor is charged to $Q_{max}=4\mu {\rm C}$ and the switch is being closed. The charge on the capacitor begins to decrease and the current through the inductor begins to increase.

- (a) At what time t_1 is the capacitor discharged for the first time?
- (b) At what time t_2 has the current through the inductor returned to zero for the first time?
- (c) What is the maximum energy stored in the capacitor at any time?
- (d) What is the maximum energy stored in the inductor at any time?

(a)
$$T = \frac{2\pi}{\omega} = 2\pi\sqrt{LC} = 2.43 \text{ms}, \qquad t_1 = \frac{T}{4} = 0.608 \text{ms}.$$



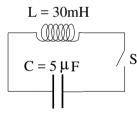


At time t=0 the capacitor is charged to $Q_{max}=4\mu C$ and the switch is being closed. The charge on the capacitor begins to decrease and the current through the inductor begins to increase.

- (a) At what time t_1 is the capacitor discharged for the first time?
- (b) At what time t_2 has the current through the inductor returned to zero for the first time?
- (c) What is the maximum energy stored in the capacitor at any time?
- (d) What is the maximum energy stored in the inductor at any time?

(a)
$$T = \frac{2\pi}{\omega} = 2\pi\sqrt{LC} = 2.43 \text{ms}, \qquad t_1 = \frac{T}{4} = 0.608 \text{ms}.$$

(b)
$$t_2 = \frac{\pi}{2} = 1.22$$
ms.





At time t=0 the capacitor is charged to $Q_{max}=4\mu C$ and the switch is being closed. The charge on the capacitor begins to decrease and the current through the inductor begins to increase.

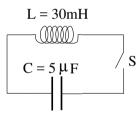
- (a) At what time t_1 is the capacitor discharged for the first time?
- (b) At what time t_2 has the current through the inductor returned to zero for the first time?
- (c) What is the maximum energy stored in the capacitor at any time?
- (d) What is the maximum energy stored in the inductor at any time?

(a)
$$T = \frac{2\pi}{\omega} = 2\pi\sqrt{LC} = 2.43 \text{ms}, \quad t_1 = \frac{T}{4} = 0.608 \text{ms}.$$

(b) $t_2 = \frac{T}{2} = 1.22 \text{ms}$

(b)
$$t_2 = \frac{T}{2} = 1.22$$
ms.

(c)
$$U_C^{max} = \frac{Q_{max}^2}{2C} = 1.6 \mu J.$$





At time t=0 the capacitor is charged to $Q_{max}=4\mu C$ and the switch is being closed. The charge on the capacitor begins to decrease and the current through the inductor begins to increase.

- (a) At what time t_1 is the capacitor discharged for the first time?
- (b) At what time t_2 has the current through the inductor returned to zero for the first time?
- (c) What is the maximum energy stored in the capacitor at any time?
- (d) What is the maximum energy stored in the inductor at any time?

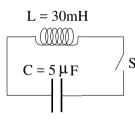
(a)
$$T = \frac{2\pi}{\omega} = 2\pi\sqrt{LC} = 2.43 \text{ms}, \quad t_1 = \frac{T}{4} = 0.608 \text{ms}.$$

(b) $t_2 = \frac{T}{-} = 1.22 \text{ms}.$

(b)
$$t_2 = \frac{T}{2} = 1.22$$
ms.

(c)
$$U_C^{max} = \frac{Q_{max}^2}{2C} = 1.6 \mu J.$$

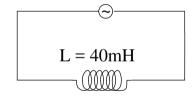
(d)
$$U_L^{max}=U_C^{max}=1.6\mu {
m J}$$
 (energy conservation.)





The ac voltage supplied in the circuit shown is $\mathcal{E} = \mathcal{E}_{max} \cos(\omega t)$ with $\mathcal{E}_{max} = 170$ V and $\omega = 377$ rad/s.

- (a) What is the maximum value I_{max} of the current?
- (b) What is the emf $\mathcal{E}(t)$ at t = 5ms?
- (c) What is the current I(t) at t = 5ms?
- (d) What is the power transfer P(t) between ac source and device at t=5ms?

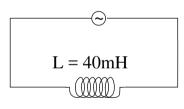




The *ac* voltage supplied in the circuit shown is $\mathcal{E} = \mathcal{E}_{max} \cos(\omega t)$ with $\mathcal{E}_{max} = 170$ V and $\omega = 377$ rad/s.

- (a) What is the maximum value I_{max} of the current?
- (b) What is the emf $\mathcal{E}(t)$ at t=5ms?
- (c) What is the current I(t) at t = 5ms?
- (d) What is the power transfer P(t) between ac source and device at t=5ms?

(a)
$$I_{max} = \frac{\mathcal{E}_{max}}{\omega L} = \frac{170 \text{V}}{(377 \text{rad/s})(40 \text{mH})} = 11.3 \text{A}.$$



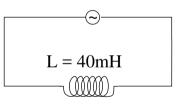


The *ac* voltage supplied in the circuit shown is $\mathcal{E} = \mathcal{E}_{max} \cos(\omega t)$ with $\mathcal{E}_{max} = 170$ V and $\omega = 377$ rad/s.

- (a) What is the maximum value I_{max} of the current?
- (b) What is the emf $\mathcal{E}(t)$ at t=5ms?
- (c) What is the current I(t) at t = 5ms?
- (d) What is the power transfer P(t) between ac source and device at t=5ms?

(a)
$$I_{max} = \frac{\mathcal{E}_{max}}{\omega L} = \frac{170 \text{V}}{(377 \text{rad/s})(40 \text{mH})} = 11.3 \text{A}.$$

(b)
$$\mathcal{E} = (170 \text{V}) \cos(1.885 \text{rad}) = (170 \text{V}) (-0.309) = -52.5 \text{V}.$$





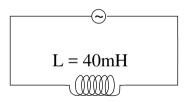
The *ac* voltage supplied in the circuit shown is $\mathcal{E} = \mathcal{E}_{max} \cos(\omega t)$ with $\mathcal{E}_{max} = 170$ V and $\omega = 377$ rad/s.

- (a) What is the maximum value I_{max} of the current?
- (b) What is the emf $\mathcal{E}(t)$ at t=5ms?
- (c) What is the current I(t) at t = 5ms?
- (d) What is the power transfer P(t) between ac source and device at t = 5ms?

(a)
$$I_{max}=rac{\mathcal{E}_{max}}{\omega L}=rac{170 \mathrm{V}}{(377 \mathrm{rad/s})(40 \mathrm{mH})}=11.3 \mathrm{A}.$$

(b)
$$\mathcal{E} = (170V)\cos(1.885rad) = (170V)(-0.309) = -52.5V.$$

(c)
$$I = (11.3A)\cos(1.885\text{rad} - \pi/2) = (11.3A)\cos(0.314) = (11.3A)(0.951) = 10.7A.$$



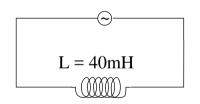


The ac voltage supplied in the circuit shown is $\mathcal{E} = \mathcal{E}_{max} \cos(\omega t)$ with $\mathcal{E}_{max} = 170$ V and $\omega = 377$ rad/s.

- (a) What is the maximum value I_{max} of the current?
- (b) What is the emf $\mathcal{E}(t)$ at t=5ms?
- (c) What is the current I(t) at t = 5ms?
- (d) What is the power transfer P(t) between ac source and device at t=5ms?

(a)
$$I_{max} = \frac{\mathcal{E}_{max}}{\omega L} = \frac{170 \text{V}}{(377 \text{rad/s})(40 \text{mH})} = 11.3 \text{A}.$$

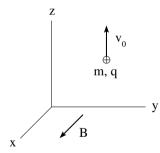
- (b) $\mathcal{E} = (170V)\cos(1.885\text{rad}) = (170V)(-0.309) = -52.5V.$
- (c) $I = (11.3A)\cos(1.885\text{rad} \pi/2) = (11.3A)\cos(0.314) = (11.3A)(0.951) = 10.7A$.
- (d) $P = \mathcal{E}I = (-52.5V)(10.7A) = -562W$.





In a region of uniform magnetic field ${\bf B}=5{
m mT}{\hat{\bf i}}$, a proton $(m=1.67\times 10^{-27}{
m kg},~q=1.60\times 10^{-19}{
m C})$ is launched with velocity ${\bf v}_0=4000{
m m/s}{\hat{\bf k}}$.

- (a) Calculate the magnitude F of the magnetic force that keeps the proton on a circular path.
- (b) Calculate the radius r of the circular path.
- (c) Calculate the time T it takes the proton to go around that circle once.
- (d) Sketch the circular path of the proton in the graph.

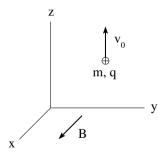




In a region of uniform magnetic field ${\bf B}=5{
m mT\hat{i}}$, a proton $(m=1.67\times 10^{-27}{
m kg},~q=1.60\times 10^{-19}{
m C})$ is launched with velocity ${\bf v}_0=4000{
m m/s}\hat{\bf k}$.

- (a) Calculate the magnitude F of the magnetic force that keeps the proton on a circular path.
- (b) Calculate the radius r of the circular path.
- (c) Calculate the time T it takes the proton to go around that circle once.
- (d) Sketch the circular path of the proton in the graph.

(a)
$$F = qv_0B = 3.2 \times 10^{-18}$$
N.





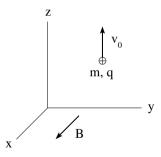
In a region of uniform magnetic field $\mathbf{B} = 5 \text{mT} \hat{\mathbf{i}}$, a proton $(m = 1.67 \times 10^{-27} \text{kg}, q = 1.60 \times 10^{-19} \text{C})$ is launched with velocity $\mathbf{v}_0 = 4000 \text{m/s} \hat{\mathbf{k}}$.

- (a) Calculate the magnitude F of the magnetic force that keeps the proton on a circular path.
- (b) Calculate the radius r of the circular path.
- (c) Calculate the time T it takes the proton to go around that circle once.
- (d) Sketch the circular path of the proton in the graph.

(a)
$$F = qv_0B = 3.2 \times 10^{-18}$$
N.

(a)
$$F = qv_0B = 3.2 \times 10^{-18} \text{N}.$$

(b) $\frac{mv_0^2}{r} = qv_0B \quad \Rightarrow \ r = \frac{mv_0}{qB} = 8.35 \text{mm}.$





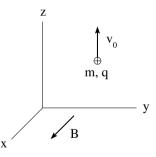
In a region of uniform magnetic field ${\bf B}=5{
m mT\hat{i}}$, a proton $(m=1.67\times 10^{-27}{
m kg},~q=1.60\times 10^{-19}{
m C})$ is launched with velocity ${\bf v}_0=4000{
m m/s}\hat{\bf k}$.

- (a) Calculate the magnitude F of the magnetic force that keeps the proton on a circular path.
- (b) Calculate the radius r of the circular path.
- (c) Calculate the time T it takes the proton to go around that circle once.
- (d) Sketch the circular path of the proton in the graph.

(a)
$$F = qv_0B = 3.2 \times 10^{-18}$$
N.

(b)
$$\frac{mv_0^2}{r} = qv_0B \implies r = \frac{mv_0}{qB} = 8.35$$
mm.

(c)
$$T = \frac{2\pi r}{v_0} = \frac{2\pi m}{qB} = 13.1 \mu s.$$





In a region of uniform magnetic field ${\bf B}=5{
m mT}{\hat{\bf i}}$, a proton $(m=1.67\times 10^{-27}{
m kg},~q=1.60\times 10^{-19}{
m C})$ is launched with velocity ${\bf v}_0=4000{
m m/s}{\hat{\bf k}}$.

- (a) Calculate the magnitude F of the magnetic force that keeps the proton on a circular path.
- (b) Calculate the radius r of the circular path.
- (c) Calculate the time T it takes the proton to go around that circle once.
- (d) Sketch the circular path of the proton in the graph.

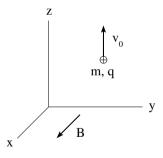
Solution:

(a)
$$F = qv_0B = 3.2 \times 10^{-18}$$
N.

(b)
$$\frac{mv_0^2}{r} = qv_0B \implies r = \frac{mv_0}{qB} = 8.35$$
mm.

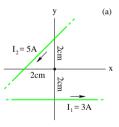
(c)
$$T = \frac{2\pi r}{v_0} = \frac{2\pi m}{aB} = 13.1 \mu s.$$

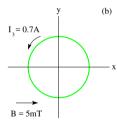
(d) Center of circle to the right of proton's initial position (cw motion).





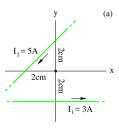
- (a) Two very long straight wires positioned in the xy-plane carry electric currents I_1, I_2 as shown. Calculate magnitude (B_1, B_2) and direction (\odot, \otimes) of the magnetic field produced by each current at the origin of the coordinate system.
- (b) A conducting loop of radius r=3cm placed in the xy-plane carries a current $I_3=0.7$ A in the direction shown. Find direction and magnitude of the torque $\vec{\tau}$ acting on the loop if it is placed in a magnetic field $\mathbf{B}=5$ m $\mathbf{T}\hat{\mathbf{i}}$.

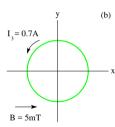






- (a) Two very long straight wires positioned in the xy-plane carry electric currents I_1, I_2 as shown. Calculate magnitude (B_1, B_2) and direction (\odot, \otimes) of the magnetic field produced by each current at the origin of the coordinate system.
- (b) A conducting loop of radius r=3cm placed in the xy-plane carries a current $I_3=0.7$ A in the direction shown. Find direction and magnitude of the torque $\vec{\tau}$ acting on the loop if it is placed in a magnetic field $\mathbf{B}=5\mathrm{mT}\hat{\mathbf{i}}$.

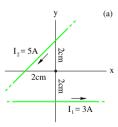


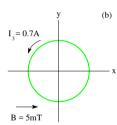


(a)
$$B_1 = \frac{\mu_0(3A)}{2\pi(2cm)} = 30\mu T$$
. \odot $B_2 = \frac{\mu_0(5A)}{2\pi(1.41cm)} = 70.9\mu T$. \odot



- (a) Two very long straight wires positioned in the xy-plane carry electric currents I_1 , I_2 as shown. Calculate magnitude (B_1, B_2) and direction (\odot, \otimes) of the magnetic field produced by each current at the origin of the coordinate system.
- (b) A conducting loop of radius r=3cm placed in the xy-plane carries a current $I_3=0.7$ A in the direction shown. Find direction and magnitude of the torque $\vec{\tau}$ acting on the loop if it is placed in a magnetic field $\mathbf{B}=5\mathrm{mT}\hat{\mathbf{i}}$.



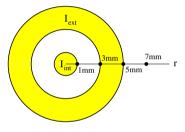


(a)
$$B_1 = \frac{\mu_0(3A)}{2\pi(2cm)} = 30\mu\text{T}.$$
 \odot $B_2 = \frac{\mu_0(5A)}{2\pi(1.41cm)} = 70.9\mu\text{T}.$ \odot

(b)
$$\vec{\mu} = \pi (3 \text{cm})^2 (0.7 \text{A}) \hat{\mathbf{k}} = 1.98 \times 10^{-3} \text{Am}^2 \hat{\mathbf{k}} \quad \Rightarrow \ \vec{\tau} = \vec{\mu} \times \mathbf{B} = 9.90 \times 10^{-6} \text{Nm} \hat{\mathbf{j}}.$$

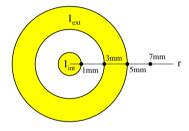


The coaxial cable shown in cross section has surfaces at radii 1mm, 3mm, and 5mm. Equal currents flow through both conductors: $I_{int} = I_{ext} = 0.03 \text{A} \odot \text{(out)}$. Find direction (\uparrow,\downarrow) and magnitude (B_1,B_3,B_5,B_7) of the magnetic field at the four radii indicated (\bullet) .





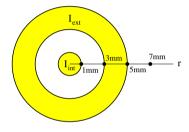
The coaxial cable shown in cross section has surfaces at radii 1mm, 3mm, and 5mm. Equal currents flow through both conductors: $I_{int} = I_{ext} = 0.03 \text{A} \odot \text{(out)}$. Find direction (\uparrow,\downarrow) and magnitude (B_1,B_3,B_5,B_7) of the magnetic field at the four radii indicated (\bullet) .



$$2\pi(1\text{mm})B_1 = \mu_0(0.03\text{A}) \quad \Rightarrow B_1 = 6\mu\text{T} \uparrow$$



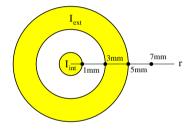
The coaxial cable shown in cross section has surfaces at radii 1mm, 3mm, and 5mm. Equal currents flow through both conductors: $I_{int} = I_{ext} = 0.03 \text{A} \odot \text{(out)}$. Find direction (\uparrow,\downarrow) and magnitude (B_1,B_3,B_5,B_7) of the magnetic field at the four radii indicated (\bullet) .



$$\begin{array}{lll} 2\pi (1\mathrm{mm})B_1 = \mu_0(0.03\mathrm{A}) & \Rightarrow B_1 = 6\mu\mathrm{T} & \uparrow \\ 2\pi (3\mathrm{mm})B_3 = \mu_0(0.03\mathrm{A}) & \Rightarrow B_3 = 2\mu\mathrm{T} & \uparrow \end{array}$$



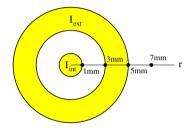
The coaxial cable shown in cross section has surfaces at radii 1mm, 3mm, and 5mm. Equal currents flow through both conductors: $I_{int} = I_{ext} = 0.03A \odot \text{(out)}$. Find direction (\uparrow,\downarrow) and magnitude (B_1,B_3,B_5,B_7) of the magnetic field at the four radii indicated (\bullet) .



$$\begin{array}{lll} 2\pi (1\mathrm{mm})B_1 = \mu_0(0.03\mathrm{A}) & \Rightarrow B_1 = 6\mu\mathrm{T} & \uparrow \\ 2\pi (3\mathrm{mm})B_3 = \mu_0(0.03\mathrm{A}) & \Rightarrow B_3 = 2\mu\mathrm{T} & \uparrow \\ 2\pi (5\mathrm{mm})B_5 = \mu_0(0.06\mathrm{A}) & \Rightarrow B_5 = 2.4\mu\mathrm{T} & \uparrow \end{array}$$



The coaxial cable shown in cross section has surfaces at radii 1mm, 3mm, and 5mm. Equal currents flow through both conductors: $I_{int} = I_{ext} = 0.03 \text{A} \odot \text{(out)}$. Find direction (\uparrow,\downarrow) and magnitude (B_1,B_3,B_5,B_7) of the magnetic field at the four radii indicated (\bullet) .

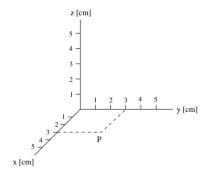


$$2\pi(1\text{mm})B_1 = \mu_0(0.03\text{A})$$
 $\Rightarrow B_1 = 6\mu\text{T}$ \uparrow $2\pi(3\text{mm})B_3 = \mu_0(0.03\text{A})$ $\Rightarrow B_3 = 2\mu\text{T}$ \uparrow $2\pi(5\text{mm})B_5 = \mu_0(0.06\text{A})$ $\Rightarrow B_5 = 2.4\mu\text{T}$ \uparrow $2\pi(7\text{mm})B_7 = \mu_0(0.06\text{A})$ $\Rightarrow B_7 = 1.71\mu\text{T}$ \uparrow



In a region of uniform magnetic field **B** a proton $(m=1.67\times10^{-27}{\rm kg},~q=1.60\times10^{-19}{\rm C})$ experiences a force ${\bf F}=9.0\times10^{-19}{\rm N}\,\hat{\bf i}$ as it passes through point P with velocity ${\bf v}_0=3000{\rm m/s}\,\hat{\bf j}$ on a circular path.

- (a) Find the magnetic field ${\bf B}$ (magnitude and direction).
- (b) Calculate the radius r of the circular path.
- (c) Locate the center *C* of the circular path in the coordinate system on the page.



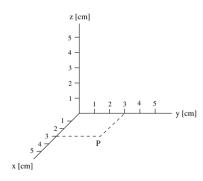


In a region of uniform magnetic field **B** a proton $(m=1.67\times10^{-27}{\rm kg},\ q=1.60\times10^{-19}{\rm C})$ experiences a force ${\bf F}=9.0\times10^{-19}{\rm N}\,\hat{\bf i}$ as it passes through point P with velocity ${\bf v}_0=3000{\rm m/s}\,\hat{\bf j}$ on a circular path.

- (a) Find the magnetic field ${\bf B}$ (magnitude and direction).
- (b) Calculate the radius r of the circular path.
- (c) Locate the center C of the circular path in the coordinate system on the page.

(a)
$$B = \frac{F}{qv_0} = 1.88 \times 10^{-3} \text{T}, \quad \hat{\mathbf{i}} = \hat{\mathbf{j}} \times \hat{\mathbf{k}}$$

 $\Rightarrow \mathbf{B} = 1.88 \times 10^{-3} \text{T } \hat{\mathbf{k}}.$





In a region of uniform magnetic field **B** a proton $(m=1.67\times10^{-27}{\rm kg},\ q=1.60\times10^{-19}{\rm C})$ experiences a force ${\bf F}=9.0\times10^{-19}{\rm N}\,\hat{\bf i}$ as it passes through point P with velocity ${\bf v}_0=3000{\rm m/s}\,\hat{\bf j}$ on a circular path.

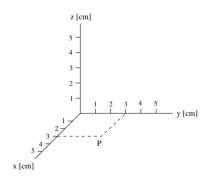
- (a) Find the magnetic field ${\bf B}$ (magnitude and direction).
- (b) Calculate the radius r of the circular path.
- (c) Locate the center C of the circular path in the coordinate system on the page.

(a)
$$B = \frac{F}{qv_0} = 1.88 \times 10^{-3} \text{T}, \quad \hat{\mathbf{i}} = \hat{\mathbf{j}} \times \hat{\mathbf{k}}$$

 $\Rightarrow \mathbf{B} = 1.88 \times 10^{-3} \text{T} \,\hat{\mathbf{k}}.$

(b)
$$F = \frac{mv_0^2}{r} = qv_0B$$

 $\Rightarrow r = \frac{mv_0^2}{F} = \frac{mv_0}{qB} = 1.67$ cm.





In a region of uniform magnetic field **B** a proton $(m=1.67\times10^{-27}{\rm kg},\ q=1.60\times10^{-19}{\rm C})$ experiences a force ${\bf F}=9.0\times10^{-19}{\rm N}\,\hat{\bf i}$ as it passes through point P with velocity ${\bf v}_0=3000{\rm m/s}\,\hat{\bf j}$ on a circular path.

- (a) Find the magnetic field ${\bf B}$ (magnitude and direction).
- (b) Calculate the radius r of the circular path.
- (c) Locate the center C of the circular path in the coordinate system on the page.

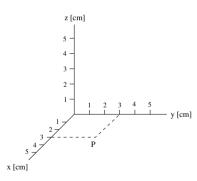
(a)
$$B = \frac{F}{qv_0} = 1.88 \times 10^{-3} \text{T}, \quad \hat{\mathbf{i}} = \hat{\mathbf{j}} \times \hat{\mathbf{k}}$$

 $\Rightarrow \mathbf{B} = 1.88 \times 10^{-3} \text{T} \hat{\mathbf{k}}.$

(b)
$$F = \frac{mv_0^2}{r} = qv_0B$$

 $\Rightarrow r = \frac{mv_0^2}{F} = \frac{mv_0}{qB} = 1.67 \text{cm}.$

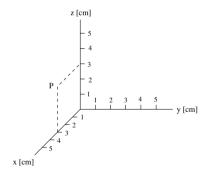
(c)
$$C = 4.67 \text{cm} \,\hat{\mathbf{i}} + 3.00 \text{cm} \,\hat{\mathbf{j}}$$
.





In a region of uniform magnetic field **B** a proton $(m=1.67\times10^{-27}{\rm kg},\ q=1.60\times10^{-19}{\rm C})$ experiences a force ${\bf F}=8.0\times10^{-19}{\rm N}\,\hat{\bf i}$ as it passes through point P with velocity ${\bf v}_0=2000{\rm m/s}\,\hat{\bf k}$ on a circular path.

- (a) Find the magnetic field ${\bf B}$ (magnitude and direction).
- (b) Calculate the radius \boldsymbol{r} of the circular path.
- (c) Locate the center C of the circular path in the coordinate system on the page.



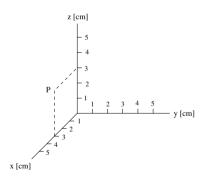


In a region of uniform magnetic field **B** a proton $(m=1.67\times10^{-27}{\rm kg},~q=1.60\times10^{-19}{\rm C})$ experiences a force ${\bf F}=8.0\times10^{-19}{\rm N\,\hat{i}}$ as it passes through point P with velocity ${\bf v}_0=2000{\rm m/s\,\hat{k}}$ on a circular path.

- (a) Find the magnetic field ${\bf B}$ (magnitude and direction).
- (b) Calculate the radius r of the circular path.
- (c) Locate the center C of the circular path in the coordinate system on the page.

(a)
$$B = \frac{F}{qv_0} = 2.50 \times 10^{-3} \text{T}, \quad \hat{\mathbf{i}} = \hat{\mathbf{k}} \times (-\hat{\mathbf{j}})$$

 $\Rightarrow \mathbf{B} = -2.50 \times 10^{-3} \text{T} \hat{\mathbf{j}}.$





In a region of uniform magnetic field **B** a proton $(m=1.67\times10^{-27}{\rm kg},\ q=1.60\times10^{-19}{\rm C})$ experiences a force ${\bf F}=8.0\times10^{-19}{\rm N}\,\hat{\bf i}$ as it passes through point P with velocity ${\bf v}_0=2000{\rm m/s}\,\hat{\bf k}$ on a circular path.

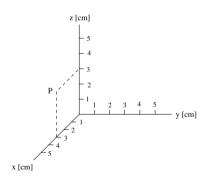
- (a) Find the magnetic field ${\bf B}$ (magnitude and direction).
- (b) Calculate the radius r of the circular path.
- (c) Locate the center C of the circular path in the coordinate system on the page.

(a)
$$B = \frac{F}{qv_0} = 2.50 \times 10^{-3} \text{T}, \quad \hat{\mathbf{i}} = \hat{\mathbf{k}} \times (-\hat{\mathbf{j}})$$

 $\Rightarrow \mathbf{B} = -2.50 \times 10^{-3} \text{T} \hat{\mathbf{j}}.$

(b)
$$F = \frac{mv_0^2}{r} = qv_0B$$

 $\Rightarrow r = \frac{mv_0^2}{F} = \frac{mv_0}{qB} = 0.835 \text{cm}.$





In a region of uniform magnetic field **B** a proton $(m=1.67\times10^{-27}{\rm kg},~q=1.60\times10^{-19}{\rm C})$ experiences a force ${\bf F}=8.0\times10^{-19}{\rm N}\,\hat{\bf i}$ as it passes through point P with velocity ${\bf v}_0=2000{\rm m/s}\,\hat{\bf k}$ on a circular path.

- (a) Find the magnetic field ${\bf B}$ (magnitude and direction).
- (b) Calculate the radius r of the circular path.
- (c) Locate the center C of the circular path in the coordinate system on the page.

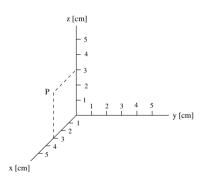
(a)
$$B = \frac{F}{qv_0} = 2.50 \times 10^{-3} \text{T}, \quad \hat{\mathbf{i}} = \hat{\mathbf{k}} \times (-\hat{\mathbf{j}})$$

 $\Rightarrow \mathbf{B} = -2.50 \times 10^{-3} \text{T} \hat{\mathbf{j}}.$

(b)
$$F = \frac{mv_0^2}{r} = qv_0B$$

 $\Rightarrow r = \frac{mv_0^2}{F} = \frac{mv_0}{qB} = 0.835$ cm.

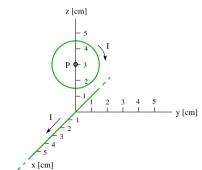
(c)
$$C = 3.84 \text{cm} \,\hat{\mathbf{i}} + 3.00 \text{cm} \,\hat{\mathbf{k}}$$
.





A very long, straight wire is positioned along the x-axis and a circular wire of 1.5cm radius in the yz plane with its center P on the z-axis as shown. Both wires carry a current I=0.6A in the directions shown.

- (a) Find the magnetic field \mathbf{B}_c (magnitude and direction) generated at point P by the current in the circular wire.
- (b) Find the magnetic field ${\bf B}_s$ (magnitude and direction) generated at point P by the current in the straight wire.
- (c) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the circular current.

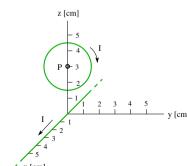




A very long, straight wire is positioned along the x-axis and a circular wire of 1.5cm radius in the yz plane with its center P on the z-axis as shown. Both wires carry a current I=0.6A in the directions shown.

- (a) Find the magnetic field \mathbf{B}_c (magnitude and direction) generated at point P by the current in the circular wire.
- (b) Find the magnetic field ${\bf B}_s$ (magnitude and direction) generated at point P by the current in the straight wire.
- (c) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the circular current.

(a)
$$\mathbf{B}_c = \frac{\mu_0(0.6\text{A})}{2(0.015\text{m})}(-\hat{\mathbf{i}}) = -2.51 \times 10^{-5}\text{T}\,\hat{\mathbf{i}}.$$





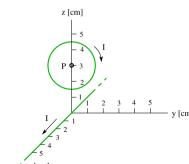
A very long, straight wire is positioned along the x-axis and a circular wire of 1.5cm radius in the yz plane with its center P on the z-axis as shown. Both wires carry a current I=0.6A in the directions shown.

- (a) Find the magnetic field B_c (magnitude and direction) generated at point P by the current in the circular wire.
- (b) Find the magnetic field \mathbf{B}_s (magnitude and direction) generated at point P by the current in the straight wire.
- (c) Find the magnetic moment \vec{u} (magnitude and direction) of the circular current.

(a)
$$\mathbf{B}_c = \frac{\mu_0(0.6A)}{2(0.015m)}(-\hat{\mathbf{i}}) = -2.51 \times 10^{-5} \mathrm{T} \,\hat{\mathbf{i}}.$$

(b) $\mathbf{B}_s = \frac{\mu_0(0.6A)}{2\pi(0.03m)}(-\hat{\mathbf{j}}) = -4.00 \times 10^{-6} \mathrm{T} \,\hat{\mathbf{j}}.$

(b)
$$\mathbf{B}_{s} = \frac{\mu_{0}(0.6\mathrm{A})}{2\pi(0.03\mathrm{m})}(-\hat{\mathbf{j}}) = -4.00 \times 10^{-6}\mathrm{T}\,\hat{\mathbf{j}}.$$





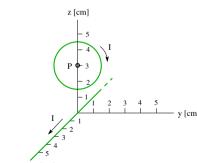
A very long, straight wire is positioned along the x-axis and a circular wire of 1.5cm radius in the yz plane with its center P on the z-axis as shown. Both wires carry a current I=0.6A in the directions shown.

- (a) Find the magnetic field \mathbf{B}_c (magnitude and direction) generated at point P by the current in the circular wire.
- (b) Find the magnetic field \mathbf{B}_s (magnitude and direction) generated at point P by the current in the straight wire.
- (c) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the circular current.

(a)
$$\mathbf{B}_c = \frac{\mu_0(0.6\mathrm{A})}{2(0.015\mathrm{m})}(-\mathbf{\hat{i}}) = -2.51 \times 10^{-5}\mathrm{T}\,\mathbf{\hat{i}}.$$

(b)
$$\mathbf{B}_s = \frac{\mu_0(0.6A)}{2\pi(0.03m)}(-\mathbf{\hat{j}}) = -4.00 \times 10^{-6} T\,\mathbf{\hat{j}}.$$

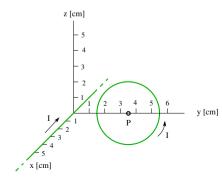
(c)
$$\vec{\mu} = \pi (0.015 \text{mm})^2 (0.6 \text{A}) (-\hat{\mathbf{i}}) = -4.24 \times 10^{-4} \text{Am}^2 \hat{\mathbf{i}}$$
.





A very long straight wire is positioned along the x-axis and a circular wire of 2.0cm radius in the yz plane with its center P on the y-axis as shown. Both wires carry a current I=0.5A in the directions shown.

- (a) Find the magnetic field \mathbf{B}_c (magnitude and direction) generated at point P by the current in the circular wire.
- (b) Find the magnetic field \mathbf{B}_s (magnitude and direction) generated at point P by the current in the straight wire.
- (c) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the circular current.

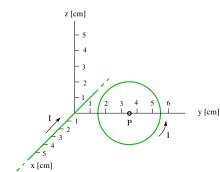




A very long straight wire is positioned along the x-axis and a circular wire of 2.0cm radius in the yz plane with its center P on the y-axis as shown. Both wires carry a current I=0.5A in the directions shown.

- (a) Find the magnetic field \mathbf{B}_c (magnitude and direction) generated at point P by the current in the circular wire.
- (b) Find the magnetic field \mathbf{B}_s (magnitude and direction) generated at point P by the current in the straight wire.
- (c) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the circular current.

(a)
$$\mathbf{B}_c = \frac{\mu_0(0.5A)}{2(0.02m)} \,\hat{\mathbf{i}} = 1.57 \times 10^{-5} \mathrm{T} \,\hat{\mathbf{i}}.$$



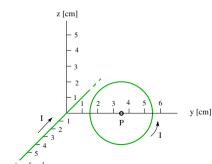


A very long straight wire is positioned along the x-axis and a circular wire of 2.0cm radius in the yz plane with its center P on the y-axis as shown. Both wires carry a current I=0.5A in the directions shown.

- (a) Find the magnetic field \mathbf{B}_c (magnitude and direction) generated at point P by the current in the circular wire.
- (b) Find the magnetic field \mathbf{B}_s (magnitude and direction) generated at point P by the current in the straight wire.
- (c) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the circular current.

(a)
$$\mathbf{B}_c = \frac{\mu_0(0.5A)}{2(0.02m)} \,\hat{\mathbf{i}} = 1.57 \times 10^{-5} \mathrm{T} \,\hat{\mathbf{i}}$$

$$\begin{aligned} \text{(a)} \;\; \mathbf{B}_c &= \frac{\mu_0(0.5\mathrm{A})}{2(0.02\mathrm{m})}\,\hat{\mathbf{i}} = 1.57 \times 10^{-5}\mathrm{T}\,\hat{\mathbf{i}}. \\ \text{(b)} \;\; \mathbf{B}_s &= \frac{\mu_0(0.5\mathrm{A})}{2\pi(0.035\mathrm{m})}(-\hat{\mathbf{k}}) = -2.86 \times 10^{-6}\mathrm{T}\,\hat{\mathbf{k}}. \end{aligned}$$





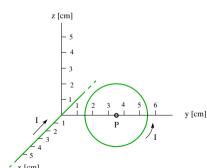
A very long straight wire is positioned along the x-axis and a circular wire of 2.0cm radius in the yz plane with its center P on the y-axis as shown. Both wires carry a current I=0.5A in the directions shown.

- (a) Find the magnetic field \mathbf{B}_c (magnitude and direction) generated at point P by the current in the circular wire.
- (b) Find the magnetic field \mathbf{B}_s (magnitude and direction) generated at point P by the current in the straight wire.
- (c) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the circular current.

(a)
$$\mathbf{B}_c = \frac{\mu_0(0.5A)}{2(0.02m)} \,\hat{\mathbf{i}} = 1.57 \times 10^{-5} \mathrm{T} \,\hat{\mathbf{i}}.$$

(b)
$$\mathbf{B}_s = \frac{\mu_0(0.5\mathrm{A})}{2\pi(0.035\mathrm{m})}(-\hat{\mathbf{k}}) = -2.86 \times 10^{-6}\mathrm{T}\,\hat{\mathbf{k}}.$$

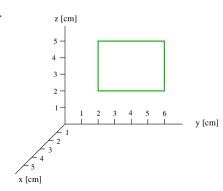
(c)
$$\vec{\mu} = \pi (0.02 \text{m})^2 (0.5 \text{A}) \,\hat{\mathbf{i}} = 6.28 \times 10^{-4} \text{Am}^2 \hat{\mathbf{i}}$$
.





Consider a wire with a resistance per unit length of 1Ω /cm bent into a rectangular loop and placed into the yz-plane as shown. The magnetic field in the entire region is uniform and increases from zero as follows:

- $\mathbf{B} = (2\hat{\mathbf{i}} + 1\hat{\mathbf{j}} + 3\hat{\mathbf{k}})t\mathsf{T/s}$, where t is the time in seconds.
- (a) Find the magnetic flux Φ_B through the rectangle at time t=2s.
- (b) Find magnitude and direction (cw/ccw) of the induced EMF ${\cal E}$ around the rectangle at time t=2s.
- (c) Infer the induced current I from the induced EMF.

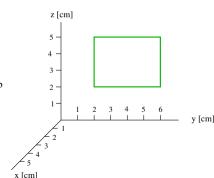




Consider a wire with a resistance per unit length of 1Ω /cm bent into a rectangular loop and placed into the yz-plane as shown. The magnetic field in the entire region is uniform and increases from zero as follows:

- $\mathbf{B} = (2\hat{\mathbf{i}} + 1\hat{\mathbf{j}} + 3\hat{\mathbf{k}})t$ T/s, where t is the time in seconds.
- (a) Find the magnetic flux Φ_B through the rectangle at time t=2s.
- (b) Find magnitude and direction (cw/ccw) of the induced EMF ${\cal E}$ around the rectangle at time t=2s.
- (c) Infer the induced current $\it I$ from the induced EMF.

(a)
$$\Phi_B = \pm (4 \text{cm})(3 \text{cm})(2 \text{T/s})(2 \text{s}) = \pm 4.8 \times 10^{-3} \text{Wb}$$



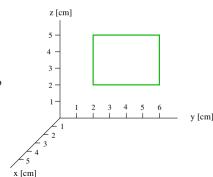


Consider a wire with a resistance per unit length of 1Ω /cm bent into a rectangular loop and placed into the yz-plane as shown. The magnetic field in the entire region is uniform and increases from zero as follows:

- $\mathbf{B} = (2\hat{\mathbf{i}} + 1\hat{\mathbf{j}} + 3\hat{\mathbf{k}})t$ T/s, where t is the time in seconds.
- (a) Find the magnetic flux Φ_B through the rectangle at time t=2s.
- (b) Find magnitude and direction (cw/ccw) of the induced EMF ${\cal E}$ around the rectangle at time t=2s.
- (c) Infer the induced current $\it I$ from the induced EMF.

(a)
$$\Phi_B = \pm (4 \text{cm})(3 \text{cm})(2 \text{T/s})(2 \text{s}) = \pm 4.8 \times 10^{-3} \text{Wb}$$

(b)
$$\mathcal{E}=\mp(4\text{cm})(3\text{cm})(2\text{T/s})=\mp2.4\text{mV}$$
 (cw)





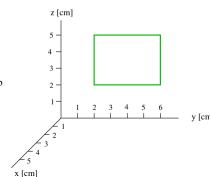
Consider a wire with a resistance per unit length of 1Ω /cm bent into a rectangular loop and placed into the yz-plane as shown. The magnetic field in the entire region is uniform and increases from zero as follows:

- $\mathbf{B} = (2\hat{\mathbf{i}} + 1\hat{\mathbf{j}} + 3\hat{\mathbf{k}})t\text{T/s}$, where t is the time in seconds.
- (a) Find the magnetic flux Φ_B through the rectangle at time t=2s.
- (b) Find magnitude and direction (cw/ccw) of the induced EMF ${\cal E}$ around the rectangle at time t=2s.
- (c) Infer the induced current $\it I$ from the induced EMF.

(a)
$$\Phi_B = \pm (4 \text{cm})(3 \text{cm})(2 \text{T/s})(2 \text{s}) = \pm 4.8 \times 10^{-3} \text{Wb}$$

(b)
$$\mathcal{E}=\mp(4\text{cm})(3\text{cm})(2\text{T/s})=\mp2.4\text{mV}$$
 (cw)

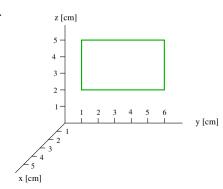
(c)
$$I = \frac{2.4 \text{mV}}{(1\Omega/\text{cm})(14\text{cm})} = 0.171 \text{mA}$$





Consider a wire with a resistance per unit length of 1Ω /cm bent into a rectangular loop and placed into the yz-plane as shown. The magnetic field in the entire region is uniform and increases from zero as follows:

- $\mathbf{B} = (3\hat{\mathbf{i}} + 1\hat{\mathbf{j}} + 2\hat{\mathbf{k}})t\mathsf{T/s}$, where t is the time in seconds.
- (a) Find the magnetic flux Φ_B through the rectangle at time t=2s.
- (b) Find magnitude and direction (cw/ccw) of the induced EMF ${\cal E}$ around the rectangle at time t=2s.
- (c) Infer the induced current I from the induced EMF.

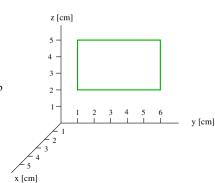




Consider a wire with a resistance per unit length of 1Ω /cm bent into a rectangular loop and placed into the yz-plane as shown. The magnetic field in the entire region is uniform and increases from zero as follows:

- $\mathbf{B} = (3\hat{\mathbf{i}} + 1\hat{\mathbf{j}} + 2\hat{\mathbf{k}})t\mathsf{T/s}$, where t is the time in seconds.
- (a) Find the magnetic flux Φ_B through the rectangle at time t=2s.
- (b) Find magnitude and direction (cw/ccw) of the induced EMF ${\cal E}$ around the rectangle at time t=2s.
- (c) Infer the induced current $\it I$ from the induced EMF.

(a)
$$\Phi_B = \pm (5 \text{cm})(3 \text{cm})(3 \text{T/s})(2 \text{s}) = \pm 9.0 \times 10^{-3} \text{Wb}$$



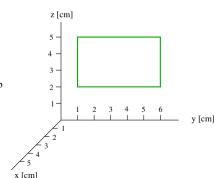


Consider a wire with a resistance per unit length of 1Ω /cm bent into a rectangular loop and placed into the yz-plane as shown. The magnetic field in the entire region is uniform and increases from zero as follows:

- $\mathbf{B} = (3\hat{\mathbf{i}} + 1\hat{\mathbf{j}} + 2\hat{\mathbf{k}})t$ T/s, where t is the time in seconds.
- (a) Find the magnetic flux Φ_B through the rectangle at time t=2s.
- (b) Find magnitude and direction (cw/ccw) of the induced EMF ${\cal E}$ around the rectangle at time t=2s.
- (c) Infer the induced current ${\it I}$ from the induced EMF.

(a)
$$\Phi_B = \pm (5 \text{cm})(3 \text{cm})(3 \text{T/s})(2 \text{s}) = \pm 9.0 \times 10^{-3} \text{Wb}$$

(b)
$$\mathcal{E} = \mp (5\text{cm})(3\text{cm})(3\text{T/s}) = \mp 4.5\text{mV}$$
 (cw)





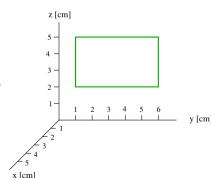
Consider a wire with a resistance per unit length of 1Ω /cm bent into a rectangular loop and placed into the yz-plane as shown. The magnetic field in the entire region is uniform and increases from zero as follows:

- $\mathbf{B} = (3\hat{\mathbf{i}} + 1\hat{\mathbf{j}} + 2\hat{\mathbf{k}})t$ T/s, where t is the time in seconds.
- (a) Find the magnetic flux Φ_B through the rectangle at time t=2s.
- (b) Find magnitude and direction (cw/ccw) of the induced EMF ${\cal E}$ around the rectangle at time t=2s.
- (c) Infer the induced current $\it I$ from the induced EMF.

(a)
$$\Phi_B = \pm (5 \text{cm})(3 \text{cm})(3 \text{T/s})(2 \text{s}) = \pm 9.0 \times 10^{-3} \text{Wb}$$

(b)
$$\mathcal{E} = \mp (5\text{cm})(3\text{cm})(3\text{T/s}) = \mp 4.5\text{mV}$$
 (cw)

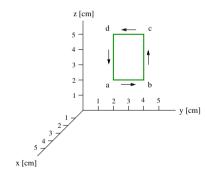
(c)
$$I = \frac{4.5 \text{mV}}{(1\Omega/\text{cm})(16\text{cm})} = 0.281 \text{mA}$$





A counterclockwise current I=1.7A [I=1.3A] is flowing through the conducting rectangular frame shown in a region of magnetic field ${\bf B}=6$ mT $\hat{\bf j}$ [${\bf B}=6$ mT $\hat{\bf k}$].

- (a) Find the force \mathbf{F}_{bc} [\mathbf{F}_{ab}] (magnitude and direction) acting on side bc [ab] of the rectangle.
- (b) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the current loop.



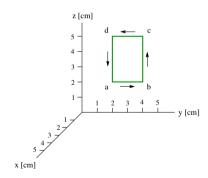


A counterclockwise current I=1.7A [I=1.3A] is flowing through the conducting rectangular frame shown in a region of magnetic field $\mathbf{B}=6$ mT $\hat{\mathbf{j}}$ [$\mathbf{B}=6$ mT $\hat{\mathbf{k}}$].

- (a) Find the force \mathbf{F}_{bc} [\mathbf{F}_{ab}] (magnitude and direction) acting on side bc [ab] of the rectangle.
- (b) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the current loop.

(a)
$$\mathbf{F}_{bc} = (1.7 \text{A})(3 \text{cm} \hat{\mathbf{k}}) \times (6 \text{mT} \hat{\mathbf{j}}) = -3.06 \times 10^{-4} \text{N} \hat{\mathbf{i}}$$

 $[\mathbf{F}_{ab} = (1.3 \text{A})(2 \text{cm} \hat{\mathbf{j}}) \times (6 \text{mT} \hat{\mathbf{k}}) = 1.56 \times 10^{-4} \text{N} \hat{\mathbf{i}}]$





A counterclockwise current I=1.7A [I=1.3A] is flowing through the conducting rectangular frame shown in a region of magnetic field ${\bf B}=6{\rm mT}{\bf \hat{j}}$ [${\bf B}=6{\rm mT\hat{k}}$].

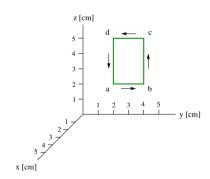
- (a) Find the force \mathbf{F}_{bc} [\mathbf{F}_{ab}] (magnitude and direction) acting on side bc [ab] of the rectangle.
- (b) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the current loop.

(a)
$$\mathbf{F}_{bc} = (1.7 \text{A})(3 \text{cm} \hat{\mathbf{k}}) \times (6 \text{mT} \hat{\mathbf{j}}) = -3.06 \times 10^{-4} \text{N} \hat{\mathbf{i}}$$

 $[\mathbf{F}_{ab} = (1.3 \text{A})(2 \text{cm} \hat{\mathbf{j}}) \times (6 \text{mT} \hat{\mathbf{k}}) = 1.56 \times 10^{-4} \text{N} \hat{\mathbf{i}}]$

(b)
$$\vec{\mu} = [(2\text{cm})(3\text{cm})\hat{\mathbf{i}}](1.7\text{A}) = 1.02 \times 10^{-3}\text{Am}^2\hat{\mathbf{i}}$$

 $[\vec{\mu} = [(2\text{cm})(3\text{cm})\hat{\mathbf{i}}](1.3\text{A}) = 7.8 \times 10^{-4}\text{Am}^2\hat{\mathbf{i}}]$





A counterclockwise current I=1.7A [I=1.3A] is flowing through the conducting rectangular frame shown in a region of magnetic field $\mathbf{B}=6$ mT $\hat{\mathbf{j}}$ [$\mathbf{B}=6$ mT $\hat{\mathbf{k}}$].

- (a) Find the force \mathbf{F}_{bc} [\mathbf{F}_{ab}] (magnitude and direction) acting on side bc [ab] of the rectangle.
- (b) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the current loop.

(a)
$$\mathbf{F}_{bc} = (1.7 \text{A})(3 \text{cm} \hat{\mathbf{k}}) \times (6 \text{mT} \hat{\mathbf{j}}) = -3.06 \times 10^{-4} \text{N} \hat{\mathbf{i}}$$

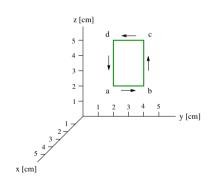
 $[\mathbf{F}_{ab} = (1.3 \text{A})(2 \text{cm} \hat{\mathbf{j}}) \times (6 \text{mT} \hat{\mathbf{k}}) = 1.56 \times 10^{-4} \text{N} \hat{\mathbf{i}}]$

(b)
$$\vec{\mu} = [(2\text{cm})(3\text{cm})\hat{\mathbf{i}}](1.7\text{A}) = 1.02 \times 10^{-3}\text{Am}^2\hat{\mathbf{i}}$$

 $[\vec{\mu} = [(2\text{cm})(3\text{cm})\hat{\mathbf{i}}](1.3\text{A}) = 7.8 \times 10^{-4}\text{Am}^2\hat{\mathbf{i}}]$

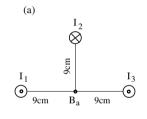
(c)
$$\vec{\tau} = (1.02 \times 10^{-3} \text{Am}^2 \hat{\mathbf{i}}) \times (6 \text{mT} \hat{\mathbf{j}}) = 6.12 \times 10^{-6} \text{Nm} \hat{\mathbf{k}}$$

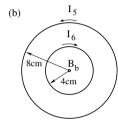
 $[\vec{\tau} = (7.8 \times 10^{-4} \text{Am}^2 \hat{\mathbf{i}}) \times (6 \text{mT} \hat{\mathbf{k}}) = -4.68 \times 10^{-6} \text{Nm} \hat{\mathbf{j}}]$





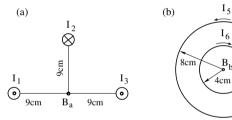
- (a) Find the magnetic field ${\bf B}_a$ (magnitude and direction) generated by the three long, straight currents $I_1=I_2=I_3=1.8$ mA [2.7mA]] in the directions shown.
- (b) Find the magnetic field \mathbf{B}_b (magnitude and direction) generated by the two circular currents $I_5 = I_6 = 1.5$ mA [2.5mA] in the directions shown.







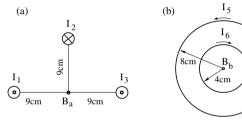
- (a) Find the magnetic field \mathbf{B}_a (magnitude and direction) generated by the three long, straight currents $I_1 = I_2 = I_3 = 1.8$ mA [2.7mA]] in the directions shown.
- (b) Find the magnetic field ${\bf B}_b$ (magnitude and direction) generated by the two circular currents $I_5=I_6=1.5$ mA [2.5mA] in the directions shown.



(a)
$$B_a=\frac{\mu_0(1.8\mathrm{mA})}{2\pi(9\mathrm{cm})}=4\times10^{-9}\mathrm{T}$$
 (directed \leftarrow)
$$[B_a=\frac{\mu_0(2.7\mathrm{mA})}{2\pi(9\mathrm{cm})}=6\times10^{-9}\mathrm{T}$$
 (directed \leftarrow)]



- (a) Find the magnetic field \mathbf{B}_a (magnitude and direction) generated by the three long, straight currents $I_1 = I_2 = I_3 = 1.8 \text{mA}$ [2.7mA]] in the directions shown.
- (b) Find the magnetic field ${\bf B}_b$ (magnitude and direction) generated by the two circular currents $I_5=I_6=1.5$ mA [2.5mA] in the directions shown.



(a)
$$B_a = \frac{\mu_0(1.8 \text{mA})}{2\pi(9 \text{cm})} = 4 \times 10^{-9} \text{T}$$
 (directed \leftarrow)
$$[B_a = \frac{\mu_0(2.7 \text{mA})}{2\pi(9 \text{cm})} = 6 \times 10^{-9} \text{T}$$
 (directed \leftarrow)]

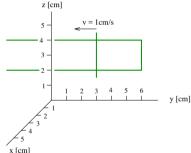
(b)
$$B_b = \frac{\mu_0(1.5 \text{mA})}{2(4 \text{cm})} - \frac{\mu_0(1.5 \text{mA})}{2(8 \text{cm})} = 1.18 \times 10^{-8} \text{T} \quad \text{(directed } \otimes \text{)}$$

$$[B_b = \frac{\mu_0(2.5 \text{mA})}{2(4 \text{cm})} - \frac{\mu_0(2.5 \text{mA})}{2(8 \text{cm})} = 1.96 \times 10^{-8} \text{T} \quad \text{(directed } \otimes \text{)}]$$



Consider a region of uniform magnetic field $\mathbf{B}=(3\hat{\mathbf{i}}+2\hat{\mathbf{j}}+1\hat{\mathbf{k}})$ mT [$\mathbf{B}=(2\hat{\mathbf{i}}+3\hat{\mathbf{j}}+1\hat{\mathbf{k}})$ mT]. A conducting rod slides along conducting rails in the yz-plane as shown. The rails are connected on the right. The clock is set to t=0 at the instant shown.

- (a) Find the magnetic flux Φ_B through the conducting loop at t=0.
- (b) Find the magnetic flux Φ_B through the conducting loop at t=1s.
- (c) Find the induced EMF.
- (d) Find the direction (cw/ccw) of the induced current.



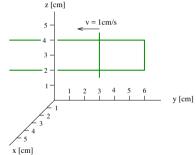


Consider a region of uniform magnetic field $\mathbf{B}=(3\hat{\mathbf{i}}+2\hat{\mathbf{j}}+1\hat{\mathbf{k}})$ mT [$\mathbf{B}=(2\hat{\mathbf{i}}+3\hat{\mathbf{j}}+1\hat{\mathbf{k}})$ mT]. A conducting rod slides along conducting rails in the yz-plane as shown. The rails are connected on the right. The clock is set to t=0 at the instant shown.

- (a) Find the magnetic flux Φ_B through the conducting loop at t=0.
- (b) Find the magnetic flux Φ_B through the conducting loop at t=1s.
- (c) Find the induced EMF.
- (d) Find the direction (cw/ccw) of the induced current.

(a)
$$\Phi_B = (3\text{cm})(2\text{cm})(3\text{mT}) = 1.8 \times 10^{-6}\text{Wb}$$

 $[\Phi_B = (3\text{cm})(2\text{cm})(2\text{mT}) = 1.2 \times 10^{-6}\text{Wb}]$





Consider a region of uniform magnetic field $\mathbf{B}=(3\hat{\mathbf{i}}+2\hat{\mathbf{j}}+1\hat{\mathbf{k}})$ mT [$\mathbf{B}=(2\hat{\mathbf{i}}+3\hat{\mathbf{j}}+1\hat{\mathbf{k}})$ mT]. A conducting rod slides along conducting rails in the yz-plane as shown. The rails are connected on the right. The clock is set to t=0 at the instant shown.

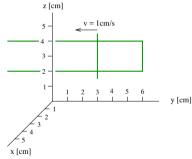
- (a) Find the magnetic flux Φ_B through the conducting loop at t=0.
- (b) Find the magnetic flux Φ_B through the conducting loop at t=1s.
- (c) Find the induced EMF.
- (d) Find the direction (cw/ccw) of the induced current.

(a)
$$\Phi_B = (3\text{cm})(2\text{cm})(3\text{mT}) = 1.8 \times 10^{-6}\text{Wb}$$

 $[\Phi_B = (3\text{cm})(2\text{cm})(2\text{mT}) = 1.2 \times 10^{-6}\text{Wb}]$

(b)
$$\Phi_B = (4\text{cm})(2\text{cm})(3\text{mT}) = 2.4 \times 10^{-6}\text{Wb}$$

 $[\Phi_B = (4\text{cm})(2\text{cm})(2\text{mT}) = 1.6 \times 10^{-6}\text{Wb}]$





Consider a region of uniform magnetic field $\mathbf{B}=(3\hat{\mathbf{i}}+2\hat{\mathbf{j}}+1\hat{\mathbf{k}})$ mT [$\mathbf{B}=(2\hat{\mathbf{i}}+3\hat{\mathbf{j}}+1\hat{\mathbf{k}})$ mT]. A conducting rod slides along conducting rails in the yz-plane as shown. The rails are connected on the right. The clock is set to t=0 at the instant shown.

- (a) Find the magnetic flux Φ_B through the conducting loop at t=0.
- (b) Find the magnetic flux Φ_B through the conducting loop at t=1s.
- (c) Find the induced EMF.
- (d) Find the direction (cw/ccw) of the induced current.

(a)
$$\Phi_B = (3\text{cm})(2\text{cm})(3\text{mT}) = 1.8 \times 10^{-6}\text{Wb}$$

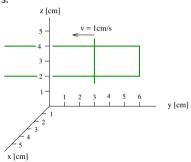
 $[\Phi_B = (3\text{cm})(2\text{cm})(2\text{mT}) = 1.2 \times 10^{-6}\text{Wb}]$

(b)
$$\Phi_B = (4\text{cm})(2\text{cm})(3\text{mT}) = 2.4 \times 10^{-6}\text{Wb}$$

 $[\Phi_B = (4\text{cm})(2\text{cm})(2\text{mT}) = 1.6 \times 10^{-6}\text{Wb}]$

(c)
$$\mathcal{E} = (1\text{cm/s})(3\text{mT})(2\text{cm}) = 6 \times 10^{-7}\text{V}$$

 $[\mathcal{E} = (1\text{cm/s})(2\text{mT})(2\text{cm}) = 4 \times 10^{-7}\text{V}]$





Consider a region of uniform magnetic field $\mathbf{B} = (3\hat{\mathbf{i}} + 2\hat{\mathbf{j}} + 1\hat{\mathbf{k}}) \mathsf{mT} [\mathbf{B} = (2\hat{\mathbf{i}} + 3\hat{\mathbf{j}} + 1\hat{\mathbf{k}}) \mathsf{mT}]$. A conducting rod slides along conducting rails in the yz-plane as shown. The rails are connected on the right. The clock is set to t=0 at the instant shown.

- (a) Find the magnetic flux Φ_R through the conducting loop at t=0.
- (b) Find the magnetic flux Φ_B through the conducting loop at t=1s.
- (c) Find the induced EMF.
- (d) Find the direction (cw/ccw) of the induced current.

Solution:

(a)
$$\Phi_B = (3\text{cm})(2\text{cm})(3\text{mT}) = 1.8 \times 10^{-6}\text{Wb}$$

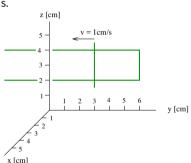
 $[\Phi_B = (3\text{cm})(2\text{cm})(2\text{mT}) = 1.2 \times 10^{-6}\text{Wb}]$

(b)
$$\Phi_B = (4cm)(2cm)(3mT) = 2.4 \times 10^{-6}Wb$$

 $[\Phi_B = (4cm)(2cm)(2mT) = 1.6 \times 10^{-6}Wb]$

(c)
$$\mathcal{E} = (1 \text{cm/s})(3 \text{mT})(2 \text{cm}) = 6 \times 10^{-7} \text{V}$$

 $[\mathcal{E} = (1 \text{cm/s})(2 \text{mT})(2 \text{cm}) = 4 \times 10^{-7} \text{V}]$



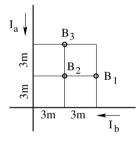
(d) cw

Unit Exam III: Problem #1 (Fall '14)



Consider two infinitely long, straight wires with currents $I_a=7$ A, $I_b=9$ A in the directions shown.

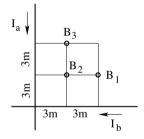
Find direction (in/out) and magnitude of the magnetic fields B_1 , B_2 , B_3 at the points marked in the graph.





Consider two infinitely long, straight wires with currents $I_a=7$ A, $I_b=9$ A in the directions shown.

Find direction (in/out) and magnitude of the magnetic fields B_1 , B_2 , B_3 at the points marked in the graph.

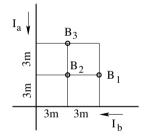


- Convention used: out = positive, in = negative
- $B_1 = \frac{\mu_0}{2\pi} \left(\frac{7A}{6m} \frac{9A}{3m} \right) = -0.367 \mu T$ (in).



Consider two infinitely long, straight wires with currents $I_a = 7A$, $I_b = 9A$ in the directions shown.

Find direction (in/out) and magnitude of the magnetic fields B_1 , B_2 , B_3 at the points marked in the graph.



Solution:

• Convention used: out = positive, in = negative

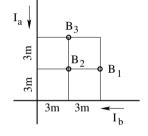
•
$$B_1 = \frac{\mu_0}{2\pi} \left(\frac{7A}{6m} - \frac{9A}{3m} \right) = -0.367 \mu T$$
 (in).

$$\begin{array}{l} \bullet \ B_1 = \frac{\mu_0}{2\pi} \left(\frac{7 \mathrm{A}}{6 \mathrm{m}} - \frac{9 \mathrm{A}}{3 \mathrm{m}} \right) = -0.367 \mu \mathrm{T} \ \text{(in)}. \\ \bullet \ B_2 = \frac{\mu_0}{2\pi} \left(\frac{7 \mathrm{A}}{3 \mathrm{m}} - \frac{9 \mathrm{A}}{3 \mathrm{m}} \right) = -0.133 \mu \mathrm{T} \ \text{(in)}. \end{array}$$



Consider two infinitely long, straight wires with currents $I_a = 7A$, $I_b = 9A$ in the directions shown.

Find direction (in/out) and magnitude of the magnetic fields B_1 , B_2 , B_3 at the points marked in the graph.



Solution:

• Convention used: out = positive, in = negative

•
$$B_1 = \frac{\mu_0}{2\pi} \left(\frac{7A}{6m} - \frac{9A}{3m} \right) = -0.367 \mu T$$
 (in).

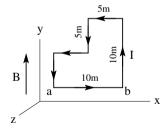
•
$$B_2 = \frac{\mu_0}{2\pi} \left(\frac{7A}{3m} - \frac{9A}{3m} \right) = -0.133 \mu T$$
 (in).

•
$$B_2 = \frac{\mu_0}{2\pi} \left(\frac{7A}{3m} - \frac{9A}{3m} \right) = -0.133 \mu T$$
 (in).
• $B_3 = \frac{\mu_0}{2\pi} \left(\frac{7A}{3m} - \frac{9A}{6m} \right) = +0.167 \mu T$ (out).



Consider the (piecewise rectangular) conducting loop in the xy-plane as shown with a counterclockwise current I=4A in a uniform magnetic field $\vec{B}=2T\hat{j}$.

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F} (magnitude and direction) acting on the side ab of the rectangle.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

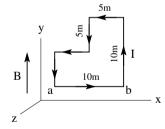




Consider the (piecewise rectangular) conducting loop in the xy-plane as shown with a counterclockwise current I=4A in a uniform magnetic field $\vec{B}=2T\hat{j}$.

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F} (magnitude and direction) acting on the side ab of the rectangle.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

(a)
$$\vec{\mu} = (4A)(75m^2)\hat{k} = 300Am^2\hat{k}$$
.



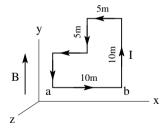


Consider the (piecewise rectangular) conducting loop in the xy-plane as shown with a counterclockwise current I=4A in a uniform magnetic field $\vec{B}=2T\hat{j}$.

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F} (magnitude and direction) acting on the side ab of the rectangle.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

(a)
$$\vec{\mu} = (4A)(75m^2)\hat{k} = 300Am^2\hat{k}$$
.

(b)
$$\vec{F} = I\vec{L} \times \vec{B} = (4A)(10m\hat{i}) \times (2T\hat{j}) = 80N\hat{k}$$
.





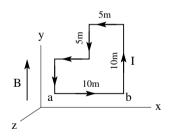
Consider the (piecewise rectangular) conducting loop in the xy-plane as shown with a counterclockwise current I=4A in a uniform magnetic field $\vec{B}=2T\hat{j}$.

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F} (magnitude and direction) acting on the side ab of the rectangle.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

(a)
$$\vec{\mu} = (4A)(75m^2)\hat{k} = 300Am^2\hat{k}$$
.

(b)
$$\vec{F} = I\vec{L} \times \vec{B} = (4A)(10\text{m}\hat{i}) \times (2\text{T}\hat{j}) = 80\text{N}\hat{k}$$
.

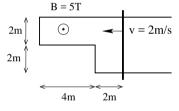
(c)
$$\vec{\tau} = \vec{\mu} \times \vec{B} = (300 \text{Am}^2 \hat{k}) \times (2T\hat{j}) = -600 \text{Nm} \hat{i}$$





A conducting frame with a moving conducting rod is located in a uniform magnetic field directed out of the plane as shown. The rod moves at constant velocity.

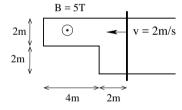
- (a) Find the magnetic flux Φ_B through the frame and the induced emf $\mathcal E$ around the frame at the instant shown.
- (b) Find the magnetic flux Φ_B through the frame and the induced emf \mathcal{E} around the frame two seconds later. Write magnitudes only (in SI units), no directions.





A conducting frame with a moving conducting rod is located in a uniform magnetic field directed out of the plane as shown. The rod moves at constant velocity.

- (a) Find the magnetic flux Φ_B through the frame and the induced emf $\mathcal E$ around the frame at the instant shown.
- (b) Find the magnetic flux Φ_B through the frame and the induced emf \mathcal{E} around the frame two seconds later. Write magnitudes only (in SI units), no directions.

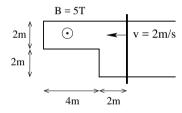


(a)
$$\Phi_B = (16m^2)(5T) = 80Wb$$
, $\mathcal{E} = (2m/s)(5T)(4m) = 40V$.



A conducting frame with a moving conducting rod is located in a uniform magnetic field directed out of the plane as shown. The rod moves at constant velocity.

- (a) Find the magnetic flux Φ_B through the frame and the induced emf $\mathcal E$ around the frame at the instant shown.
- (b) Find the magnetic flux Φ_B through the frame and the induced emf \mathcal{E} around the frame two seconds later. Write magnitudes only (in SI units), no directions.



(a)
$$\Phi_B = (16m^2)(5T) = 80Wb$$
, $\mathcal{E} = (2m/s)(5T)(4m) = 40V$.

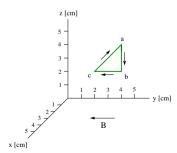
(b)
$$\Phi_B = (4m^2)(5T) = 20Wb$$
, $\mathcal{E} = (2m/s)(5T)(2m) = 20V$.



A clockwise current I=2.1A is flowing around the conducting triangular frame shown in a region of uniform magnetic field $\vec{B}=-3$ m $\hat{\mathbf{I}}$.

- (a) Find the force \vec{F}_{ab} acting on side ab of the triangle.
- (b) Find the force \vec{F}_{bc} acting on side bc of the triangle.
- (c) Find the magnetic moment $\vec{\mu}$ of the current loop.
- (d) Find the torque $\vec{\tau}$ acting on the current loop.

Remember that vectors have components or magnitude and direction.



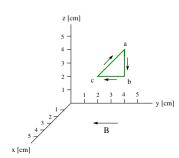


A clockwise current I=2.1A is flowing around the conducting triangular frame shown in a region of uniform magnetic field $\vec{B}=-3$ m $\hat{\mathbf{I}}$ i.

- (a) Find the force \vec{F}_{ab} acting on side ab of the triangle.
- (b) Find the force \vec{F}_{bc} acting on side bc of the triangle.
- (c) Find the magnetic moment $\vec{\mu}$ of the current loop.
- (d) Find the torque $\vec{\tau}$ acting on the current loop.

Remember that vectors have components or magnitude and direction.

(a)
$$\vec{F}_{ab} = (2.1 \text{A}) (-2 \text{cm} \hat{\mathbf{k}}) \times (-3 \text{mT} \hat{\mathbf{j}}) = -1.26 \times 10^{-4} \text{N} \hat{\mathbf{i}}.$$





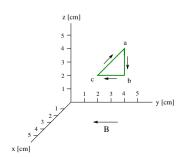
A clockwise current I=2.1A is flowing around the conducting triangular frame shown in a region of uniform magnetic field $\vec{B}=-3$ m $\hat{\bf r}_{\bf i}$.

- (a) Find the force \vec{F}_{ab} acting on side ab of the triangle.
- (b) Find the force \vec{F}_{bc} acting on side bc of the triangle.
- (c) Find the magnetic moment $\vec{\mu}$ of the current loop.
- (d) Find the torque $\vec{\tau}$ acting on the current loop.

Remember that vectors have components or magnitude and direction.

(a)
$$\vec{F}_{ab} = (2.1\text{A})(-2\text{cm}\hat{\mathbf{k}}) \times (-3\text{mT}\hat{\mathbf{j}}) = -1.26 \times 10^{-4}\text{N}\hat{\mathbf{i}}.$$

(b)
$$\vec{F}_{bc} = 0$$
.





A clockwise current I=2.1A is flowing around the conducting triangular frame shown in a region of uniform magnetic field $\vec{B}=-3$ m $\hat{\mathbf{I}}$ i.

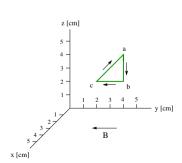
- (a) Find the force \vec{F}_{ab} acting on side ab of the triangle.
- (b) Find the force \vec{F}_{bc} acting on side bc of the triangle.
- (c) Find the magnetic moment $\vec{\mu}$ of the current loop.
- (d) Find the torque $\vec{\tau}$ acting on the current loop.

Remember that vectors have components or magnitude and direction.

(a)
$$\vec{F}_{ab} = (2.1\text{A})(-2\text{cm}\hat{\mathbf{k}}) \times (-3\text{mT}\hat{\mathbf{j}}) = -1.26 \times 10^{-4}\text{N}\hat{\mathbf{i}}.$$

(b)
$$\vec{F}_{bc} = 0$$
.

(c)
$$\vec{\mu} = \left[-\frac{1}{2} (2\text{cm}) (2\text{cm}) \hat{\mathbf{i}} \right] (2.1\text{A}) = -4.2 \times 10^{-4} \text{Am}^2 \hat{\mathbf{i}}.$$





A clockwise current I=2.1A is flowing around the conducting triangular frame shown in a region of uniform magnetic field $\vec{B}=-3$ m $\hat{\bf T}_{\bf i}$.

- (a) Find the force \vec{F}_{ab} acting on side ab of the triangle.
- (b) Find the force \vec{F}_{bc} acting on side bc of the triangle.
- (c) Find the magnetic moment $\vec{\mu}$ of the current loop.
- (d) Find the torque $\vec{\tau}$ acting on the current loop.

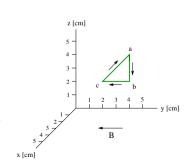
Remember that vectors have components or magnitude and direction.

(a)
$$\vec{F}_{ab} = (2.1\text{A})(-2\text{cm}\hat{\mathbf{k}}) \times (-3\text{mT}\hat{\mathbf{j}}) = -1.26 \times 10^{-4}\text{N}\hat{\mathbf{i}}.$$

(b)
$$\vec{F}_{bc} = 0$$
.

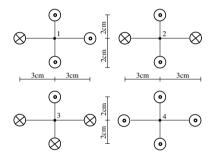
(c)
$$\vec{\mu} = \left[-\frac{1}{2} (2\text{cm})(2\text{cm}) \hat{\mathbf{i}} \right] (2.1\text{A}) = -4.2 \times 10^{-4} \text{Am}^2 \hat{\mathbf{i}}.$$

(d)
$$\vec{\tau} = (-4.2 \times 10^{-4} Am^2 \hat{\mathbf{i}}) \times (-3mT \hat{\mathbf{j}}) = 1.26 \times 10^{-6} Nm \hat{\mathbf{k}}.$$





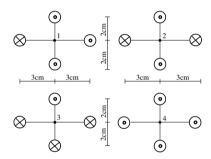
Consider four long, straight currents in four different configurations. All currents are I=4mA in the directions shown ($\otimes=$ in, $\odot=$ out). Find the magnitude (in SI units) and the direction ($\leftarrow,\rightarrow,\uparrow,\downarrow$) of the magnetic fields ${\bf B}_1,{\bf B}_2,{\bf B}_3,{\bf B}_4$ generated at the points $1,\ldots,4$, respectively.





Consider four long, straight currents in four different configurations. All currents are I=4mA in the directions shown ($\otimes=$ in, $\odot=$ out). Find the magnitude (in SI units) and the direction ($\leftarrow,\rightarrow,\uparrow,\downarrow$) of the magnetic fields ${\bf B_1},{\bf B_2},{\bf B_3},{\bf B_4}$ generated at the points 1,...,4, respectively.

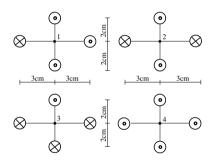
•
$$B_1 = 2 \, \frac{\mu_0(4 \text{mA})}{2\pi (3 \text{cm})} = 5.33 \times 10^{-8} \text{T}$$
 (directed \downarrow).





Consider four long, straight currents in four different configurations. All currents are I=4mA in the directions shown ($\otimes=$ in, $\odot=$ out). Find the magnitude (in SI units) and the direction ($\leftarrow,\rightarrow,\uparrow,\downarrow$) of the magnetic fields $\mathbf{B}_1,\mathbf{B}_2,\mathbf{B}_3,\mathbf{B}_4$ generated at the points $1,\ldots,4$, respectively.

- $B_1 = 2 \, \frac{\mu_0(4 {
 m mA})}{2\pi (3 {
 m cm})} = 5.33 \times 10^{-8} {
 m T} \quad \mbox{(directed \downarrow)}.$
- $B_2 = 0$ (no direction).

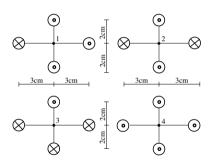




Consider four long, straight currents in four different configurations. All currents are I=4mA in the directions shown ($\otimes=$ in, $\odot=$ out). Find the magnitude (in SI units) and the direction ($\leftarrow,\rightarrow,\uparrow,\downarrow$) of the magnetic fields ${\bf B}_1,{\bf B}_2,{\bf B}_3,{\bf B}_4$ generated at the points $1,\ldots,4$, respectively.

•
$$B_1 = 2 \frac{\mu_0(4\text{mA})}{2\pi(3\text{cm})} = 5.33 \times 10^{-8}\text{T}$$
 (directed \downarrow).

- $B_2 = 0$ (no direction).
- $B_3 = 2 \frac{\mu_0(4\text{mA})}{2\pi(2\text{cm})} = 8.00 \times 10^{-8}\text{T}$ (directed \to).

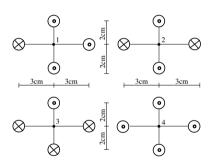




Consider four long, straight currents in four different configurations. All currents are I=4mA in the directions shown ($\otimes=$ in, $\odot=$ out). Find the magnitude (in SI units) and the direction (\leftarrow , \rightarrow , \uparrow , \downarrow) of the magnetic fields \mathbf{B}_1 , \mathbf{B}_2 , \mathbf{B}_3 , \mathbf{B}_4 generated at the points 1,...,4, respectively.

•
$$B_1 = 2 \frac{\mu_0(4\text{mA})}{2\pi(3\text{cm})} = 5.33 \times 10^{-8}\text{T}$$
 (directed \downarrow).

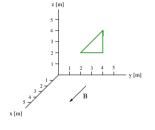
- $B_2 = 0$ (no direction).
- $B_3 = 2 \frac{\mu_0(4\text{mA})}{2\pi(2\text{cm})} = 8.00 \times 10^{-8}\text{T}$ (directed \to).
- $B_4 = 0$ (no direction).

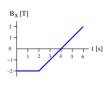




A wire shaped into a triangle has resistance $R=3.5\Omega$ and is placed in the yz-plane as shown. A uniform time-dependent magnetic field $\mathbf{B}=B_x(t)\hat{\mathbf{i}}$ is present. The dependence of B_x on time is shown graphically.

- (a) Find magnitude $|\Phi_B^{(1)}|$ and $|\Phi_B^{(4)}|$ of the magnetic flux through the triangle at times t=1s and t=4s, respectively.
- (b) Find magnitude I_1 , I_4 and direction (cw/ccw) of the induced current at times t=1s and t=4s, respectively.



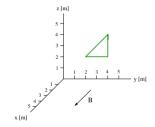


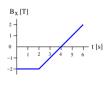


A wire shaped into a triangle has resistance $R=3.5\Omega$ and is placed in the yz-plane as shown. A uniform time-dependent magnetic field $\mathbf{B}=B_x(t)\hat{\mathbf{i}}$ is present. The dependence of B_x on time is shown graphically.

- (a) Find magnitude $|\Phi_B^{(1)}|$ and $|\Phi_B^{(4)}|$ of the magnetic flux through the triangle at times t=1s and t=4s, respectively.
- (b) Find magnitude I_1 , I_4 and direction (cw/ccw) of the induced current at times t=1s and t=4s, respectively.

(a)
$$|\Phi_B^{(1)}| = |(2m^2)(-2T)| = 4.0 \,\text{Wb},$$
 $|\Phi_B^{(4)}| = |(2m^2)(0T) = 0.$







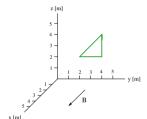
A wire shaped into a triangle has resistance $R=3.5\Omega$ and is placed in the yz-plane as shown. A uniform time-dependent magnetic field $\mathbf{B}=B_x(t)\hat{\mathbf{i}}$ is present. The dependence of B_x on time is shown graphically.

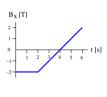
- (a) Find magnitude $|\Phi_B^{(1)}|$ and $|\Phi_B^{(4)}|$ of the magnetic flux through the triangle at times t=1s and t=4s, respectively.
- (b) Find magnitude I_1 , I_4 and direction (cw/ccw) of the induced current at times t=1s and t=4s, respectively.

(a)
$$|\Phi_B^{(1)}| = |(2m^2)(-2T)| = 4.0 \,\text{Wb},$$
 $|\Phi_B^{(4)}| = |(2m^2)(0T) = 0.$

(b)
$$\left| \frac{d\Phi_B^{(1)}}{dt} \right| = \left| A \frac{dB}{dt} \right| = |(2\text{m}^2)(0\text{T/s}) = 0$$

 $\Rightarrow I_1 = 0,$
 $\left| \frac{d\Phi_B^{(4)}}{dt} \right| = \left| A \frac{dB}{dt} \right| = |(2\text{m}^2)(1\text{T/s})| = 2.0\text{V}$
 $\Rightarrow I_4 = \frac{2.0\text{V}}{3.5\Omega} = 0.571\text{A}$ (cw).

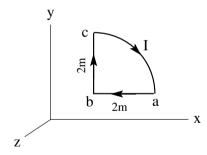






Consider a region with uniform magnetic field (i) $\vec{B} = 5T\hat{i}$, (ii) $\vec{B} = -6T\hat{i}$. A conducting loop in the xy-plane has the shape of a quarter circle with a clockwise current (i) I = 4A, (ii) I = 3A.

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F} (magnitude and direction) acting on the side (i) ab, (ii) bc of the loop.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

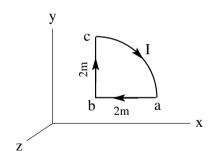




Consider a region with uniform magnetic field (i) $\vec{B} = 5T\hat{j}$, (ii) $\vec{B} = -6T\hat{i}$. A conducting loop in the xy-plane has the shape of a quarter circle with a clockwise current (i) I = 4A, (ii) I = 3A.

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F} (magnitude and direction) acting on the side (i) ab, (ii) bc of the loop.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

(ia)
$$\vec{\mu} = (4A)(3.14m^2)(-\hat{k}) = -12.6Am^2\hat{k}$$
.

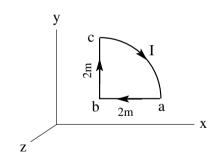




Consider a region with uniform magnetic field (i) $\vec{B} = 5T_1^2$, (ii) $\vec{B} = -6T_1^2$. A conducting loop in the xy-plane has the shape of a quarter circle with a clockwise current (i) I=4A, (ii) I=3A.

- (a) Find the magnetic moment \vec{u} (magnitude and direction) of the loop.
- (b) Find the force \vec{F} (magnitude and direction) acting on the side (i) ab, (ii) bc of the loop.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

- (ia) $\vec{\mu} = (4A)(3.14m^2)(-\hat{k}) = -12.6Am^2\hat{k}$. (ib) $\vec{F}_{ab} = (4A)(-2m\hat{i}) \times (5T\hat{j}) = -40N\hat{k}$.





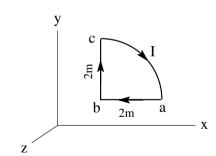
Consider a region with uniform magnetic field (i) $\vec{B} = 5T\hat{j}$, (ii) $\vec{B} = -6T\hat{i}$. A conducting loop in the xy-plane has the shape of a quarter circle with a clockwise current (i) I = 4A, (ii) I = 3A.

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F} (magnitude and direction) acting on the side (i) ab, (ii) bc of the loop.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

(ia)
$$\vec{\mu} = (4A)(3.14m^2)(-\hat{k}) = -12.6Am^2\hat{k}$$
.

(ib)
$$\vec{F}_{ab} = (4A)(-2m\hat{i}) \times (5T\hat{j}) = -40N\hat{k}$$
.

(ic)
$$\vec{\tau} = (-12.6 \text{Am}^2 \hat{k}) \times (5 \text{T} \hat{j}) = 63.0 \text{Nm} \hat{i}$$





Consider a region with uniform magnetic field (i) $\vec{B} = 5T\hat{j}$, (ii) $\vec{B} = -6T\hat{i}$. A conducting loop in the xy-plane has the shape of a quarter circle with a clockwise current (i) I = 4A, (ii) I = 3A.

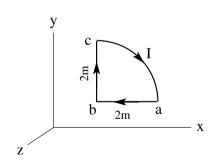
- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F} (magnitude and direction) acting on the side (i) ab, (ii) bc of the loop.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

(ia)
$$\vec{\mu} = (4A)(3.14m^2)(-\hat{k}) = -12.6Am^2\hat{k}$$
.

(ib)
$$\vec{F}_{ab} = (4A)(-2m\hat{i}) \times (5T\hat{j}) = -40N\hat{k}$$
.

(ic)
$$\vec{\tau} = (-12.6 \text{Am}^2 \hat{k}) \times (5 \text{T} \hat{j}) = 63.0 \text{Nm} \hat{i}$$

(iia)
$$\vec{\mu} = (3A)(3.14m^2)(-\hat{k}) = -9.42Am^2\hat{k}$$
.





Consider a region with uniform magnetic field (i) $\vec{B}=5T\hat{j}$, (ii) $\vec{B}=-6T\hat{i}$. A conducting loop in the xy-plane has the shape of a quarter circle with a clockwise current (i) I=4A, (ii) I=3A.

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F} (magnitude and direction) acting on the side (i) ab, (ii) bc of the loop.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

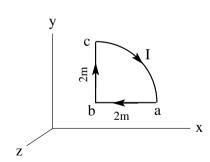
(ia)
$$\vec{\mu} = (4A)(3.14m^2)(-\hat{k}) = -12.6Am^2\hat{k}$$
.

(ib)
$$\vec{F}_{ab} = (4A)(-2m\hat{i}) \times (5T\hat{j}) = -40N\hat{k}$$
.

(ic)
$$\vec{\tau} = (-12.6 \text{Am}^2 \hat{k}) \times (5 \text{T} \hat{j}) = 63.0 \text{Nm} \hat{i}$$

(iia)
$$\vec{\mu} = (3A)(3.14m^2)(-\hat{k}) = -9.42Am^2\hat{k}$$
.

(iib)
$$\vec{F}_{bc} = (3A)(2m\hat{j}) \times (-6T\hat{i}) = 36N\hat{k}$$
.





Consider a region with uniform magnetic field (i) $\vec{B}=5T\hat{j}$, (ii) $\vec{B}=-6T\hat{i}$. A conducting loop in the xy-plane has the shape of a quarter circle with a clockwise current (i) I=4A, (ii) I=3A.

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F} (magnitude and direction) acting on the side (i) ab, (ii) bc of the loop.
- (c) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

(ia)
$$\vec{\mu} = (4A)(3.14m^2)(-\hat{k}) = -12.6Am^2\hat{k}$$
.

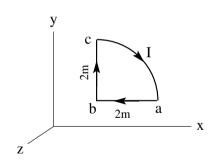
(ib)
$$\vec{F}_{ab} = (4A)(-2m\hat{i}) \times (5T\hat{j}) = -40N\hat{k}$$
.

(ic)
$$\vec{\tau} = (-12.6 \text{Am}^2 \hat{k}) \times (5 \text{T} \hat{j}) = 63.0 \text{Nm} \hat{i}$$

(iia)
$$\vec{\mu} = (3A)(3.14m^2)(-\hat{k}) = -9.42Am^2\hat{k}$$
.

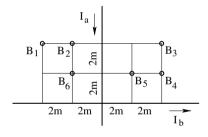
(iib)
$$\vec{F}_{bc} = (3A)(2m\hat{j}) \times (-6T\hat{i}) = 36N\hat{k}$$
.

(iic)
$$\vec{\tau} = (-9.42 \text{Am}^2 \hat{k}) \times (-6 \text{T} \hat{i}) = 56.5 \text{Nm} \hat{j}$$





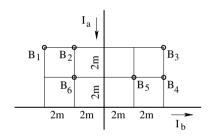
Consider two infinitely long, straight wires with currents of equal magnitude $I_a = I_b = 6$ A in the directions shown. Find direction (in/out) and magnitude of the magnetic fields \mathbf{B}_1 , ..., \mathbf{B}_6 at the points marked in the graph.





Consider two infinitely long, straight wires with currents of equal magnitude $I_a = I_b = 6$ A in the directions shown. Find direction (in/out) and magnitude of the magnetic fields \mathbf{B}_1 , ..., \mathbf{B}_6 at the points marked in the graph.

•
$$B_1=rac{\mu_0}{2\pi}\left(rac{6A}{4m}-rac{6A}{4m}
ight)=0$$
 (no direction).

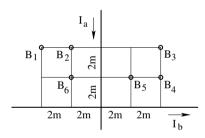




Consider two infinitely long, straight wires with currents of equal magnitude $I_a = I_b = 6$ A in the directions shown. Find direction (in/out) and magnitude of the magnetic fields \mathbf{B}_1 , ..., \mathbf{B}_6 at the points marked in the graph.

•
$$B_1=rac{\mu_0}{2\pi}\left(rac{6\mathrm{A}}{4\mathrm{m}}-rac{6\mathrm{A}}{4\mathrm{m}}
ight)=0$$
 (no direction).

•
$$B_2 = \frac{\mu_0}{2\pi} \left(\frac{6A}{4m} - \frac{6A}{2m} \right) = -0.3 \mu T$$
 (into plane).



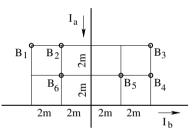


Consider two infinitely long, straight wires with currents of equal magnitude $I_a = I_b = 6A$ in the directions shown. Find direction (in/out) and magnitude of the magnetic fields \mathbf{B}_1 , ..., \mathbf{B}_6 at the points marked in the graph.

•
$$B_1=rac{\mu_0}{2\pi}\left(rac{6\mathrm{A}}{4\mathrm{m}}-rac{6\mathrm{A}}{4\mathrm{m}}
ight)=0$$
 (no direction).

•
$$B_2=rac{\mu_0}{2\pi}\left(rac{6A}{4m}-rac{6A}{2m}
ight)=-0.3\mu T$$
 (into plane).

•
$$B_3 = \frac{\mu_0}{2\pi} \left(\frac{6A}{4m} + \frac{6A}{4m} \right) = +0.6 \mu T$$
 (out of plane).





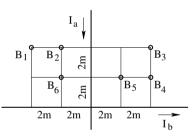
Consider two infinitely long, straight wires with currents of equal magnitude $I_a = I_b = 6A$ in the directions shown. Find direction (in/out) and magnitude of the magnetic fields \mathbf{B}_1 , ..., \mathbf{B}_6 at the points marked in the graph.

•
$$B_1=rac{\mu_0}{2\pi}\left(rac{6\mathrm{A}}{4\mathrm{m}}-rac{6\mathrm{A}}{4\mathrm{m}}
ight)=0$$
 (no direction).

•
$$B_2=rac{\mu_0}{2\pi}\left(rac{6\mathrm{A}}{4\mathrm{m}}-rac{6\mathrm{A}}{2\mathrm{m}}
ight)=-0.3\mu\mathrm{T}$$
 (into plane).

•
$$B_3=rac{\mu_0}{2\pi}\left(rac{6\mathrm{A}}{4\mathrm{m}}+rac{6\mathrm{A}}{4\mathrm{m}}
ight)=+0.6\mu\mathrm{T}$$
 (out of plane).

•
$$B_4=rac{\mu_0}{2\pi}\left(rac{6\mathrm{A}}{2\mathrm{m}}+rac{6\mathrm{A}}{4\mathrm{m}}
ight)=0.9\mu\mathrm{T}$$
 (out of plane).





Consider two infinitely long, straight wires with currents of equal magnitude $I_a = I_b = 6$ A in the directions shown. Find direction (in/out) and magnitude of the magnetic fields \mathbf{B}_1 , ..., \mathbf{B}_6 at the points marked in the graph.

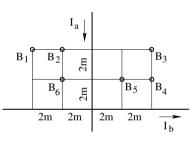
•
$$B_1=rac{\mu_0}{2\pi}\left(rac{6\mathrm{A}}{4\mathrm{m}}-rac{6\mathrm{A}}{4\mathrm{m}}
ight)=0$$
 (no direction).

•
$$B_2=rac{\mu_0}{2\pi}\left(rac{6\mathrm{A}}{4\mathrm{m}}-rac{6\mathrm{A}}{2\mathrm{m}}
ight)=-0.3\mu\mathrm{T}$$
 (into plane).

•
$$B_3=rac{\mu_0}{2\pi}\left(rac{6\mathrm{A}}{4\mathrm{m}}+rac{6\mathrm{A}}{4\mathrm{m}}
ight)=+0.6\mu\mathrm{T}$$
 (out of plane).

•
$$B_4=rac{\mu_0}{2\pi}\left(rac{6A}{2m}+rac{6A}{4m}
ight)=0.9\mu T$$
 (out of plane).

•
$$B_5=rac{\mu_0}{2\pi}\left(rac{6\mathrm{A}}{2\mathrm{m}}+rac{6\mathrm{A}}{2\mathrm{m}}
ight)=1.2\mu\mathrm{T}$$
 (out of plane).





Consider two infinitely long, straight wires with currents of equal magnitude $I_a = I_b = 6$ A in the directions shown. Find direction (in/out) and magnitude of the magnetic fields \mathbf{B}_1 , ..., \mathbf{B}_6 at the points marked in the graph.

•
$$B_1=rac{\mu_0}{2\pi}\left(rac{6\mathrm{A}}{4\mathrm{m}}-rac{6\mathrm{A}}{4\mathrm{m}}
ight)=0$$
 (no direction).

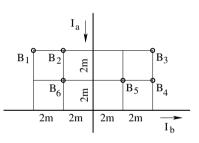
•
$$B_2=rac{\mu_0}{2\pi}\left(rac{6A}{4m}-rac{6A}{2m}
ight)=-0.3\mu T$$
 (into plane).

•
$$B_3=rac{\mu_0}{2\pi}\left(rac{6\mathrm{A}}{4\mathrm{m}}+rac{6\mathrm{A}}{4\mathrm{m}}
ight)=+0.6\mu\mathrm{T}$$
 (out of plane).

•
$$B_4=rac{\mu_0}{2\pi}\left(rac{6\mathrm{A}}{2\mathrm{m}}+rac{6\mathrm{A}}{4\mathrm{m}}
ight)=0.9\mu\mathrm{T}$$
 (out of plane).

•
$$B_5=rac{\mu_0}{2\pi}\left(rac{6\mathrm{A}}{2\mathrm{m}}+rac{6\mathrm{A}}{2\mathrm{m}}
ight)=1.2\mu\mathrm{T}$$
 (out of plane).

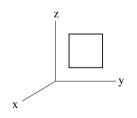
•
$$B_6 = \frac{\mu_0}{2\pi} \left(\frac{6A}{2m} - \frac{6A}{2m} \right) = 0$$
 (no direction).

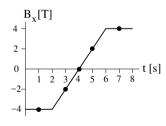




A conducting wire bent into a square of side (i) 1.2m, (ii) 1.3m is placed in the yz-plane. The time-dependence of the magnetic field $\mathbf{B}(t) = B_x(t)\hat{\mathbf{i}}$ is shown graphically.

- (a) Find the magnitude $|\Phi_B|$ of the magnetic flux through the square at times (i) t=1s, t=3s, and t=4s, (ii) t=4s, t=5s, and t=7s.
- (b) Find the magnitude $|\mathcal{E}|$ of the induced EMF at the above times.
- (c) Find the direction (cw, ccw, zero) of the induced current at the above times.







(ia)
$$|\Phi_B^{(1)}| = (1.44\text{m}^2)(4\text{T}) = 5.76\,\text{Wb}$$

$$|\Phi_B^{(3)}| = (1.44 \text{m}^2)(2\text{T}) = 2.88 \,\text{Wb}$$

$$|\Phi_B^{(4)}| = (1.44 \text{m}^2)(0\text{T}) = 0$$



(ia)
$$|\Phi_B^{(1)}| = (1.44\text{m}^2)(4\text{T}) = 5.76\,\text{Wb}$$

$$|\Phi_B^{(3)}| = (1.44 \text{m}^2)(2\text{T}) = 2.88 \, \text{Wb}$$

$$|\Phi_B^{(4)}| = (1.44 \text{m}^2)(0\text{T}) = 0$$

(ib)
$$\mathcal{E}^{(1)} = (1.44 m^2)(0 T/s) = 0$$

$$\mathcal{E}^{(3)} = (1.44 m^2)(2T/s) = 2.88 V$$

$$\mathcal{E}^{(4)} = (1.44 m^2)(2T/s) = 2.88 V$$



Solution:

(ia)
$$|\Phi_B^{(1)}| = (1.44\text{m}^2)(4\text{T}) = 5.76\,\text{Wb}$$

$$|\Phi_B^{(3)}| = (1.44 \text{m}^2)(2\text{T}) = 2.88 \, \text{Wb}$$

$$|\Phi_B^{(4)}| = (1.44 \text{m}^2)(0\text{T}) = 0$$

(ib)
$$\mathcal{E}^{(1)} = (1.44m^2)(0T/s) = 0$$

$$\mathcal{E}^{(3)} = (1.44 m^2)(2T/s) = 2.88 V$$

$$\mathcal{E}^{(4)} = (1.44 \text{m}^2)(2\text{T/s}) = 2.88\text{V}$$

(ic) zero, cw, cw



(ia)
$$|\Phi_B^{(1)}| = (1.44\text{m}^2)(4\text{T}) = 5.76\,\text{Wb}$$

$$|\Phi_B^{(3)}| = (1.44 \text{m}^2)(2\text{T}) = 2.88 \,\text{Wb}$$

$$|\Phi_B^{(4)}| = (1.44 \text{m}^2)(0\text{T}) = 0$$

(ib)
$$\mathcal{E}^{(1)} = (1.44 m^2)(0 T/s) = 0$$

$$\mathcal{E}^{(3)} = (1.44 \text{m}^2)(2\text{T/s}) = 2.88\text{V}$$

$$\mathcal{E}^{(4)} = (1.44 \text{m}^2)(2\text{T/s}) = 2.88\text{V}$$

(iia)
$$|\Phi_p^{(4)}| = (1.69 \text{m}^2)(0\text{T}) = 0$$

$$|\Phi_B^{(5)}| = (1.69 \text{m}^2)(2\text{T}) = 3.38 \, \text{Wb}$$

$$|\Phi_B^{(7)}| = (1.69 \text{m}^2)(4\text{T}) = 6.76 \,\text{Wb}$$



(ia)
$$|\Phi_B^{(1)}| = (1.44\text{m}^2)(4\text{T}) = 5.76\,\text{Wb}$$

$$|\Phi_B^{(3)}| = (1.44 \text{m}^2)(2\text{T}) = 2.88 \,\text{Wb}$$

$$|\Phi_B^{(4)}| = (1.44 \text{m}^2)(0\text{T}) = 0$$

(ib)
$$\mathcal{E}^{(1)} = (1.44 \text{m}^2)(0 \text{T/s}) = 0$$

$$\mathcal{E}^{(3)} = (1.44 \text{m}^2)(2\text{T/s}) = 2.88\text{V}$$

$$\mathcal{E}^{(4)} = (1.44 \text{m}^2)(2\text{T/s}) = 2.88\text{V}$$

(iia)
$$|\Phi_{R}^{(4)}| = (1.69 \text{m}^2)(0\text{T}) = 0$$

$$|\Phi_B^{(5)}| = (1.69 \text{m}^2)(2\text{T}) = 3.38 \,\text{Wb}$$

$$|\Phi_B^{(7)}| = (1.69 \text{m}^2)(4\text{T}) = 6.76 \,\text{Wb}$$

(iib)
$$\mathcal{E}^{(4)} = (1.69 \text{m}^2)(2\text{T/s}) = 3.38\text{V}$$

$$\mathcal{E}^{(5)} = (1.69 \text{m}^2)(2\text{T/s}) = 3.38\text{V}$$

$$\mathcal{E}^{(7)} = (1.69 \text{m}^2)(0\text{T/s}) = 0$$



(ia)
$$|\Phi_B^{(1)}| = (1.44\text{m}^2)(4\text{T}) = 5.76\,\text{Wb}$$

$$|\Phi_B^{(3)}| = (1.44 \text{m}^2)(2\text{T}) = 2.88 \,\text{Wb}$$

$$|\Phi_B^{(4)}| = (1.44 \text{m}^2)(0\text{T}) = 0$$

(ib)
$$\mathcal{E}^{(1)} = (1.44 \text{m}^2)(0 \text{T/s}) = 0$$

$$\mathcal{E}^{(3)} = (1.44 \text{m}^2)(2\text{T/s}) = 2.88\text{V}$$

$$\mathcal{E}^{(4)} = (1.44 \text{m}^2)(2\text{T/s}) = 2.88\text{V}$$

(iia)
$$|\Phi_{R}^{(4)}| = (1.69 \text{m}^2)(0\text{T}) = 0$$

$$|\Phi_B^{(5)}| = (1.69 \text{m}^2)(2\text{T}) = 3.38 \,\text{Wb}$$

$$|\Phi_B^{(7)}| = (1.69 \text{m}^2)(4\text{T}) = 6.76 \,\text{Wb}$$

(iib)
$$\mathcal{E}^{(4)} = (1.69 \text{m}^2)(2\text{T/s}) = 3.38\text{V}$$

$$\mathcal{E}^{(5)} = (1.69 \text{m}^2)(2\text{T/s}) = 3.38\text{V}$$

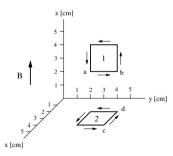
$$\mathcal{E}^{(7)} = (1.69 \text{m}^2)(0\text{T/s}) = 0$$



Conducting squares 1 and 2, each of side 2cm, are positioned as shown. A current I=3A is flowing around each square in the direction shown. A uniform magnetic field $\vec{B}=5\text{mT}\hat{\mathbf{k}}$ exists in the entire region.

- (a) Find the forces \vec{F}_{ab} and \vec{F}_{cd} acting on sides ab and cd, respectively.
- (b) Find the magnetic moments $\vec{\mu}_1$ and $\vec{\mu}_2$ of squares 1 and 2, respectively.
- (c) Find the torques $\vec{\tau}_1$ and $\vec{\tau}_2$ acting on squares 1 and 2, respectively.

Remember that vectors have components or magnitude and direction.





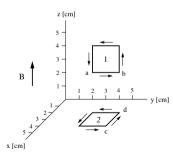
Conducting squares 1 and 2, each of side 2cm, are positioned as shown. A current I=3A is flowing around each square in the direction shown. A uniform magnetic field $\vec{B}=5\text{mT}\hat{\mathbf{k}}$ exists in the entire region.

- (a) Find the forces \vec{F}_{ab} and \vec{F}_{cd} acting on sides ab and cd, respectively.
- (b) Find the magnetic moments $\vec{\mu}_1$ and $\vec{\mu}_2$ of squares 1 and 2, respectively.
- (c) Find the torques $\vec{\tau}_1$ and $\vec{\tau}_2$ acting on squares 1 and 2, respectively.

Remember that vectors have components or magnitude and direction.

(a)
$$\vec{F}_{ab} = (3A)(2cm\hat{j}) \times (5mT\hat{k}) = 3 \times 10^{-4}N\hat{i}$$
.

$$\vec{F}_{cd} = (3\mathrm{A})(-2\mathrm{cm}\mathbf{\hat{i}}) \times (5\mathrm{mT}\mathbf{\hat{k}}) = 3 \times 10^{-4}\mathrm{N}\mathbf{\hat{j}}.$$





Conducting squares 1 and 2, each of side 2cm, are positioned as shown. A current I=3A is flowing around each square in the direction shown. A uniform magnetic field $\vec{B}=5\text{mT}\hat{\mathbf{k}}$ exists in the entire region.

- (a) Find the forces \vec{F}_{ab} and \vec{F}_{cd} acting on sides ab and cd, respectively.
- (b) Find the magnetic moments $\vec{\mu}_1$ and $\vec{\mu}_2$ of squares 1 and 2, respectively.
- (c) Find the torques $\vec{\tau}_1$ and $\vec{\tau}_2$ acting on squares 1 and 2, respectively.

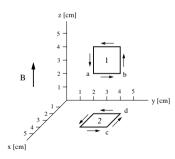
Remember that vectors have components or magnitude and direction.

(a)
$$\vec{F}_{ab} = (3A)(2cm\hat{j}) \times (5mT\hat{k}) = 3 \times 10^{-4}N\hat{i}$$
.

$$\vec{F}_{cd} = (3\mathrm{A})(-2\mathrm{cm}\mathbf{\hat{i}}) \times (5\mathrm{m}T\mathbf{\hat{k}}) = 3 \times 10^{-4}\mathrm{N}\mathbf{\hat{j}}.$$

(b)
$$\vec{\mu}_1 = (2\text{cm})^2 (3\text{A})\hat{\mathbf{i}} = 1.2 \times 10^{-3} \text{Am}^2 \hat{\mathbf{i}}.$$

$$\vec{\mu}_2 = (2\text{cm})^2 (3\text{A})\hat{\mathbf{k}} = 1.2 \times 10^{-3} \text{Am}^2 \hat{\mathbf{k}}.$$





Conducting squares 1 and 2, each of side 2cm, are positioned as shown. A current I=3A is flowing around each square in the direction shown. A uniform magnetic field $\vec{B}=5\text{mT}\hat{\mathbf{k}}$ exists in the entire region.

- (a) Find the forces \vec{F}_{ab} and \vec{F}_{cd} acting on sides ab and cd, respectively.
- (b) Find the magnetic moments $\vec{\mu}_1$ and $\vec{\mu}_2$ of squares 1 and 2, respectively.
- (c) Find the torques $\vec{\tau}_1$ and $\vec{\tau}_2$ acting on squares 1 and 2, respectively.

Remember that vectors have components or magnitude and direction.

(a)
$$\vec{F}_{ab} = (3A)(2cm\hat{\mathbf{j}}) \times (5mT\hat{\mathbf{k}}) = 3 \times 10^{-4}\text{N}\hat{\mathbf{i}}.$$

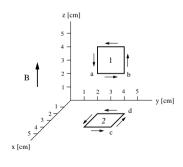
 $\vec{F}_{cd} = (3A)(-2cm\hat{\mathbf{i}}) \times (5mT\hat{\mathbf{k}}) = 3 \times 10^{-4}\text{N}\hat{\mathbf{i}}.$

(b)
$$\vec{\mu}_1 = (2\text{cm})^2 (3\text{A})\hat{\mathbf{i}} = 1.2 \times 10^{-3} \text{Am}^2 \hat{\mathbf{i}}.$$

$$\vec{\mu}_2 = (2\text{cm})^2 (3\text{A})\hat{\mathbf{k}} = 1.2 \times 10^{-3} \text{Am}^2 \hat{\mathbf{k}}.$$

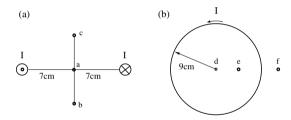
(c)
$$\vec{\tau}_1 = (1.2 \times 10^{-3} Am^2 \hat{\mathbf{i}}) \times (5mT \hat{\mathbf{k}}) = -6 \times 10^{-6} Nm \hat{\mathbf{j}}.$$

$$\vec{\tau}_2 = (1.2 \times 10^{-3} Am^2 \hat{\mathbf{k}}) \times (5mT \hat{\mathbf{k}}) = 0.$$



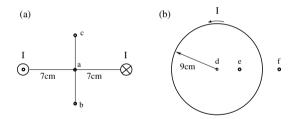


- (a) Consider two long, straight currents I=3mA in the directions shown. Find the magnitude of the magnetic field at point a. Find the directions $(\leftarrow,\rightarrow,\uparrow,\downarrow)$ of the magnetic field at points b and c.
- (b) Consider a circular current I=3mA in the direction shown. Find the magnitude of the magnetic field at point d. Find the directions (\otimes, \odot) of the magnetic field at points e and f.





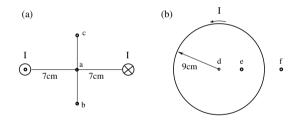
- (a) Consider two long, straight currents I=3mA in the directions shown. Find the magnitude of the magnetic field at point a. Find the directions $(\leftarrow,\rightarrow,\uparrow,\downarrow)$ of the magnetic field at points b and c.
- (b) Consider a circular current I=3mA in the direction shown. Find the magnitude of the magnetic field at point d. Find the directions (\otimes, \odot) of the magnetic field at points e and f.



(a)
$$B_a = 2 \frac{\mu_0(3\text{mA})}{2\pi(7\text{cm})} = 1.71 \times 10^{-8}\text{T}$$
 $B_b \uparrow$, $B_c \uparrow$.



- (a) Consider two long, straight currents I=3mA in the directions shown. Find the magnitude of the magnetic field at point a. Find the directions $(\leftarrow,\rightarrow,\uparrow,\downarrow)$ of the magnetic field at points b and c.
- (b) Consider a circular current I=3mA in the direction shown. Find the magnitude of the magnetic field at point d. Find the directions (\otimes, \odot) of the magnetic field at points e and f.



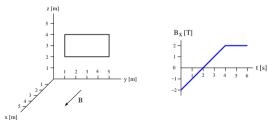
(a)
$$B_a = 2\frac{\mu_0(3\text{mA})}{2\pi(7\text{cm})} = 1.71 \times 10^{-8}\text{T}$$
 $B_b \uparrow$, $B_c \uparrow$.

(b)
$$B_d = \frac{\mu_0(3 {
m mA})}{2(9 {
m cm})} = 2.09 \times 10^{-8} {
m T}, \quad B_e \odot, \quad B_f \otimes.$$



A wire shaped into a rectangular loop as shown is placed in the yz-plane. A uniform time-dependent magnetic field $\mathbf{B} = B_x(t)\hat{\mathbf{i}}$ is present. The dependence of B_x on time is shown graphically.

- (a) Find magnitude $|\Phi_B^{(2)}|$ of the magnetic flux through the loop at time t=2s.
- (b) Find magnitude $|\Phi_B^{(5)}|$ of the magnetic flux through the loop at time t=5s.
- (c) Find magnitude $|\mathcal{E}^{(2)}|$ of the induced EMF at time t=2s.
- (d) Find magnitude $|\mathcal{E}^{(5)}|$ of the induced EMF at time t=5s.
- (e) Find the direction (cw/ccw) and magnitude I of the induced current at time t=2s if the wire has resistance 1Ω per meter of length.

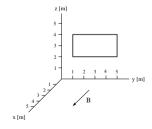


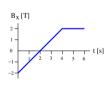


A wire shaped into a rectangular loop as shown is placed in the yz-plane. A uniform time-dependent magnetic field $\mathbf{B} = B_x(t)\hat{\mathbf{i}}$ is present. The dependence of B_x on time is shown graphically.

- (a) Find magnitude $|\Phi_B^{(2)}|$ of the magnetic flux through the loop at time t=2s.
- (b) Find magnitude $|\Phi_B^{(5)}|$ of the magnetic flux through the loop at time t=5s.
- (c) Find magnitude $|\mathcal{E}^{(2)}|$ of the induced EMF at time t=2s.
- (d) Find magnitude $|\mathcal{E}^{(5)}|$ of the induced EMF at time t=5s.
- (e) Find the direction (cw/ccw) and magnitude I of the induced current at time t=2s if the wire has resistance 1Ω per meter of length.

(a)
$$|\Phi_B^{(2)}| = |(8m^2)(0T)| = 0$$
,





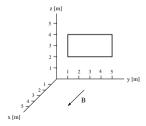


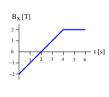
A wire shaped into a rectangular loop as shown is placed in the yz-plane. A uniform time-dependent magnetic field $\mathbf{B} = B_x(t)\hat{\mathbf{i}}$ is present. The dependence of B_x on time is shown graphically.

- (a) Find magnitude $|\Phi_B^{(2)}|$ of the magnetic flux through the loop at time t=2s.
- (b) Find magnitude $|\Phi_B^{(5)}|$ of the magnetic flux through the loop at time t=5s.
- (c) Find magnitude $|\mathcal{E}^{(2)}|$ of the induced EMF at time t=2s.
- (d) Find magnitude $|\mathcal{E}^{(5)}|$ of the induced EMF at time t=5s.
- (e) Find the direction (cw/ccw) and magnitude I of the induced current at time t=2s if the wire has resistance 1Ω per meter of length.

(a)
$$|\Phi_B^{(2)}| = |(8m^2)(0T)| = 0$$
,

(b)
$$|\Phi_B^{(5)}| = |(8m^2)(2T)| = 16 \text{ Wb},$$







A wire shaped into a rectangular loop as shown is placed in the yz-plane. A uniform time-dependent magnetic field $\mathbf{B} = B_{\mathbf{r}}(t)\hat{\mathbf{i}}$ is present. The dependence of $B_{\mathbf{r}}$ on time is shown graphically.

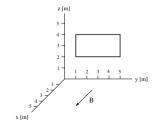
- (a) Find magnitude $|\Phi_p^{(2)}|$ of the magnetic flux through the loop at time t=2s.
- (b) Find magnitude $|\Phi_R^{(5)}|$ of the magnetic flux through the loop at time t=5s.
- (c) Find magnitude $|\mathcal{E}^{(2)}|$ of the induced EMF at time t=2s.
- (d) Find magnitude $|\mathcal{E}^{(5)}|$ of the induced EMF at time t=5s.
- (e) Find the direction (cw/ccw) and magnitude I of the induced current at time t=2s if the wire has resistance 1Ω per meter of length.

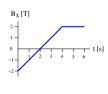
(a)
$$|\Phi_B^{(2)}| = |(8m^2)(0T)| = 0$$
,

(b)
$$|\Phi_B^{(5)}| = |(8m^2)(2T)| = 16 \,\text{Wb}$$

(b)
$$|\Phi_B^{(5)}| = |(8m^2)(2T)| = 16 \text{ Wb},$$

(c) $|\mathcal{E}^{(2)}| = \left| A \frac{dB}{dt} \right| = |(8m^2)(1T/s) = 8V$







A wire shaped into a rectangular loop as shown is placed in the yz-plane. A uniform time-dependent magnetic field $\mathbf{B} = B_{\mathbf{r}}(t)\hat{\mathbf{i}}$ is present. The dependence of $B_{\mathbf{r}}$ on time is shown graphically.

- (a) Find magnitude $|\Phi_{p}^{(2)}|$ of the magnetic flux through the loop at time t=2s.
- (b) Find magnitude $|\Phi_R^{(5)}|$ of the magnetic flux through the loop at time t=5s.
- (c) Find magnitude $|\mathcal{E}^{(2)}|$ of the induced EMF at time t=2s.
- (d) Find magnitude $|\mathcal{E}^{(5)}|$ of the induced EMF at time t=5s.
- (e) Find the direction (cw/ccw) and magnitude I of the induced current at time t=2s if the wire has resistance 1Ω per meter of length.

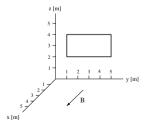
(a)
$$|\Phi_B^{(2)}| = |(8m^2)(0T)| = 0$$
,

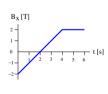
(b)
$$|\Phi_B^{(5)}| = |(8m^2)(2T)| = 16 \,\text{Wb},$$

(c)
$$|\mathcal{E}^{(2)}| = \left| A \frac{dB}{dt} \right| = |(8\text{m}^2)(1\text{T/s}) = 8\text{V}$$

(b)
$$|\Phi_B^{(1)}| = |(8m^2)(21)| = 16 \text{ Wb},$$

(c) $|\mathcal{E}^{(2)}| = |A\frac{dB}{dt}| = |(8m^2)(1\text{T/s}) = 8\text{V}$
(d) $|\mathcal{E}^{(5)}| = |A\frac{dB}{dt}| = |(8m^2)(0\text{T/s}) = 0$







A wire shaped into a rectangular loop as shown is placed in the yz-plane. A uniform time-dependent magnetic field $\mathbf{B} = B_{\mathbf{r}}(t)\hat{\mathbf{i}}$ is present. The dependence of $B_{\mathbf{r}}$ on time is shown graphically.

- (a) Find magnitude $|\Phi_{p}^{(2)}|$ of the magnetic flux through the loop at time t=2s.
- (b) Find magnitude $|\Phi_n^{(5)}|$ of the magnetic flux through the loop at time t=5s.
- (c) Find magnitude $|\mathcal{E}^{(2)}|$ of the induced EMF at time t=2s.
- (d) Find magnitude $|\mathcal{E}^{(5)}|$ of the induced EMF at time t=5s.
- (e) Find the direction (cw/ccw) and magnitude I of the induced current at time t=2s if the wire has resistance 1Ω per meter of length.

(a)
$$|\Phi_B^{(2)}| = |(8m^2)(0T)| = 0$$
,

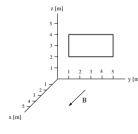
(b)
$$|\Phi_B^{(5)}| = |(8m^2)(2T)| = 16 \,\text{Wb}$$
,

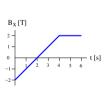
(c)
$$|\mathcal{E}^{(2)}| = \left| A \frac{dB}{dt} \right| = |(8\text{m}^2)(1\text{T/s}) = 8\text{V}$$

(c)
$$|\mathcal{E}^{(2)}| = \left| A \frac{dB}{dt} \right| = |(8\text{m}^2)(1\text{T/s}) = 8\text{V}$$

(d) $|\mathcal{E}^{(5)}| = \left| A \frac{dB}{dt} \right| = |(8\text{m}^2)(0\text{T/s}) = 0$
(e) $I^{(2)} = \frac{8\text{V}}{12\Omega} = 0.667\text{A}$. (cw).

(e)
$$I^{(2)} = \frac{8V}{12O} = 0.667A$$
. (cw).

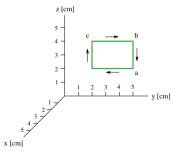






A current I is flowing around the conducting rectangular frame in the direction shown. The frame is located in a region of uniform magnetic field \mathbf{B} .

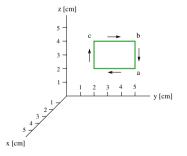
- (a) Find the force \mathbf{F}_{ab} (magnitude and direction) acting on side ab.
- (b) Find the force \mathbf{F}_{bc} (magnitude and direction) acting on side bc.
- (c) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the frame.





A current I is flowing around the conducting rectangular frame in the direction shown. The frame is located in a region of uniform magnetic field \mathbf{B} .

- (a) Find the force \mathbf{F}_{ab} (magnitude and direction) acting on side ab.
- (b) Find the force \mathbf{F}_{bc} (magnitude and direction) acting on side bc.
- (c) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the frame.

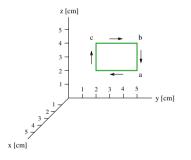


(a)
$$\mathbf{F}_{ab} = (1.2A)(-2cm\hat{\mathbf{k}}) \times (0.7mT\hat{\mathbf{k}}) = 0.$$



A current I is flowing around the conducting rectangular frame in the direction shown. The frame is located in a region of uniform magnetic field \mathbf{B} .

- (a) Find the force \mathbf{F}_{ab} (magnitude and direction) acting on side ab.
- (b) Find the force \mathbf{F}_{bc} (magnitude and direction) acting on side bc.
- (c) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the frame.



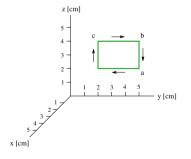
(a)
$$\mathbf{F}_{ab} = (1.2A)(-2cm\hat{\mathbf{k}}) \times (0.7mT\hat{\mathbf{k}}) = 0.$$

(b)
$$\mathbf{F}_{bc} = (1.2 \mathrm{A})(3 \mathrm{cm} \hat{\mathbf{j}}) \times (0.7 \mathrm{m} T \hat{\mathbf{k}}) = 2.52 \times 10^{-5} \mathrm{N} \hat{\mathbf{i}}.$$



A current I is flowing around the conducting rectangular frame in the direction shown. The frame is located in a region of uniform magnetic field \mathbf{B} .

- (a) Find the force \mathbf{F}_{ab} (magnitude and direction) acting on side ab.
- (b) Find the force \mathbf{F}_{bc} (magnitude and direction) acting on side bc.
- (c) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the frame.



(a)
$$\mathbf{F}_{ab} = (1.2A)(-2cm\hat{\mathbf{k}}) \times (0.7mT\hat{\mathbf{k}}) = 0.$$

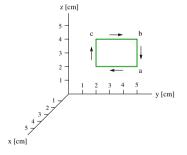
(b)
$$\mathbf{F}_{bc} = (1.2 \text{A})(3 \text{cm}\hat{\mathbf{j}}) \times (0.7 \text{mT}\hat{\mathbf{k}}) = 2.52 \times 10^{-5} \text{N}\hat{\mathbf{i}}.$$

(c)
$$\vec{\mu} = (2\text{cm})(3\text{cm})(1.2\text{A})(-\hat{\mathbf{i}}) = -7.2 \times 10^{-4} \text{Am}^2 \hat{\mathbf{i}}$$
.



A current I is flowing around the conducting rectangular frame in the direction shown. The frame is located in a region of uniform magnetic field \mathbf{B} .

- (a) Find the force \mathbf{F}_{ab} (magnitude and direction) acting on side ab.
- (b) Find the force \mathbf{F}_{bc} (magnitude and direction) acting on side bc.
- (c) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the frame.



(a)
$$\mathbf{F}_{ab} = (1.2A)(-2cm\mathbf{\hat{k}}) \times (0.7mT\mathbf{\hat{k}}) = 0.$$

(b)
$$\mathbf{F}_{bc} = (1.2 \text{A})(3 \text{cm}\hat{\mathbf{j}}) \times (0.7 \text{mT}\hat{\mathbf{k}}) = 2.52 \times 10^{-5} \text{N}\hat{\mathbf{i}}.$$

(c)
$$\vec{\mu} = (2\text{cm})(3\text{cm})(1.2\text{A})(-\hat{\mathbf{i}}) = -7.2 \times 10^{-4}\text{Am}^2\hat{\mathbf{i}}$$
.

(d)
$$\vec{\tau} = (-7.2 \times 10^{-4} Am^2 \hat{\mathbf{i}}) \times (0.7 mT \hat{\mathbf{k}}) = 5.04 \times 10^{-7} Nm \hat{\mathbf{j}}.$$



Solution for
$$I = 2.1$$
A, $\mathbf{B} = 0.8$ m \mathbf{T} $\hat{\mathbf{j}}$

(a)
$$\mathbf{F}_{ab} = (2.1 \mathrm{A}) (-2 \mathrm{cm} \hat{\mathbf{k}}) \times (0.8 \mathrm{mT} \hat{\mathbf{j}}) = 3.36 \times 10^{-5} \mathrm{N} \hat{\mathbf{i}}.$$



Solution for I = 2.1A, B = 0.8mT \hat{j}

(a)
$$\mathbf{F}_{ab} = (2.1 \mathrm{A}) (-2 \mathrm{cm} \mathbf{\hat{k}}) \times (0.8 \mathrm{mT} \mathbf{\hat{j}}) = 3.36 \times 10^{-5} \mathrm{N} \mathbf{\hat{i}}$$
.

(b)
$$\mathbf{F}_{bc} = (2.1 \text{A})(3 \text{cm}\hat{\mathbf{j}}) \times (0.8 \text{mT}\hat{\mathbf{j}}) = 0.$$



Solution for I = 2.1A, $\mathbf{B} = 0.8$ m \mathbf{T} $\hat{\mathbf{j}}$

(a)
$$\mathbf{F}_{ab} = (2.1 \text{A})(-2 \text{cm}\hat{\mathbf{k}}) \times (0.8 \text{mT}\hat{\mathbf{j}}) = 3.36 \times 10^{-5} \text{N}\hat{\mathbf{i}}.$$

(b)
$$\mathbf{F}_{bc} = (2.1 \text{A})(3 \text{cm}\hat{\mathbf{j}}) \times (0.8 \text{mT}\hat{\mathbf{j}}) = 0.$$

(c)
$$\vec{\mu} = (2\text{cm})(3\text{cm})(2.1\text{A})(-\hat{\mathbf{i}}) = -1.26 \times 10^{-3}\text{Am}^2\hat{\mathbf{i}}.$$



Solution for I = 2.1A, $\mathbf{B} = 0.8 \text{mT} \hat{\mathbf{j}}$

(a)
$$\mathbf{F}_{ab} = (2.1 \mathrm{A}) (-2 \mathrm{cm} \hat{\mathbf{k}}) \times (0.8 \mathrm{mT} \hat{\mathbf{j}}) = 3.36 \times 10^{-5} \mathrm{N} \hat{\mathbf{i}}.$$

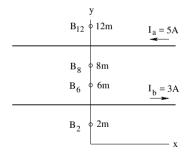
(b)
$$\mathbf{F}_{bc} = (2.1 \text{A})(3 \text{cm}\hat{\mathbf{j}}) \times (0.8 \text{mT}\hat{\mathbf{j}}) = 0.$$

(c)
$$\vec{\mu} = (2\text{cm})(3\text{cm})(2.1\text{A})(-\hat{\mathbf{i}}) = -1.26 \times 10^{-3} \text{Am}^2 \hat{\mathbf{i}}.$$

(d)
$$\vec{\tau} = (-1.26 \times 10^{-3} \text{Am}^2 \hat{\mathbf{i}}) \times (0.8 \text{mT} \hat{\mathbf{j}}) = -1.01 \times 10^{-6} \text{Nm} \hat{\mathbf{k}}.$$

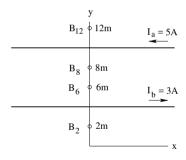


Two infinitely long, straight wires at positions y=10m and y=4m carry currents I_a and I_b , respectively. Find direction (in/out) and magnitude of the magnetic fields ${\bf B}_{12}$, ${\bf B}_{8}$, ${\bf B}_{6}$, and ${\bf B}_{2}$ at the points marked in the graph.





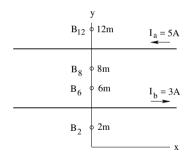
Two infinitely long, straight wires at positions y=10m and y=4m carry currents I_a and I_b , respectively. Find direction (in/out) and magnitude of the magnetic fields ${\bf B}_{12}$, ${\bf B}_8$, ${\bf B}_6$, and ${\bf B}_2$ at the points marked in the graph.



•
$$B_{12} = \frac{\mu_0}{2\pi} \left(-\frac{5A}{2m} + \frac{3A}{8m} \right) = -4.25 \times 10^{-7} T$$
 (in).



Two infinitely long, straight wires at positions y=10m and y=4m carry currents I_a and I_b , respectively. Find direction (in/out) and magnitude of the magnetic fields ${\bf B}_{12}$, ${\bf B}_{8}$, ${\bf B}_{6}$, and ${\bf B}_{2}$ at the points marked in the graph.

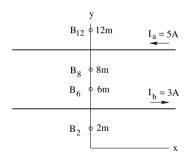


•
$$B_{12} = \frac{\mu_0}{2\pi} \left(-\frac{5A}{2m} + \frac{3A}{8m} \right) = -4.25 \times 10^{-7} T$$
 (in).

•
$$B_8 = \frac{\mu_0}{2\pi} \left(\frac{5A}{2m} + \frac{3A}{4m} \right) = 6.50 \times 10^{-7} T$$
 (out).



Two infinitely long, straight wires at positions y=10m and y=4m carry currents I_a and I_b , respectively. Find direction (in/out) and magnitude of the magnetic fields ${\bf B}_{12}$, ${\bf B}_{8}$, ${\bf B}_{6}$, and ${\bf B}_{2}$ at the points marked in the graph.



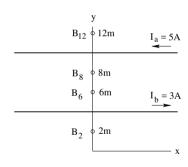
•
$$B_{12} = \frac{\mu_0}{2\pi} \left(-\frac{5A}{2m} + \frac{3A}{8m} \right) = -4.25 \times 10^{-7} T$$
 (in).

•
$$B_8 = \frac{\mu_0}{2\pi} \left(\frac{5A}{2m} + \frac{3A}{4m} \right) = 6.50 \times 10^{-7} T$$
 (out).

•
$$B_6 = \frac{\mu_0}{2\pi} \left(\frac{5A}{4m} + \frac{3A}{2m} \right) = 5.50 \times 10^{-7} T$$
 (out).



Two infinitely long, straight wires at positions y=10m and y=4m carry currents I_a and I_b , respectively. Find direction (in/out) and magnitude of the magnetic fields ${\bf B}_{12}$, ${\bf B}_{8}$, ${\bf B}_{6}$, and ${\bf B}_{2}$ at the points marked in the graph.



•
$$B_{12} = \frac{\mu_0}{2\pi} \left(-\frac{5A}{2m} + \frac{3A}{8m} \right) = -4.25 \times 10^{-7} T$$
 (in).

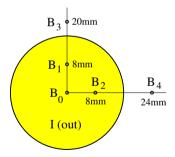
•
$$B_8 = \frac{\mu_0}{2\pi} \left(\frac{5 \mathrm{A}}{2 \mathrm{m}} + \frac{3 \mathrm{A}}{4 \mathrm{m}} \right) = 6.50 \times 10^{-7} \mathrm{T}$$
 (out).

•
$$B_6 = \frac{\mu_0}{2\pi} \left(\frac{5A}{4m} + \frac{3A}{2m} \right) = 5.50 \times 10^{-7} T$$
 (out).

•
$$B_2 = \frac{\mu_0}{2\pi} \left(\frac{5A}{8m} - \frac{3A}{2m} \right) = -1.75 \times 10^{-7} T$$
 (in).

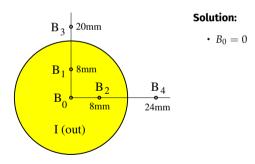


A conducting wire of 16mm radius carries a current I that is uniformly distributed over its cross section and directed out of the plane. Find direction (left/right/up/down) and magnitude of the magnetic fields \mathbf{B}_0 , \mathbf{B}_1 , \mathbf{B}_2 , \mathbf{B}_3 , and \mathbf{B}_4 at the positions indicated if the current is I=2.5A.



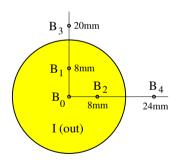


A conducting wire of 16mm radius carries a current I that is uniformly distributed over its cross section and directed out of the plane. Find direction (left/right/up/down) and magnitude of the magnetic fields \mathbf{B}_0 , \mathbf{B}_1 , \mathbf{B}_2 , \mathbf{B}_3 , and \mathbf{B}_4 at the positions indicated if the current is I=2.5A.





A conducting wire of 16mm radius carries a current I that is uniformly distributed over its cross section and directed out of the plane. Find direction (left/right/up/down) and magnitude of the magnetic fields \mathbf{B}_0 , \mathbf{B}_1 , \mathbf{B}_2 , \mathbf{B}_3 , and \mathbf{B}_4 at the positions indicated if the current is I=2.5A.

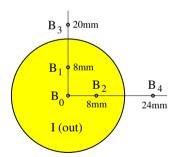


•
$$B_0 = 0$$

•
$$(B_1)(2\pi)(8\text{mm}) = \mu_0(I/4) \implies B_1 = 1.56 \times 10^{-5}\text{T}$$
 (left)



A conducting wire of 16mm radius carries a current I that is uniformly distributed over its cross section and directed out of the plane. Find direction (left/right/up/down) and magnitude of the magnetic fields \mathbf{B}_0 , \mathbf{B}_1 , \mathbf{B}_2 , \mathbf{B}_3 , and \mathbf{B}_4 at the positions indicated if the current is I=2.5A.



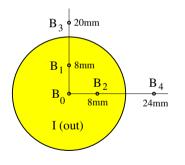
•
$$B_0 = 0$$

•
$$(B_1)(2\pi)(8\text{mm}) = \mu_0(I/4) \implies B_1 = 1.56 \times 10^{-5}\text{T}$$
 (left)

•
$$(B_2)(2\pi)(8\text{mm}) = \mu_0(I/4) \implies B_2 = 1.56 \times 10^{-5}\text{T}$$
 (up)



A conducting wire of 16mm radius carries a current I that is uniformly distributed over its cross section and directed out of the plane. Find direction (left/right/up/down) and magnitude of the magnetic fields \mathbf{B}_0 , \mathbf{B}_1 , \mathbf{B}_2 , \mathbf{B}_3 , and \mathbf{B}_4 at the positions indicated if the current is I=2.5A.



•
$$B_0 = 0$$

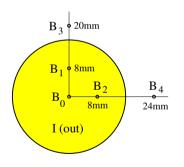
•
$$(B_1)(2\pi)(8\text{mm}) = \mu_0(I/4) \implies B_1 = 1.56 \times 10^{-5}\text{T}$$
 (left)

•
$$(B_2)(2\pi)(8{\rm mm}) = \mu_0(I/4) \quad \Rightarrow \ B_2 = 1.56 \times 10^{-5}{\rm T}$$
 (up)

•
$$(B_3)(2\pi)(20\text{mm}) = \mu_0 I \quad \Rightarrow B_3 = 2.5 \times 10^{-5} \text{T}$$
 (left)



A conducting wire of 16mm radius carries a current I that is uniformly distributed over its cross section and directed out of the plane. Find direction (left/right/up/down) and magnitude of the magnetic fields \mathbf{B}_0 , \mathbf{B}_1 , \mathbf{B}_2 , \mathbf{B}_3 , and \mathbf{B}_4 at the positions indicated if the current is I=2.5A.



•
$$B_0 = 0$$

•
$$(B_1)(2\pi)(8\text{mm}) = \mu_0(I/4) \implies B_1 = 1.56 \times 10^{-5}\text{T}$$
 (left)

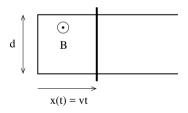
•
$$(B_2)(2\pi)(8{\rm mm}) = \mu_0(I/4) \quad \Rightarrow \ B_2 = 1.56 \times 10^{-5}{\rm T}$$
 (up)

•
$$(B_3)(2\pi)(20\text{mm}) = \mu_0 I \implies B_3 = 2.5 \times 10^{-5}\text{T}$$
 (left)

•
$$(B_4)(2\pi)(24\text{mm}) = \mu_0 I \implies B_4 = 2.08 \times 10^{-5}\text{T}$$
 (up)



A conducting frame of width d=1.6m with a moving conducting rod is located in a uniform magnetic field B=3T directed out of the plane. The rod moves at constant velocity v=0.4m/s toward the right. Its instantaneous position is x(t)=vt. Find the magnetic flux Φ_B through the frame and the induced emf $\mathcal E$ around the frame at times $t_2=2$ s, $t_3=3$ s, $t_4=4$ s, and $t_5=5$ s. Write magnitudes only (in SI units), no directions. Is the induced current directed clockwise or counterclockwise?

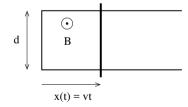




A conducting frame of width d=1.6m with a moving conducting rod is located in a uniform magnetic field B=3T directed out of the plane. The rod moves at constant velocity v=0.4m/s toward the right. Its instantaneous position is x(t)=vt. Find the magnetic flux Φ_B through the frame and the induced emf $\mathcal E$ around the frame at times $t_2=2$ s, $t_3=3$ s, $t_4=4$ s, and $t_5=5$ s. Write magnitudes only (in SI units), no directions. Is the induced current directed clockwise or counterclockwise?

•
$$\Phi_B^{(2)} = (1.6\text{m})(0.8\text{m})(3\text{T}) = 3.84\text{Wb},$$

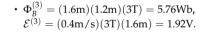
 $\mathcal{E}^{(2)} = (0.4\text{m/s})(3\text{T})(1.6\text{m}) = 1.92\text{V}.$

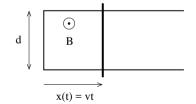




A conducting frame of width d=1.6m with a moving conducting rod is located in a uniform magnetic field B=3T directed out of the plane. The rod moves at constant velocity v=0.4m/s toward the right. Its instantaneous position is x(t)=vt. Find the magnetic flux Φ_B through the frame and the induced emf $\mathcal E$ around the frame at times $t_2=2$ s, $t_3=3$ s, $t_4=4$ s, and $t_5=5$ s. Write magnitudes only (in SI units), no directions. Is the induced current directed clockwise or counterclockwise?









A conducting frame of width d=1.6m with a moving conducting rod is located in a uniform magnetic field B=3T directed out of the plane. The rod moves at constant velocity v=0.4m/s toward the right. Its instantaneous position is x(t)=vt. Find the magnetic flux Φ_B through the frame and the induced emf $\mathcal E$ around the frame at times $t_2=2$ s, $t_3=3$ s, $t_4=4$ s, and $t_5=5$ s. Write magnitudes only (in SI units), no directions. Is the induced current directed clockwise or counterclockwise?

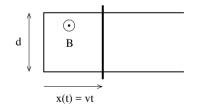


•
$$\Phi_B^{(3)} = (1.6\text{m})(1.2\text{m})(3\text{T}) = 5.76\text{Wb},$$

 $\mathcal{E}^{(3)} = (0.4\text{m/s})(3\text{T})(1.6\text{m}) = 1.92\text{V}.$

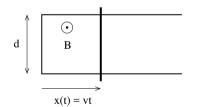
•
$$\Phi_B^{(4)} = (1.6\text{m})(1.6\text{m})(3\text{T}) = 7.68\text{Wb},$$

 $\mathcal{E}^{(4)} = (0.4\text{m/s})(3\text{T})(1.6\text{m}) = 1.92\text{V}.$





A conducting frame of width d=1.6m with a moving conducting rod is located in a uniform magnetic field B=3T directed out of the plane. The rod moves at constant velocity v=0.4m/s toward the right. Its instantaneous position is x(t)=vt. Find the magnetic flux Φ_B through the frame and the induced emf $\mathcal E$ around the frame at times $t_2=2$ s, $t_3=3$ s, $t_4=4$ s, and $t_5=5$ s. Write magnitudes only (in SI units), no directions. Is the induced current directed clockwise or counterclockwise?



•
$$\Phi_B^{(2)} = (1.6\text{m})(0.8\text{m})(3\text{T}) = 3.84\text{Wb},$$

 $\mathcal{E}^{(2)} = (0.4\text{m/s})(3\text{T})(1.6\text{m}) = 1.92\text{V}.$

•
$$\Phi_B^{(3)} = (1.6\text{m})(1.2\text{m})(3\text{T}) = 5.76\text{Wb},$$

 $\mathcal{E}^{(3)} = (0.4\text{m/s})(3\text{T})(1.6\text{m}) = 1.92\text{V}.$

•
$$\Phi_B^{(4)} = (1.6\text{m})(1.6\text{m})(3\text{T}) = 7.68\text{Wb},$$

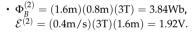
 $\mathcal{E}^{(4)} = (0.4\text{m/s})(3\text{T})(1.6\text{m}) = 1.92\text{V}.$

•
$$\Phi_B^{(5)} = (1.6\text{m})(2.0\text{m})(3\text{T}) = 9.60\text{Wb},$$

 $\mathcal{E}^{(5)} = (0.4\text{m/s})(3\text{T})(1.6\text{m}) = 1.92\text{V}.$



A conducting frame of width $d=1.6\mathrm{m}$ with a moving conducting rod is located in a uniform magnetic field $B=3\mathrm{T}$ directed out of the plane. The rod moves at constant velocity $v=0.4\mathrm{m/s}$ toward the right. Its instantaneous position is x(t)=vt. Find the magnetic flux Φ_B through the frame and the induced emf $\mathcal E$ around the frame at times $t_2=2\mathrm{s}, t_3=3\mathrm{s}, t_4=4\mathrm{s},$ and $t_5=5\mathrm{s}.$ Write magnitudes only (in SI units), no directions. Is the induced current directed clockwise or counterclockwise?



•
$$\Phi_B^{(3)} = (1.6\text{m})(1.2\text{m})(3\text{T}) = 5.76\text{Wb},$$

 $\mathcal{E}^{(3)} = (0.4\text{m/s})(3\text{T})(1.6\text{m}) = 1.92\text{V}.$

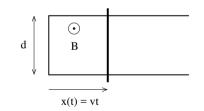
•
$$\Phi_B^{(4)} = (1.6\text{m})(1.6\text{m})(3\text{T}) = 7.68\text{Wb},$$

 $\mathcal{E}^{(4)} = (0.4\text{m/s})(3\text{T})(1.6\text{m}) = 1.92\text{V}.$

•
$$\Phi_B^{(5)} = (1.6\text{m})(2.0\text{m})(3\text{T}) = 9.60\text{Wb},$$

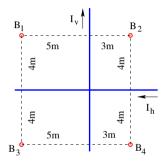
 $\mathcal{E}^{(5)} = (0.4\text{m/s})(3\text{T})(1.6\text{m}) = 1.92\text{V}.$







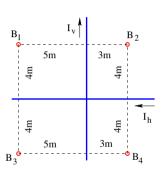
Consider two infinitely long, straight wires with currents $I_v = 6.9$ A, $I_h = 7.2$ A in the directions shown. Find direction (in/out) and magnitude of the magnetic fields $\mathbf{B_1}$, $\mathbf{B_2}$, $\mathbf{B_3}$, $\mathbf{B_4}$, at the points marked in the graph.





Consider two infinitely long, straight wires with currents $I_v = 6.9$ A, $I_h = 7.2$ A in the directions shown. Find direction (in/out) and magnitude of the magnetic fields \mathbf{B}_1 , \mathbf{B}_2 , \mathbf{B}_3 , \mathbf{B}_4 , at the points marked in the graph.

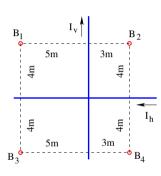
Solution:





Consider two infinitely long, straight wires with currents $I_v = 6.9$ A, $I_h = 7.2$ A in the directions shown. Find direction (in/out) and magnitude of the magnetic fields $\mathbf{B_1}$, $\mathbf{B_2}$, $\mathbf{B_3}$, $\mathbf{B_4}$, at the points marked in the graph.

- Convention used: out = positive, in = negative
- $B_1=rac{\mu_0}{2\pi}\left(rac{6.9 {
 m A}}{5 {
 m m}}-rac{7.2 {
 m A}}{4 {
 m m}}
 ight)=-0.84 imes 10^{-7} {
 m T}$ (in).



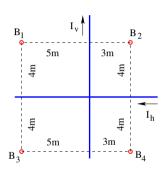


Consider two infinitely long, straight wires with currents $I_v = 6.9$ A, $I_h = 7.2$ A in the directions shown. Find direction (in/out) and magnitude of the magnetic fields \mathbf{B}_1 , \mathbf{B}_2 , \mathbf{B}_3 , \mathbf{B}_4 , at the points marked in the graph.

Solution:

•
$$B_1 = \frac{\mu_0}{2\pi} \left(\frac{6.9 \text{A}}{5 \text{m}} - \frac{7.2 \text{A}}{4 \text{m}} \right) = -0.84 \times 10^{-7} \text{T}$$
 (in).

•
$$B_2=rac{\mu_0}{2\pi}\left(-rac{6.9 {
m A}}{3 {
m m}}-rac{7.2 {
m A}}{4 {
m m}}
ight)=-8.20 imes 10^{-7} {
m T}$$
 (in).





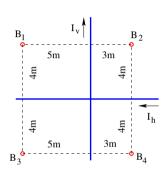
Consider two infinitely long, straight wires with currents $I_v = 6.9$ A, $I_h = 7.2$ A in the directions shown. Find direction (in/out) and magnitude of the magnetic fields \mathbf{B}_1 , \mathbf{B}_2 , \mathbf{B}_3 , \mathbf{B}_4 , at the points marked in the graph.

Solution:

•
$$B_1 = \frac{\mu_0}{2\pi} \left(\frac{6.9 \text{A}}{5 \text{m}} - \frac{7.2 \text{A}}{4 \text{m}} \right) = -0.84 \times 10^{-7} \text{T}$$
 (in).

•
$$B_2 = \frac{\mu_0}{2\pi} \left(-\frac{6.9A}{3m} - \frac{7.2A}{4m} \right) = -8.20 \times 10^{-7} T$$
 (in).

•
$$B_3 = \frac{\mu_0}{2\pi} \left(\frac{6.9 \text{A}}{5 \text{m}} + \frac{7.2 \text{A}}{4 \text{m}} \right) = 6.36 \times 10^{-7} \text{T} \text{ (out)}.$$





Consider two infinitely long, straight wires with currents $I_v = 6.9$ A, $I_h = 7.2$ A in the directions shown. Find direction (in/out) and magnitude of the magnetic fields $\mathbf{B_1}$, $\mathbf{B_2}$, $\mathbf{B_3}$, $\mathbf{B_4}$, at the points marked in the graph.

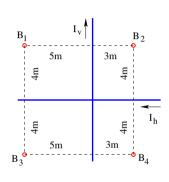
Solution:

•
$$B_1 = \frac{\mu_0}{2\pi} \left(\frac{6.9 \text{A}}{5 \text{m}} - \frac{7.2 \text{A}}{4 \text{m}} \right) = -0.84 \times 10^{-7} \text{T}$$
 (in).

•
$$B_2=rac{\mu_0}{2\pi}\left(-rac{6.9 A}{3 m}-rac{7.2 A}{4 m}
ight)=-8.20 imes 10^{-7} T$$
 (in).

•
$$B_3 = \frac{\mu_0}{2\pi} \left(\frac{6.9A}{5m} + \frac{7.2A}{4m} \right) = 6.36 \times 10^{-7} T$$
 (out).

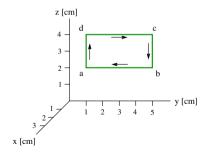
•
$$B_4=rac{\mu_0}{2\pi}\left(-rac{6.9 A}{3 m}+rac{7.2 A}{4 m}
ight)=-1.00 imes 10^{-7} T$$
 (in).





In a region of uniform magnetic field ${\bf B}=4{\rm mT}{\hat {\bf k}}~[{\bf B}=5{\rm mT}{\hat {\bf j}}]$ a clockwise current $I=1.4{\rm A}~[I=1.5{\rm A}]$ is flowing through the conducting rectangular frame.

- (i) Find the force \mathbf{F}_{dc} (magnitude and direction) acting on side dc of the rectangle. (ii) Find the force \mathbf{F}_{ad} (magnitude and direction) acting on side ad of the rectangle.
- (iii) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (iv) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the current loop.

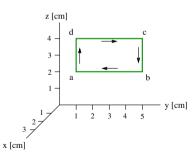




In a region of uniform magnetic field ${\bf B}=4{\rm mT}{\hat {\bf k}}~[{\bf B}=5{\rm mT}{\hat {\bf j}}]$ a clockwise current $I=1.4{\rm A}~[I=1.5{\rm A}]$ is flowing through the conducting rectangular frame.

- (i) Find the force \mathbf{F}_{dc} (magnitude and direction) acting on side dc of the rectangle. (ii) Find the force \mathbf{F}_{ad} (magnitude and direction) acting on side ad of the rectangle.
- (iii) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (iv) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the current loop.

(i)
$$\mathbf{F}_{dc} = (1.4 \mathrm{A}) (4 \mathrm{cm} \hat{\mathbf{j}}) \times (4 \mathrm{m} \mathrm{T} \hat{\mathbf{k}}) = 2.24 \times 10^{-4} \mathrm{N} \hat{\mathbf{i}}.$$
 $[\mathbf{F}_{dc} = (1.5 \mathrm{A}) (4 \mathrm{cm} \hat{\mathbf{j}}) \times (5 \mathrm{m} \mathrm{T} \hat{\mathbf{j}}) = 0.]$

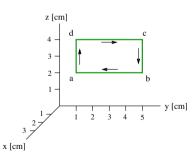




In a region of uniform magnetic field ${\bf B}=4{\rm mT}{\hat {\bf k}}~[{\bf B}=5{\rm mT}{\hat {\bf j}}]$ a clockwise current $I=1.4{\rm A}~[I=1.5{\rm A}]$ is flowing through the conducting rectangular frame.

- (i) Find the force \mathbf{F}_{dc} (magnitude and direction) acting on side dc of the rectangle. (ii) Find the force \mathbf{F}_{ad} (magnitude and direction) acting on side ad of the rectangle.
- (iii) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (iv) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the current loop.

- (i) $\mathbf{F}_{dc} = (1.4 \mathrm{A})(4 \mathrm{cm}\hat{\mathbf{j}}) \times (4 \mathrm{mT}\hat{\mathbf{k}}) = 2.24 \times 10^{-4} \mathrm{N}\hat{\mathbf{i}}.$ $[\mathbf{F}_{dc} = (1.5 \mathrm{A})(4 \mathrm{cm}\hat{\mathbf{j}}) \times (5 \mathrm{mT}\hat{\mathbf{j}}) = 0.]$
- (ii) $\mathbf{F}_{ad} = (1.4 \mathrm{A}) (2 \mathrm{cm} \hat{\mathbf{k}}) \times (4 \mathrm{m} T \hat{\mathbf{k}}) = 0.$ $[\mathbf{F}_{ad} = (1.5 \mathrm{A}) (2 \mathrm{cm} \hat{\mathbf{k}}) \times (5 \mathrm{m} T \hat{\mathbf{j}}) = -1.50 \times 10^{-4} \mathrm{N} \hat{\mathbf{i}}.]$





In a region of uniform magnetic field ${\bf B}=4{\rm mT\hat{k}}\,[{\bf B}=5{\rm mT\hat{j}}]$ a clockwise current $I=1.4{\rm A}\,[I=1.5{\rm A}]$ is flowing through the conducting rectangular frame.

- (i) Find the force \mathbf{F}_{dc} (magnitude and direction) acting on side dc of the rectangle. (ii) Find the force \mathbf{F}_{ad} (magnitude and direction) acting on side ad of the rectangle.
- (iii) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (iv) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the current loop.

(i)
$$\mathbf{F}_{dc} = (1.4 \text{A})(4 \text{cm}\hat{\mathbf{j}}) \times (4 \text{mT}\hat{\mathbf{k}}) = 2.24 \times 10^{-4} \text{N}\hat{\mathbf{i}}.$$

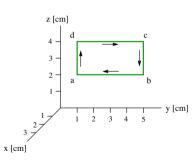
 $[\mathbf{F}_{dc} = (1.5 \text{A})(4 \text{cm}\hat{\mathbf{j}}) \times (5 \text{mT}\hat{\mathbf{j}}) = 0.]$

(ii)
$$\mathbf{F}_{ad} = (1.4 \mathrm{A}) (2 \mathrm{cm} \hat{\mathbf{k}}) \times (4 \mathrm{m} T \hat{\mathbf{k}}) = 0.$$

$$[\mathbf{F}_{ad} = (1.5 \mathrm{A}) (2 \mathrm{cm} \hat{\mathbf{k}}) \times (5 \mathrm{m} T \hat{\mathbf{j}}) = -1.50 \times 10^{-4} \mathrm{N} \hat{\mathbf{i}}.]$$

(iii)
$$\vec{\mu} = [-(4\text{cm})(2\text{cm})\hat{\mathbf{i}}](1.4\text{A}) = -1.12 \times 10^{-3}\text{Am}^2\hat{\mathbf{i}}.$$

$$[\vec{\mu} = [-(4\text{cm})(2\text{cm})\hat{\mathbf{i}}](1.5\text{A}) = -1.20 \times 10^{-3}\text{Am}^2\hat{\mathbf{i}}.]$$





In a region of uniform magnetic field ${\bf B}=4{\rm mT}{\hat {\bf k}}~[{\bf B}=5{\rm mT}{\hat {\bf j}}]$ a clockwise current $I=1.4{\rm A}~[I=1.5{\rm A}]$ is flowing through the conducting rectangular frame.

- (i) Find the force \mathbf{F}_{dc} (magnitude and direction) acting on side dc of the rectangle. (ii) Find the force \mathbf{F}_{ad} (magnitude and direction) acting on side ad of the rectangle.
- (iii) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (iv) Find the torque $\vec{ au}$ (magnitude and direction) acting on the current loop.

(i)
$$\mathbf{F}_{dc} = (1.4 \text{A})(4 \text{cm}\hat{\mathbf{j}}) \times (4 \text{mT}\hat{\mathbf{k}}) = 2.24 \times 10^{-4} \text{N}\hat{\mathbf{i}}.$$

 $[\mathbf{F}_{dc} = (1.5 \text{A})(4 \text{cm}\hat{\mathbf{i}}) \times (5 \text{mT}\hat{\mathbf{i}}) = 0.]$

(ii)
$$\mathbf{F}_{ad} = (1.4 \text{A})(2 \text{cm} \hat{\mathbf{k}}) \times (4 \text{m} T \hat{\mathbf{k}}) = 0.$$

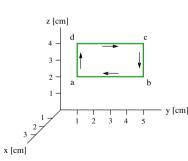
 $[\mathbf{F}_{ad} = (1.5 \text{A})(2 \text{cm} \hat{\mathbf{k}}) \times (5 \text{m} T \hat{\mathbf{i}}) = -1.50 \times 10^{-4} \text{N} \hat{\mathbf{i}}.]$

(iii)
$$\vec{\mu} = [-(4\text{cm})(2\text{cm})\hat{\mathbf{i}}](1.4\text{A}) = -1.12 \times 10^{-3}\text{Am}^2\hat{\mathbf{i}}.$$

$$[\vec{\mu} = [-(4\text{cm})(2\text{cm})\hat{\mathbf{i}}](1.5\text{A}) = -1.20 \times 10^{-3}\text{Am}^2\hat{\mathbf{i}}.]$$

(iv)
$$\vec{\tau} = (-1.12 \times 10^{-3} \text{Am}^2 \hat{\mathbf{i}}) \times (4 \text{mT} \hat{\mathbf{k}}) = 4.48 \times 10^{-6} \text{Nm} \hat{\mathbf{j}}.$$

 $[\vec{\tau} = (-1.20 \times 10^{-3} \text{Am}^2 \hat{\mathbf{i}}) \times (5 \text{mT} \hat{\mathbf{j}}) = -6.00 \times 10^{-6} \text{Nm} \hat{\mathbf{k}}.]$



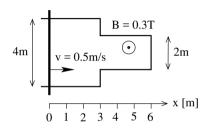


A conducting frame with a moving conducting rod is located in a uniform magnetic field directed out of the plane as shown. The rod moves at constant velocity.

Find the magnetic flux Φ_B through the frame and the induced emf $\mathcal E$ around the frame when the rod is

- (a) at position x = 1m,
- (b) at position x = 4m.
- (c) at position x = 2m,
- (d) at position x = 5m.

Write magnitudes only (in SI units), no directions.



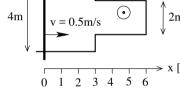


A conducting frame with a moving conducting rod is located in a uniform magnetic field directed out of the plane as shown. The rod moves at constant velocity.

Find the magnetic flux Φ_B through the frame and the induced emf $\mathcal E$ around the frame when the rod is

- (a) at position x = 1m,
- (b) at position x = 4m.
- (c) at position x = 2m,
- (d) at position x = 5m.

Write magnitudes only (in SI units), no directions.



(a)
$$\Phi_B = (8+6)m^2(0.3T) = 4.2Wb$$
, $\mathcal{E} = (0.5m/s)(0.3T)(4m) = 0.6V$.

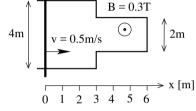


A conducting frame with a moving conducting rod is located in a uniform magnetic field directed out of the plane as shown. The rod moves at constant velocity.

Find the magnetic flux Φ_B through the frame and the induced emf ${\mathcal E}$ around the frame when the rod is

- (a) at position x = 1m,
- (b) at position x = 4m.
- (c) at position x = 2m,
- (d) at position x = 5m.

Write magnitudes only (in SI units), no directions.



(a)
$$\Phi_B = (8+6)m^2(0.3T) = 4.2Wb$$
, $\mathcal{E} = (0.5m/s)(0.3T)(4m) = 0.6V$.

(b)
$$\Phi_{\text{B}} = (4m^2)(0.3T) = 1.2 \text{Wb}, \quad \mathcal{E} = (0.5 \text{m/s})(0.3T)(2\text{m}) = 0.3 \text{V}.$$

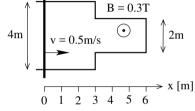


A conducting frame with a moving conducting rod is located in a uniform magnetic field directed out of the plane as shown. The rod moves at constant velocity.

Find the magnetic flux Φ_B through the frame and the induced emf ${\mathcal E}$ around the frame when the rod is

- (a) at position x = 1m,
- (b) at position x = 4m.
- (c) at position x = 2m,
- (d) at position x = 5m.

Write magnitudes only (in SI units), no directions.



(a)
$$\Phi_B = (8+6)m^2(0.3T) = 4.2Wb$$
, $\mathcal{E} = (0.5m/s)(0.3T)(4m) = 0.6V$.

(b)
$$\Phi_B = (4m^2)(0.3T) = 1.2Wb$$
, $\mathcal{E} = (0.5m/s)(0.3T)(2m) = 0.3V$.

(c)
$$\Phi_B = (4+6)m^2(0.3T) = 3.0Wb$$
, $\mathcal{E} = (0.5m/s)(0.3T)(4m) = 0.6V$.

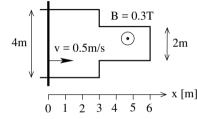


A conducting frame with a moving conducting rod is located in a uniform magnetic field directed out of the plane as shown. The rod moves at constant velocity.

Find the magnetic flux Φ_B through the frame and the induced emf ${\cal E}$ around the frame when the rod is

- (a) at position x = 1m,
- (b) at position x = 4m.
- (c) at position x = 2m,
- (d) at position x = 5m.

Write magnitudes only (in SI units), no directions.



(a)
$$\Phi_B = (8+6)m^2(0.3T) = 4.2Wb$$
, $\mathcal{E} = (0.5m/s)(0.3T)(4m) = 0.6V$.

(b)
$$\Phi_B = (4m^2)(0.3T) = 1.2Wb$$
, $\mathcal{E} = (0.5m/s)(0.3T)(2m) = 0.3V$.

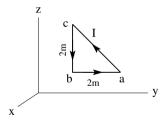
(c)
$$\Phi_B = (4+6)m^2(0.3T) = 3.0Wb$$
, $\mathcal{E} = (0.5m/s)(0.3T)(4m) = 0.6V$.

(d)
$$\Phi_B = (2m^2)(0.3T) = 0.6Wb$$
, $\mathcal{E} = (0.5m/s)(0.3T)(2m) = 0.3V$.



Consider a region with uniform magnetic field $\vec{B}=4T\hat{j}$ [$\vec{B}=5T\hat{k}$]. A conducting loop in the yz-plane has the shape of a right-angled triangle as shown with a counterclockwise current I=0.7A [I=0.9A].

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F}_{ab} (magnitude and direction) acting on the side ab of the loop.
- (c) Find the force \vec{F}_{bc} (magnitude and direction) acting on the side bc of the loop.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.



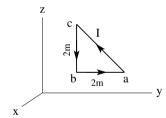


Consider a region with uniform magnetic field $\vec{B}=4T\hat{j}$ [$\vec{B}=5T\hat{k}$]. A conducting loop in the yz-plane has the shape of a right-angled triangle as shown with a counterclockwise current I=0.7A [I=0.9A].

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F}_{ab} (magnitude and direction) acting on the side ab of the loop.
- (c) Find the force \vec{F}_{bc} (magnitude and direction) acting on the side bc of the loop.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

(a)
$$\vec{\mu} = (0.7A)(2m^2)\hat{i} = 1.4Am^2\hat{i}$$

 $[\vec{\mu} = (0.9A)(2m^2)\hat{i} = 1.8Am^2\hat{i}]$





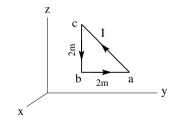
Consider a region with uniform magnetic field $\vec{B}=4T\hat{j}$ [$\vec{B}=5T\hat{k}$]. A conducting loop in the yz-plane has the shape of a right-angled triangle as shown with a counterclockwise current I=0.7A [I=0.9A].

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F}_{ab} (magnitude and direction) acting on the side ab of the loop.
- (c) Find the force \vec{F}_{bc} (magnitude and direction) acting on the side bc of the loop.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

(a)
$$\vec{\mu} = (0.7A)(2m^2)\hat{i} = 1.4Am^2\hat{i}$$

 $[\vec{\mu} = (0.9A)(2m^2)\hat{i} = 1.8Am^2\hat{i}]$

(b)
$$\vec{F}_{ab} = 0$$
 $[\vec{F}_{ab} = (0.9\text{A})(2\text{m}\hat{j}) \times (5\text{T}\hat{k}) = 9.0\text{N}\hat{i}]$





Consider a region with uniform magnetic field $\vec{B}=4T\hat{j}$ [$\vec{B}=5T\hat{k}$]. A conducting loop in the yz-plane has the shape of a right-angled triangle as shown with a counterclockwise current I=0.7A [I=0.9A].

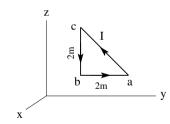
- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F}_{ab} (magnitude and direction) acting on the side ab of the loop.
- (c) Find the force \vec{F}_{bc} (magnitude and direction) acting on the side bc of the loop.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

(a)
$$\vec{\mu} = (0.7A)(2m^2)\hat{i} = 1.4Am^2\hat{i}$$

 $[\vec{\mu} = (0.9A)(2m^2)\hat{i} = 1.8Am^2\hat{i}]$

(b)
$$\vec{F}_{ab} = 0$$
 $[\vec{F}_{ab} = (0.9\text{A})(2\text{m}\hat{j}) \times (5\text{T}\hat{k}) = 9.0\text{N}\hat{i}]$

(c)
$$\vec{F}_{bc} = (0.7\text{A})(-2\text{m}\hat{k}) \times (4\text{T}\hat{j}) = 5.6\text{N}\hat{i} \quad [\vec{F}_{bc} = 0]$$





Consider a region with uniform magnetic field $\vec{B}=4T\hat{j}$ [$\vec{B}=5T\hat{k}$]. A conducting loop in the yz-plane has the shape of a right-angled triangle as shown with a counterclockwise current I=0.7A [I=0.9A].

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F}_{ab} (magnitude and direction) acting on the side ab of the loop.
- (c) Find the force \vec{F}_{bc} (magnitude and direction) acting on the side bc of the loop.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

(a)
$$\vec{\mu} = (0.7A)(2m^2)\hat{i} = 1.4Am^2\hat{i}$$

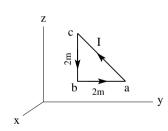
 $[\vec{\mu} = (0.9A)(2m^2)\hat{i} = 1.8Am^2\hat{i}]$

(b)
$$\vec{F}_{ab} = 0$$
 $[\vec{F}_{ab} = (0.9A)(2m\hat{j}) \times (5T\hat{k}) = 9.0N\hat{i}]$

(c)
$$\vec{F}_{bc} = (0.7 \text{A}) (-2 \text{m} \hat{k}) \times (4 \text{T} \hat{j}) = 5.6 \text{N} \hat{i} \quad [\vec{F}_{bc} = 0]$$

(d)
$$\vec{\tau} = (1.4 \text{Am}^2 \hat{i}) \times (4 \text{T} \hat{j}) = 5.6 \text{Nm} \hat{k}$$

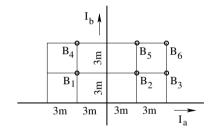
 $[\vec{\tau} = (1.8 \text{Am}^2 \hat{i}) \times (5 \text{T} \hat{k}) = -9.0 \text{Nm} \hat{j}]$





Consider two infinitely long, straight wires with currents $I_a = I_b = 7$ A in the directions shown.

Find direction (in/out) and magnitude of the magnetic fields B_1 , B_2 , B_3 , B_4 , B_5 , B_6 at the points marked in the graph.

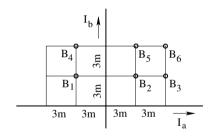




Consider two infinitely long, straight wires with currents $I_a = I_b = 7$ A in the directions shown.

Find direction (in/out) and magnitude of the magnetic fields B_1 , B_2 , B_3 , B_4 , B_5 , B_6 at the points marked in the graph.

•
$$B_1 = \frac{\mu_0}{2\pi} \left(\frac{7A}{3m} + \frac{7A}{3m} \right) = +0.933 \mu T$$
 (out of plane).



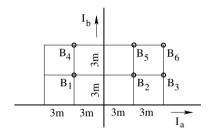


Consider two infinitely long, straight wires with currents $I_a = I_b = 7$ A in the directions shown.

Find direction (in/out) and magnitude of the magnetic fields B_1 , B_2 , B_3 , B_4 , B_5 , B_6 at the points marked in the graph.

•
$$B_1=rac{\mu_0}{2\pi}\left(rac{7\mathrm{A}}{3\mathrm{m}}+rac{7\mathrm{A}}{3\mathrm{m}}
ight)=+0.933\mu\mathrm{T}$$
 (out of plane).

•
$$B_2 = \frac{\mu_0}{2\pi} \left(\frac{7A}{3m} - \frac{7A}{3m} \right) = 0$$
 (no direction).





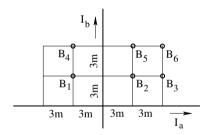
Consider two infinitely long, straight wires with currents $I_a = I_b = 7$ A in the directions shown.

Find direction (in/out) and magnitude of the magnetic fields B_1 , B_2 , B_3 , B_4 , B_5 , B_6 at the points marked in the graph.

•
$$B_1=rac{\mu_0}{2\pi}\left(rac{7\mathrm{A}}{3\mathrm{m}}+rac{7\mathrm{A}}{3\mathrm{m}}
ight)=+0.933\mu\mathrm{T}$$
 (out of plane).

•
$$B_2 = \frac{\mu_0}{2\pi} \left(\frac{7A}{3m} - \frac{7A}{3m} \right) = 0$$
 (no direction).

•
$$B_3=rac{\mu_0}{2\pi}\left(rac{7\mathrm{A}}{3\mathrm{m}}-rac{7\mathrm{A}}{6\mathrm{m}}
ight)=+0.233\mu\mathrm{T}$$
 (out of plane).





Consider two infinitely long, straight wires with currents $I_a = I_b = 7$ A in the directions shown.

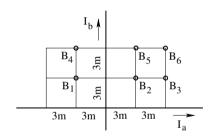
Find direction (in/out) and magnitude of the magnetic fields B_1 , B_2 , B_3 , B_4 , B_5 , B_6 at the points marked in the graph.

•
$$B_1=rac{\mu_0}{2\pi}\left(rac{7\mathrm{A}}{3\mathrm{m}}+rac{7\mathrm{A}}{3\mathrm{m}}
ight)=+0.933\mu\mathrm{T}$$
 (out of plane).

•
$$B_2=rac{\mu_0}{2\pi}\left(rac{7A}{3m}-rac{7A}{3m}
ight)=0$$
 (no direction).

•
$$B_3 = \frac{\mu_0}{2\pi} \left(\frac{7A}{3m} - \frac{7A}{6m} \right) = +0.233 \mu T$$
 (out of plane).

+
$$B_4=rac{\mu_0}{2\pi}\left(rac{7A}{6m}+rac{7A}{3m}
ight)=0.7\mu T$$
 (out of plane).





Consider two infinitely long, straight wires with currents $I_a=I_b=7\mathrm{A}$ in the directions shown.

Find direction (in/out) and magnitude of the magnetic fields B_1 , B_2 , B_3 , B_4 , B_5 , B_6 at the points marked in the graph.

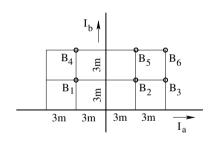
•
$$B_1=rac{\mu_0}{2\pi}\left(rac{7A}{3m}+rac{7A}{3m}
ight)=+0.933\mu T$$
 (out of plane).

•
$$B_2=rac{\mu_0}{2\pi}\left(rac{7A}{3m}-rac{7A}{3m}
ight)=0$$
 (no direction).

•
$$B_3=rac{\mu_0}{2\pi}\left(rac{7A}{3m}-rac{7A}{6m}
ight)=+0.233\mu T$$
 (out of plane).

+
$$B_4=rac{\mu_0}{2\pi}\left(rac{7A}{6m}+rac{7A}{3m}
ight)=0.7\mu T$$
 (out of plane).

•
$$B_5 = \frac{\mu_0}{2\pi} \left(\frac{7A}{6m} - \frac{7A}{3m} \right) = -0.233 \mu T$$
 (into plane).





Consider two infinitely long, straight wires with currents $I_a = I_b = 7$ A in the directions shown.

Find direction (in/out) and magnitude of the magnetic fields B_1 , B_2 , B_3 , B_4 , B_5 , B_6 at the points marked in the graph.

•
$$B_1=rac{\mu_0}{2\pi}\left(rac{7\mathrm{A}}{3\mathrm{m}}+rac{7\mathrm{A}}{3\mathrm{m}}
ight)=+0.933\mu\mathrm{T}$$
 (out of plane).

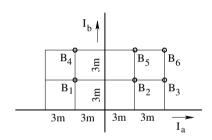
•
$$B_2=rac{\mu_0}{2\pi}\left(rac{7A}{3m}-rac{7A}{3m}
ight)=0$$
 (no direction).

•
$$B_3=rac{\mu_0}{2\pi}\left(rac{7A}{3m}-rac{7A}{6m}
ight)=+0.233\mu T$$
 (out of plane).

+
$$B_4=rac{\mu_0}{2\pi}\left(rac{7A}{6m}+rac{7A}{3m}
ight)=0.7\mu T$$
 (out of plane).

•
$$B_5 = \frac{\mu_0}{2\pi} \left(\frac{7A}{6m} - \frac{7A}{3m} \right) = -0.233 \mu T$$
 (into plane).

•
$$B_6 = \frac{\mu_0}{2\pi} \left(\frac{7A}{6m} - \frac{7A}{6m} \right) = 0$$
 (no direction).

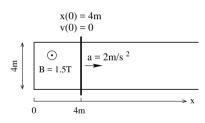




A conducting frame with a moving conducting rod is placed in a uniform magnetic field directed out of the plane. The rod starts from rest at time t=0 at the position shown and moves with constant acceleration to the right.

- (a) Find the magnetic flux Φ_B through the conducting loop and the induced emf ${\cal E}$ around the loop at t=0.
- (b) Find the position x(3s) and velocity v(3s) of the rod at time t=3s.
- (c) Find the magnetic flux Φ_B through the loop and the induced emf ${\mathcal E}$ around the loop at time t=3s.

Write magnitudes only (in SI units), no directions.



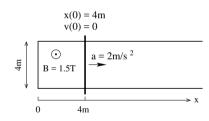


A conducting frame with a moving conducting rod is placed in a uniform magnetic field directed out of the plane. The rod starts from rest at time t=0 at the position shown and moves with constant acceleration to the right.

- (a) Find the magnetic flux Φ_B through the conducting loop and the induced emf ${\cal E}$ around the loop at t=0.
- (b) Find the position x(3s) and velocity v(3s) of the rod at time t=3s.
- (c) Find the magnetic flux Φ_B through the loop and the induced emf ${\mathcal E}$ around the loop at time t=3s.

Write magnitudes only (in SI units), no directions.

(a)
$$\Phi_B = (16m^2)(1.5T) = 24Wb$$
, $\mathcal{E} = 0$.

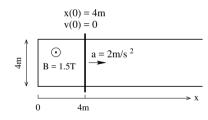




A conducting frame with a moving conducting rod is placed in a uniform magnetic field directed out of the plane. The rod starts from rest at time t=0 at the position shown and moves with constant acceleration to the right.

- (a) Find the magnetic flux Φ_B through the conducting loop and the induced emf ${\cal E}$ around the loop at t=0.
- (b) Find the position x(3s) and velocity v(3s) of the rod at time t=3s.
- (c) Find the magnetic flux Φ_B through the loop and the induced emf ${\mathcal E}$ around the loop at time t=3s.

Write magnitudes only (in SI units), no directions.



(a)
$$\Phi_B = (16m^2)(1.5T) = 24Wb$$
, $\mathcal{E} = 0$.

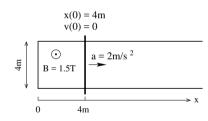
(b)
$$x(2s) = 4m + \frac{1}{2}(2m/s^2)(3s)^2 = 13m$$
, $v(3s) = (2m/s^2)(3s) = 6m/s$.



A conducting frame with a moving conducting rod is placed in a uniform magnetic field directed out of the plane. The rod starts from rest at time t=0 at the position shown and moves with constant acceleration to the right.

- (a) Find the magnetic flux Φ_B through the conducting loop and the induced emf ${\cal E}$ around the loop at t=0.
- (b) Find the position x(3s) and velocity v(3s) of the rod at time t=3s.
- (c) Find the magnetic flux Φ_B through the loop and the induced emf ${\cal E}$ around the loop at time t=3s.

Write magnitudes only (in SI units), no directions.



(a)
$$\Phi_B = (16\text{m}^2)(1.5\text{T}) = 24\text{Wb}, \quad \mathcal{E} = 0.$$

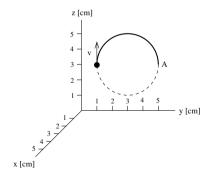
(b)
$$x(2s) = 4m + \frac{1}{2}(2m/s^2)(3s)^2 = 13m$$
, $v(3s) = (2m/s^2)(3s) = 6m/s$.

(c)
$$\Phi_B = (52\text{m}^2)(1.5\text{T}) = 78\text{Wb}, \quad \mathcal{E} = (6\text{m/s})(1.5\text{T})(4\text{m}) = 36\text{V}.$$



In a uniform magnetic field of strength B=3.5mT [B=5.3mT], a proton with specifications ($m=1.67\times 10^{-27}$ kg, $q=1.60\times 10^{-19}$ C) moves at speed v around a circle in the yz-plane as shown.

- (a) Show that the direction of the magnetic field must be $+\hat{\mathbf{i}}$
- (b) What is the speed of the proton?
- (c) How long does it take the proton to reach point A from its current position?

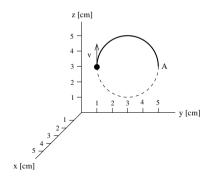




In a uniform magnetic field of strength B=3.5mT [B=5.3mT], a proton with specifications ($m=1.67\times 10^{-27}$ kg, $q=1.60\times 10^{-19}$ C) moves at speed v around a circle in the yz-plane as shown.

- (a) Show that the direction of the magnetic field must be $+\hat{\mathbf{i}}$
- (b) What is the speed of the proton?
- (c) How long does it take the proton to reach point A from its current position?

(a)
$$F\hat{\mathbf{j}} = qv\hat{\mathbf{k}} \times B\hat{\mathbf{i}}$$
.





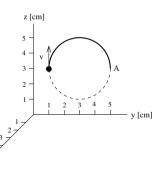
In a uniform magnetic field of strength B=3.5mT [B=5.3mT], a proton with specifications ($m=1.67\times 10^{-27}$ kg, $q=1.60\times 10^{-19}$ C) moves at speed v around a circle in the yz-plane as shown.

x [cm]

- (a) Show that the direction of the magnetic field must be $+\hat{\mathbf{i}}$
- (b) What is the speed of the proton?
- (c) How long does it take the proton to reach point A from its current position?

(a)
$$F\hat{\mathbf{j}} = qv\hat{\mathbf{k}} \times B\hat{\mathbf{i}}$$
.

(b)
$$\frac{mv^2}{r} = qvB \implies v = \frac{qBr}{m} = 6.71 \times 10^3 \text{m/s} [10.2 \times 10^3 \text{m/s}].$$





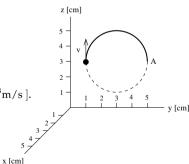
In a uniform magnetic field of strength B=3.5mT [B=5.3mT], a proton with specifications ($m=1.67\times 10^{-27}$ kg, $q=1.60\times 10^{-19}$ C) moves at speed v around a circle in the yz-plane as shown.

- (a) Show that the direction of the magnetic field must be $+\hat{\mathbf{i}}$
- (b) What is the speed of the proton?
- (c) How long does it take the proton to reach point A from its current position?

(a)
$$F\hat{\mathbf{j}} = qv\hat{\mathbf{k}} \times B\hat{\mathbf{i}}$$
.

(b)
$$\frac{mv^2}{r} = qvB \implies v = \frac{qBr}{m} = 6.71 \times 10^3 \text{m/s} [10.2 \times 10^3 \text{m/s}].$$

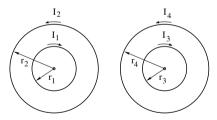
(c)
$$t = \frac{\pi r}{v} = \frac{\pi m}{qB} = 9.37 \times 10^{-6} \text{s} \quad [6.19 \times 10^{-6} \text{s}].$$





Consider two pairs of concentric circular currents in separate regions. The current directions are indicated by arrows. The radii are $r_1=r_3=5 {\rm cm}$ and $r_2=r_4=10 {\rm cm}$

- (a) Find magnitude B_1 and direction (\odot, \otimes) of the magnetic field produced by current $I_1=1.5$ A at the center.
- (b) Find magnitude μ_4 and direction (\odot, \otimes) of the magnetic dipole moment produced by current $I_4=4.5$ A.
- (c) What must be the ratio I_2/I_1 such that the magnetic field at the center is zero?
- (d) What must be the ratio I_4/I_3 such that the magnetic dipole moment is zero?

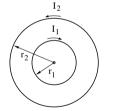


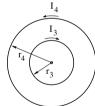


Consider two pairs of concentric circular currents in separate regions. The current directions are indicated by arrows. The radii are $r_1 = r_3 = 5$ cm and $r_2 = r_4 = 10$ cm

- (a) Find magnitude B_1 and direction (\odot, \otimes) of the magnetic field produced by current $I_1 = 1.5$ A at the center.
- (b) Find magnitude μ_4 and direction (\odot, \otimes) of the magnetic dipole moment produced by current $I_4=4.5$ A.
- (c) What must be the ratio I_2/I_1 such that the magnetic field at the center is zero?
- (d) What must be the ratio I_4/I_3 such that the magnetic dipole moment is zero?

(a)
$$B_1 = \frac{\mu_0(1.5A)}{2(5cm)} = 1.88 \times 10^{-5} T \otimes$$





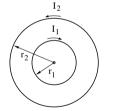


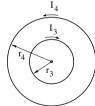
Consider two pairs of concentric circular currents in separate regions. The current directions are indicated by arrows. The radii are $r_1 = r_3 = 5$ cm and $r_2 = r_4 = 10$ cm

- (a) Find magnitude B_1 and direction (\odot, \otimes) of the magnetic field produced by current $I_1 = 1.5$ A at the center.
- (b) Find magnitude μ_4 and direction (\odot, \otimes) of the magnetic dipole moment produced by current $I_4=4.5$ A.
- (c) What must be the ratio I_2/I_1 such that the magnetic field at the center is zero?
- (d) What must be the ratio I_4/I_3 such that the magnetic dipole moment is zero?

(a)
$$B_1 = \frac{\mu_0(1.5A)}{2(5cm)} = 1.88 \times 10^{-5} T \otimes$$

(b)
$$\mu_4 = \pi (10 \text{cm})^2 (4.5 \text{A}) = 1.41 \times 10^{-1} \text{Am}^2$$
 \odot







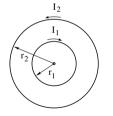
Consider two pairs of concentric circular currents in separate regions. The current directions are indicated by arrows. The radii are $r_1=r_3=5\mathrm{cm}$ and $r_2=r_4=10\mathrm{cm}$

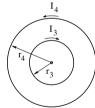
- (a) Find magnitude B_1 and direction (\odot, \otimes) of the magnetic field produced by current $I_1 = 1.5$ A at the center.
- (b) Find magnitude μ_4 and direction (\odot, \otimes) of the magnetic dipole moment produced by current $I_4=4.5$ A.
- (c) What must be the ratio I_2/I_1 such that the magnetic field at the center is zero?
- (d) What must be the ratio I_4/I_3 such that the magnetic dipole moment is zero?

(a)
$$B_1 = \frac{\mu_0(1.5A)}{2(5cm)} = 1.88 \times 10^{-5} T \otimes$$

(b)
$$\mu_4 = \pi (10 \text{cm})^2 (4.5 \text{A}) = 1.41 \times 10^{-1} \text{Am}^2$$
 \odot

(c)
$$B_1 = B_2 \implies \frac{I_2}{I_1} = \frac{r_2}{r_1} = 2.$$







Consider two pairs of concentric circular currents in separate regions. The current directions are indicated by arrows. The radii are $r_1=r_3=5\mathrm{cm}$ and $r_2=r_4=10\mathrm{cm}$

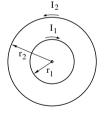
- (a) Find magnitude B_1 and direction (\odot, \otimes) of the magnetic field produced by current $I_1 = 1.5$ A at the center.
- (b) Find magnitude μ_4 and direction (\odot, \otimes) of the magnetic dipole moment produced by current $I_4=4.5$ A.
- (c) What must be the ratio I_2/I_1 such that the magnetic field at the center is zero?
- (d) What must be the ratio I_4/I_3 such that the magnetic dipole moment is zero?

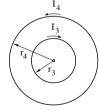
(a)
$$B_1 = \frac{\mu_0(1.5A)}{2(5cm)} = 1.88 \times 10^{-5} T \otimes$$

(b)
$$\mu_4 = \pi (10 \text{cm})^2 (4.5 \text{A}) = 1.41 \times 10^{-1} \text{Am}^2$$
 \odot

(c)
$$B_1 = B_2 \implies \frac{I_2}{I_1} = \frac{r_2}{r_1} = 2.$$

(d)
$$\mu_3 = \mu_4 \implies \frac{I_4}{I_3} = \frac{r_3^2}{r_4^2} = 0.25.$$

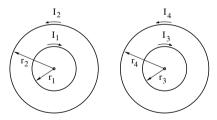






Consider two pairs of concentric circular currents in separate regions. The current directions are indicated by arrows. The radii are $r_1=r_3=5 {\rm cm}$ and $r_2=r_4=10 {\rm cm}$

- (a) Find magnitude B_2 and direction (\odot, \otimes) of the magnetic field produced by current $I_2=2.5A$ at the center.
- (b) Find magnitude μ_3 and direction (\odot, \otimes) of the magnetic dipole moment produced by current $I_3=3$ A.
- (c) What must be the ratio I_2/I_1 such that the magnetic field at the center is zero?
- (d) What must be the ratio I_4/I_3 such that the magnetic dipole moment is zero?

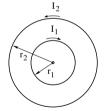


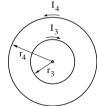


Consider two pairs of concentric circular currents in separate regions. The current directions are indicated by arrows. The radii are $r_1=r_3=5 {\rm cm}$ and $r_2=r_4=10 {\rm cm}$

- (a) Find magnitude B_2 and direction (\odot, \otimes) of the magnetic field produced by current $I_2 = 2.5A$ at the center.
- (b) Find magnitude μ_3 and direction (\odot, \otimes) of the magnetic dipole moment produced by current $I_3 = 3A$.
- (c) What must be the ratio I_2/I_1 such that the magnetic field at the center is zero?
- (d) What must be the ratio I_4/I_3 such that the magnetic dipole moment is zero?

(a)
$$B_2 = \frac{\mu_0(2.5A)}{2(10cm)} = 1.57 \times 10^{-5}T$$
 \odot





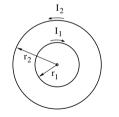


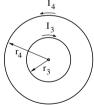
Consider two pairs of concentric circular currents in separate regions. The current directions are indicated by arrows. The radii are $r_1=r_3=5 {\rm cm}$ and $r_2=r_4=10 {\rm cm}$

- (a) Find magnitude B_2 and direction (\odot, \otimes) of the magnetic field produced by current $I_2 = 2.5A$ at the center.
- (b) Find magnitude μ_3 and direction (\odot, \otimes) of the magnetic dipole moment produced by current $I_3 = 3A$.
- (c) What must be the ratio I_2/I_1 such that the magnetic field at the center is zero?
- (d) What must be the ratio I_4/I_3 such that the magnetic dipole moment is zero?

(a)
$$B_2 = \frac{\mu_0(2.5\text{A})}{2(10\text{cm})} = 1.57 \times 10^{-5}\text{T}$$
 \odot

(b)
$$\mu_3 = \pi (5 \text{cm})^2 (3 \text{A}) = 2.36 \times 10^{-2} \text{Am}^2 \otimes$$







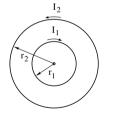
Consider two pairs of concentric circular currents in separate regions. The current directions are indicated by arrows. The radii are $r_1=r_3=5 {\rm cm}$ and $r_2=r_4=10 {\rm cm}$

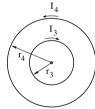
- (a) Find magnitude B_2 and direction (\odot, \otimes) of the magnetic field produced by current $I_2 = 2.5A$ at the center.
- (b) Find magnitude μ_3 and direction (\odot, \otimes) of the magnetic dipole moment produced by current $I_3 = 3A$.
- (c) What must be the ratio I_2/I_1 such that the magnetic field at the center is zero?
- (d) What must be the ratio I_4/I_3 such that the magnetic dipole moment is zero?

(a)
$$B_2 = \frac{\mu_0(2.5\text{A})}{2(10\text{cm})} = 1.57 \times 10^{-5}\text{T}$$
 \odot

(b)
$$\mu_3 = \pi (5 \text{cm})^2 (3 \text{A}) = 2.36 \times 10^{-2} \text{Am}^2 \otimes$$

(c)
$$B_1 = B_2 \implies \frac{I_2}{I_1} = \frac{r_2}{r_1} = 2.$$







Consider two pairs of concentric circular currents in separate regions. The current directions are indicated by arrows. The radii are $r_1=r_3=5\mathrm{cm}$ and $r_2=r_4=10\mathrm{cm}$

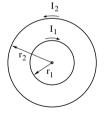
- (a) Find magnitude B_2 and direction (\odot, \otimes) of the magnetic field produced by current $I_2 = 2.5A$ at the center.
- (b) Find magnitude μ_3 and direction (\odot, \otimes) of the magnetic dipole moment produced by current $I_3 = 3A$.
- (c) What must be the ratio I_2/I_1 such that the magnetic field at the center is zero?
- (d) What must be the ratio I_4/I_3 such that the magnetic dipole moment is zero?

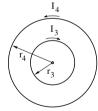
(a)
$$B_2 = \frac{\mu_0(2.5\text{A})}{2(10\text{cm})} = 1.57 \times 10^{-5}\text{T}$$
 \odot

(b)
$$\mu_3 = \pi (5 \text{cm})^2 (3 \text{A}) = 2.36 \times 10^{-2} \text{Am}^2 \otimes$$

(c)
$$B_1 = B_2 \implies \frac{I_2}{I_1} = \frac{r_2}{r_1} = 2.$$

(d)
$$\mu_3 = \mu_4 \implies \frac{I_4}{I_3} = \frac{r_3^2}{r_4^2} = 0.25.$$



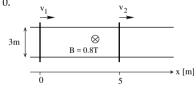




A pair of fixed rails are connected by two moving rods. A uniform magnetic field B is present. The positions of the rods at time t=0 are as shown. The (constant) velocities are

$$v_1=0.5 \mathrm{m/s}$$
, $v_2=2.5 \mathrm{m/s}$ [$v_1=1.5 \mathrm{m/s}$, $v_2=0.5 \mathrm{m/s}$].

- (a) Find the magnetic flux Φ_0 at time t=0 and Φ_1 at t=2s (magnitude only).
- (b) Find the induced emf \mathcal{E}_0 at time t=0 and \mathcal{E}_1 at t=2s (magnitude only).
- (c) Find the direction (cw/ccw) of the induced current at t = 0.

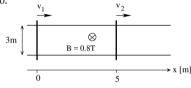




A pair of fixed rails are connected by two moving rods. A uniform magnetic field B is present. The positions of the rods at time t=0 are as shown. The (constant) velocities are

$$v_1=0.5 \mathrm{m/s}$$
, $v_2=2.5 \mathrm{m/s}$ [$v_1=1.5 \mathrm{m/s}$, $v_2=0.5 \mathrm{m/s}$].

- (a) Find the magnetic flux Φ_0 at time t=0 and Φ_1 at t=2s (magnitude only).
- (b) Find the induced emf \mathcal{E}_0 at time t=0 and \mathcal{E}_1 at t=2s (magnitude only).
- (c) Find the direction (cw/ccw) of the induced current at t = 0.



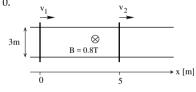
(a)
$$\Phi_0 = (5m - 0m)(3m)(0.8T) = 12Wb$$
, $\Phi_1 = (10m - 1m)(3m)(0.8T) = 21.6Wb$
[$\Phi_0 = (5m - 0m)(3m)(0.8T) = 12Wb$, $\Phi_1 = (6m - 3m)(3m)(0.8T) = 7.2Wb$]



A pair of fixed rails are connected by two moving rods. A uniform magnetic field B is present. The positions of the rods at time t=0 are as shown. The (constant) velocities are

$$v_1=0.5 \mathrm{m/s}$$
, $v_2=2.5 \mathrm{m/s}$ [$v_1=1.5 \mathrm{m/s}$, $v_2=0.5 \mathrm{m/s}$].

- (a) Find the magnetic flux Φ_0 at time t=0 and Φ_1 at t=2s (magnitude only).
- (b) Find the induced emf \mathcal{E}_0 at time t=0 and \mathcal{E}_1 at t=2s (magnitude only).
- (c) Find the direction (cw/ccw) of the induced current at t = 0.



(a)
$$\Phi_0 = (5m - 0m)(3m)(0.8T) = 12Wb$$
, $\Phi_1 = (10m - 1m)(3m)(0.8T) = 21.6Wb$
[$\Phi_0 = (5m - 0m)(3m)(0.8T) = 12Wb$, $\Phi_1 = (6m - 3m)(3m)(0.8T) = 7.2Wb$]

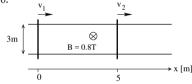
(b)
$$|\mathcal{E}_0| = |\mathcal{E}_1| = (2.5\text{m/s} - 0.5\text{m/s})(0.8\text{T})(3\text{m}) = 4.8\text{V}$$

 $[|\mathcal{E}_0| = |\mathcal{E}_1| = (1.5\text{m/s} - 0.5\text{m/s})(0.8\text{T})(3\text{m}) = 2.4\text{V}]$



A pair of fixed rails are connected by two moving rods. A uniform magnetic field B is present. The positions of the rods at time t=0 are as shown. The (constant) velocities are $v_1=0.5$ m/s, $v_2=2.5$ m/s [$v_1=1.5$ m/s, $v_2=0.5$ m/s].

- (a) Find the magnetic flux Φ_0 at time t=0 and Φ_1 at t=2s (magnitude only).
- (b) Find the induced emf \mathcal{E}_0 at time t=0 and \mathcal{E}_1 at t=2s (magnitude only).
- (c) Find the direction (cw/ccw) of the induced current at t = 0.



Solution:

(a)
$$\Phi_0 = (5m - 0m)(3m)(0.8T) = 12Wb$$
, $\Phi_1 = (10m - 1m)(3m)(0.8T) = 21.6Wb$
[$\Phi_0 = (5m - 0m)(3m)(0.8T) = 12Wb$, $\Phi_1 = (6m - 3m)(3m)(0.8T) = 7.2Wb$]

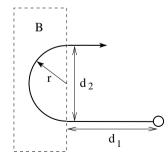
$$\begin{split} \text{(b)} \ |\mathcal{E}_0| &= |\mathcal{E}_1| = (2.5\text{m/s} - 0.5\text{m/s})(0.8\text{T})(3\text{m}) = 4.8\text{V} \\ &[\ |\mathcal{E}_0| = |\mathcal{E}_1| = (1.5\text{m/s} - 0.5\text{m/s})(0.8\text{T})(3\text{m}) = 2.4\text{V}\] \end{split}$$

(c) ccw [cw]



A proton $(m=1.67\times 10^{-27} {\rm kg},\ q=1.60\times 10^{-19} {\rm C})$, launched with initial speed $v_0=4000 {\rm m/s} \ [3000 {\rm m/s}]$ a distance $d_1=25 {\rm cm} \ [32 {\rm cm}]$ from a region of magnetic field, exits that region after a half-circle turn of diameter $d_2=30 {\rm cm} \ [35 {\rm cm}]$.

- (a) Find the centripetal force *F* provided by the magnetic field.
- (b) Find magnitude and direction (\odot,\otimes) of the magnetic field B.
- (c) Find the time t_1 elapsed between launch and entrance into the region of field.
- (d) Find the time t_2 elapsed between entrance and exit.

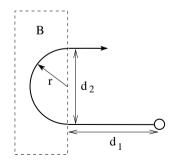




A proton $(m=1.67\times 10^{-27} {\rm kg},\ q=1.60\times 10^{-19} {\rm C})$, launched with initial speed $v_0=4000 {\rm m/s}$ [3000m/s] a distance $d_1=25 {\rm cm}$ [32cm] from a region of magnetic field, exits that region after a half-circle turn of diameter $d_2=30 {\rm cm}$ [35cm].

- (a) Find the centripetal force *F* provided by the magnetic field.
- (b) Find magnitude and direction (\odot, \otimes) of the magnetic field **B**.
- (c) Find the time t_1 elapsed between launch and entrance into the region of field.
- (d) Find the time t_2 elapsed between entrance and exit.

(a)
$$\frac{mv_0^2}{d_2/2} = 1.78 \times 10^{-19} \mathrm{N} \quad [8.59 \times 10^{-20} \mathrm{N}].$$





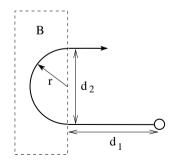
A proton $(m = 1.67 \times 10^{-27} \text{kg}, q = 1.60 \times 10^{-19} \text{C})$, launched with initial speed $v_0 = 4000 \text{m/s} [3000 \text{m/s}]$ a distance $d_1 = 25$ cm [32cm] from a region of magnetic field, exits that region after a half-circle turn of diameter $d_2 = 30$ cm [35cm].

- (a) Find the centripetal force F provided by the magnetic field.
- (b) Find magnitude and direction (\odot, \otimes) of the magnetic field **B**.
- (c) Find the time t_1 elapsed between launch and entrance into the region of field.
- (d) Find the time t_2 elapsed between entrance and exit.

(a)
$$\frac{mv_0^2}{d_2/2} = 1.78 \times 10^{-19} \text{N} \quad [8.59 \times 10^{-20} \text{N}].$$

(b) $B = \frac{F}{qv_0} = 2.78 \times 10^{-4} \text{T} \quad [1.79 \times 10^{-4} \text{T}] \quad \odot$

(b)
$$B = \frac{F}{qv_0} = 2.78 \times 10^{-4} \text{T} \quad [1.79 \times 10^{-4} \text{T}]$$





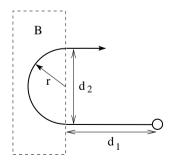
A proton $(m = 1.67 \times 10^{-27} \text{kg}, q = 1.60 \times 10^{-19} \text{C})$, launched with initial speed $v_0 = 4000 \text{m/s} [3000 \text{m/s}]$ a distance $d_1 = 25$ cm [32cm] from a region of magnetic field, exits that region after a half-circle turn of diameter $d_2 = 30$ cm [35cm].

- (a) Find the centripetal force F provided by the magnetic field.
- (b) Find magnitude and direction (\odot, \otimes) of the magnetic field **B**.
- (c) Find the time t_1 elapsed between launch and entrance into the region of field.
- (d) Find the time t_2 elapsed between entrance and exit.

(a)
$$\frac{mv_0^2}{d_2/2} = 1.78 \times 10^{-19} \text{N}$$
 [8.59 × 10⁻²⁰N].

(a)
$$\frac{mv_0^2}{d_2/2} = 1.78 \times 10^{-19} \text{N}$$
 [8.59 × 10⁻²⁰N].
(b) $B = \frac{F}{qv_0} = 2.78 \times 10^{-4} \text{T}$ [1.79 × 10⁻⁴T] \odot
(c) $t_1 = \frac{d_1}{v_0} = 6.25 \times 10^{-5} \text{s}$ [1.07 × 10⁻⁴s].

(c)
$$t_1 = \frac{d_1}{v_0} = 6.25 \times 10^{-5} \text{s} \quad [1.07 \times 10^{-4} \text{s}].$$





A proton $(m = 1.67 \times 10^{-27} \text{kg}, q = 1.60 \times 10^{-19} \text{C})$, launched with initial speed $v_0 = 4000 \text{m/s} [3000 \text{m/s}]$ a distance $d_1 = 25$ cm [32cm] from a region of magnetic field, exits that region after a half-circle turn of diameter $d_2 = 30$ cm [35cm].

- (a) Find the centripetal force F provided by the magnetic field.
- (b) Find magnitude and direction (\odot, \otimes) of the magnetic field **B**.
- (c) Find the time t_1 elapsed between launch and entrance into the region of field.
- (d) Find the time t_2 elapsed between entrance and exit.

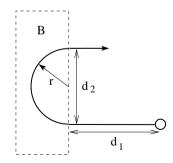
(a)
$$\frac{mv_0^2}{d_2/2} = 1.78 \times 10^{-19} \text{N} \quad [8.59 \times 10^{-20} \text{N}].$$

(a)
$$\frac{mv_0^2}{d_2/2} = 1.78 \times 10^{-19} \text{N} \quad [8.59 \times 10^{-20} \text{N}].$$

(b) $B = \frac{F}{qv_0} = 2.78 \times 10^{-4} \text{T} \quad [1.79 \times 10^{-4} \text{T}] \quad \odot$

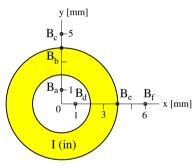
(c)
$$t_1 = \frac{d_1}{v_0} = 6.25 \times 10^{-5} \text{s} \quad [1.07 \times 10^{-4} \text{s}].$$

(d)
$$t_2 = \frac{\pi d_2}{2v_0} = 1.18 \times 10^{-4} \text{s} \quad [1.83 \times 10^{-4} \text{s}].$$





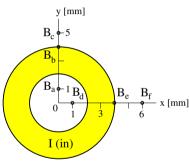
A wire in the shape of a cylindrical shell with a 2mm inner radius and 4mm outer radius carries a current I=3.7A [4.1A] that is uniformly distributed over its cross section and directed into the plane. Find direction (left/right/up/down/in/out) and magnitude of the magnetic fields \mathbf{B}_a , \mathbf{B}_b , \mathbf{B}_c [\mathbf{B}_d , \mathbf{B}_e , \mathbf{B}_f] at the positions indicated.





A wire in the shape of a cylindrical shell with a 2mm inner radius and 4mm outer radius carries a current I=3.7A [4.1A] that is uniformly distributed over its cross section and directed into the plane. Find direction (left/right/up/down/in/out) and magnitude of the magnetic fields \mathbf{B}_a , \mathbf{B}_b , \mathbf{B}_c [\mathbf{B}_d , \mathbf{B}_e , \mathbf{B}_f] at the positions indicated.

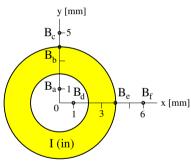
•
$$B_a=0$$





A wire in the shape of a cylindrical shell with a 2mm inner radius and 4mm outer radius carries a current I=3.7A [4.1A] that is uniformly distributed over its cross section and directed into the plane. Find direction (left/right/up/down/in/out) and magnitude of the magnetic fields \mathbf{B}_a , \mathbf{B}_b , \mathbf{B}_c [\mathbf{B}_d , \mathbf{B}_e , \mathbf{B}_f] at the positions indicated.

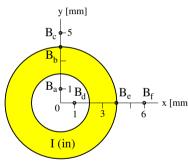
- $B_a = 0$
- $(B_b)(2\pi)(4\text{mm}) = \mu_0(3.7\text{A})$ $\Rightarrow B_b = 1.85 \times 10^{-4}\text{T}$ (right)





A wire in the shape of a cylindrical shell with a 2mm inner radius and 4mm outer radius carries a current I=3.7A [4.1A] that is uniformly distributed over its cross section and directed into the plane. Find direction (left/right/up/down/in/out) and magnitude of the magnetic fields \mathbf{B}_a , \mathbf{B}_b , \mathbf{B}_c [\mathbf{B}_d , \mathbf{B}_e , \mathbf{B}_f] at the positions indicated.

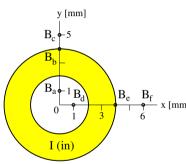
- $B_a = 0$
- $(B_b)(2\pi)(4\text{mm}) = \mu_0(3.7\text{A})$ $\Rightarrow B_b = 1.85 \times 10^{-4}\text{T}$ (right)
- $(B_c)(2\pi)(5\text{mm}) = \mu_0(3.7\text{A})$ $\Rightarrow B_c = 1.48 \times 10^{-4}\text{T}$ (right)





A wire in the shape of a cylindrical shell with a 2mm inner radius and 4mm outer radius carries a current I=3.7A [4.1A] that is uniformly distributed over its cross section and directed into the plane. Find direction (left/right/up/down/in/out) and magnitude of the magnetic fields \mathbf{B}_a , \mathbf{B}_b , \mathbf{B}_c [\mathbf{B}_d , \mathbf{B}_e , \mathbf{B}_f] at the positions indicated.

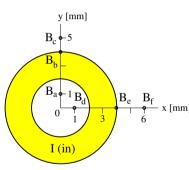
- $B_a = 0$
- $(B_b)(2\pi)(4\text{mm}) = \mu_0(3.7\text{A})$ $\Rightarrow B_b = 1.85 \times 10^{-4}\text{T}$ (right)
- $(B_c)(2\pi)(5\text{mm}) = \mu_0(3.7\text{A})$ $\Rightarrow B_c = 1.48 \times 10^{-4}\text{T}$ (right)
- $[B_d = 0]$





A wire in the shape of a cylindrical shell with a 2mm inner radius and 4mm outer radius carries a current I=3.7A [4.1A] that is uniformly distributed over its cross section and directed into the plane. Find direction (left/right/up/down/in/out) and magnitude of the magnetic fields \mathbf{B}_a , \mathbf{B}_b , \mathbf{B}_c [\mathbf{B}_d , \mathbf{B}_e , \mathbf{B}_f] at the positions indicated.

- $B_a=0$
- $(B_b)(2\pi)(4\text{mm}) = \mu_0(3.7\text{A})$ $\Rightarrow B_b = 1.85 \times 10^{-4}\text{T}$ (right)
- $(B_c)(2\pi)(5\text{mm}) = \mu_0(3.7\text{A})$ $\Rightarrow B_c = 1.48 \times 10^{-4}\text{T}$ (right)
- $[B_d = 0]$
- $[(B_e)(2\pi)(4\text{mm}) = \mu_0(4.1\text{A}) \implies B_e = 2.05 \times 10^{-4}\text{T}$ (down)]



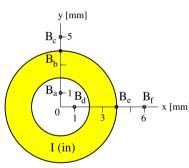


A wire in the shape of a cylindrical shell with a 2mm inner radius and 4mm outer radius carries a current I=3.7A [4.1A] that is uniformly distributed over its cross section and directed into the plane. Find direction (left/right/up/down/in/out) and magnitude of the magnetic fields \mathbf{B}_a , \mathbf{B}_b , \mathbf{B}_c [\mathbf{B}_d , \mathbf{B}_e , \mathbf{B}_f] at the positions indicated.

- $B_a = 0$
- $(B_b)(2\pi)(4\text{mm}) = \mu_0(3.7\text{A})$ $\Rightarrow B_b = 1.85 \times 10^{-4}\text{T}$ (right)
- $(B_c)(2\pi)(5\text{mm}) = \mu_0(3.7\text{A})$ $\Rightarrow B_c = 1.48 \times 10^{-4}\text{T}$ (right)



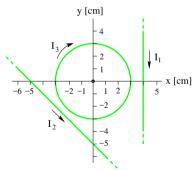
- $[(B_e)(2\pi)(4\text{mm}) = \mu_0(4.1\text{A}) \Rightarrow B_e = 2.05 \times 10^{-4}\text{T} \text{ (down)}]$
- $[(B_f)(2\pi)(6\text{mm}) = \mu_0(4.1\text{A}) \Rightarrow B_f = 1.37 \times 10^{-4}\text{T} \text{ (down)}]$





Two very long straight wires and a circular wire positioned in the xy-plane carry electric currents $I_1=I_2=I_3=1.3$ A [1.7A] in the directions shown.

- (a) Calculate magnitude (B_1, B_2, B_2) and direction (left/right/up/down/in/out) of the magnetic field produced by each current at the origin of the coordinate system.
- (b) Calculate magnitude μ and direction (left/right/up/down/in/out) of the magnetic dipole moment produced by the circular current.

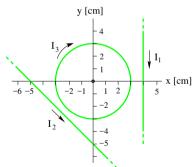




Two very long straight wires and a circular wire positioned in the xy-plane carry electric currents $I_1 = I_2 = I_3 = 1.3$ A [1.7A] in the directions shown.

- (a) Calculate magnitude (B_1, B_2, B_2) and direction (left/right/up/down/in/out) of the magnetic field produced by each current at the origin of the coordinate system.
- (b) Calculate magnitude μ and direction (left/right/up/down/in/out) of the magnetic dipole moment produced by the circular current.

(a)
$$B_1 = \frac{\mu_0(I_1)}{2\pi(4\mathrm{cm})} = 6.5\mu\mathrm{T}$$
 [8.5 $\mu\mathrm{T}$]. (in)
$$B_2 = \frac{\mu_0(I_2)}{2\pi(5\mathrm{cm}/\sqrt{2})} = 7.35\mu\mathrm{T}$$
 [9.62 $\mu\mathrm{T}$] (out)
$$B_3 = \frac{\mu_0(I_3)}{2(3\mathrm{cm})} = 27.2\mu\mathrm{T}$$
 [35.6 $\mu\mathrm{T}$] (in)

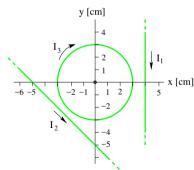




Two very long straight wires and a circular wire positioned in the xy-plane carry electric currents $I_1 = I_2 = I_3 = 1.3$ A [1.7A] in the directions shown.

- (a) Calculate magnitude (B_1, B_2, B_2) and direction (left/right/up/down/in/out) of the magnetic field produced by each current at the origin of the coordinate system.
- (b) Calculate magnitude μ and direction (left/right/up/down/in/out) of the magnetic dipole moment produced by the circular current.

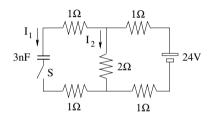
(a)
$$B_1=\frac{\mu_0(I_1)}{2\pi(4\mathrm{cm})}=6.5\mu\mathrm{T}$$
 [8.5 $\mu\mathrm{T}$]. (in)
$$B_2=\frac{\mu_0(I_2)}{2\pi(5\mathrm{cm}/\sqrt{2})}=7.35\mu\mathrm{T}$$
 [9.62 $\mu\mathrm{T}$] (out)
$$B_3=\frac{\mu_0(I_3)}{2(3\mathrm{cm})}=27.2\mu\mathrm{T}$$
 [35.6 $\mu\mathrm{T}$] (in) (b) $\mu=\pi(3\mathrm{cm})^2(I_3)=3.68\times10^{-3}\mathrm{Am}^2$ [4.81 $\times10^{-3}\mathrm{Am}^2$] (in)





This circuit is in a steady state with the switch open and the capacitor discharged.

- (a) Find the currents I_1 and I_2 while the switch is still open.
- (b) Find the currents I_1 and I_2 right after the switch has been closed.
- (c) Find the currents I_1 and I_2 a long time later.
- (d) Find the voltage ${\it V}$ across the capacitor, also a long time later.

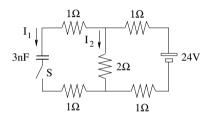




This circuit is in a steady state with the switch open and the capacitor discharged.

- (a) Find the currents I_1 and I_2 while the switch is still open.
- (b) Find the currents I_1 and I_2 right after the switch has been closed.
- (c) Find the currents I_1 and I_2 a long time later.
- (d) Find the voltage ${\it V}$ across the capacitor, also a long time later.

(a)
$$I_1 = 0$$
, $I_2 = \frac{24V}{1\Omega + 2\Omega + 1\Omega} = 6A$.



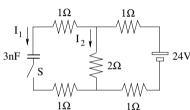


This circuit is in a steady state with the switch open and the capacitor discharged.

- (a) Find the currents I_1 and I_2 while the switch is still open.
- (b) Find the currents I_1 and I_2 right after the switch has been closed.
- (c) Find the currents I_1 and I_2 a long time later.
- (d) Find the voltage V across the capacitor, also a long time later.

(a)
$$I_1 = 0$$
, $I_2 = \frac{24V}{1\Omega + 2\Omega + 1\Omega} = 6A$.

(a)
$$I_1=0$$
, $I_2=\frac{21V}{1\Omega+2\Omega+1\Omega}=6A$.
(b) $R_{eq}=1\Omega+\left(\frac{1}{2\Omega}+\frac{1}{1\Omega+1\Omega}\right)^{-1}+1\Omega=3\Omega$ (capacitor discharged)
$$\Rightarrow I_1+I_2=\frac{24V}{3\Omega}=8A,\quad I_1=I_2=4A.$$

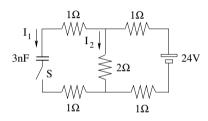




This circuit is in a steady state with the switch open and the capacitor discharged.

- (a) Find the currents I_1 and I_2 while the switch is still open.
- (b) Find the currents I_1 and I_2 right after the switch has been closed.
- (c) Find the currents I_1 and I_2 a long time later.
- (d) Find the voltage ${\it V}$ across the capacitor, also a long time later.

(a)
$$I_1 = 0$$
, $I_2 = \frac{24V}{1\Omega + 2\Omega + 1\Omega} = 6A$.



(b)
$$R_{eq}=1\Omega+\left(\frac{1}{2\Omega}+\frac{1}{1\Omega+1\Omega}\right)^{-1}+1\Omega=3\Omega$$
 (capacitor discharged)
$$\Rightarrow I_1+I_2=\frac{24\mathrm{V}}{3\Omega}=8\mathrm{A},\quad I_1=I_2=4\mathrm{A}.$$

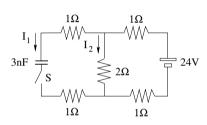
(c) capacitor fully charged:
$$I_1=0,\quad I_2=\frac{24V}{1\Omega+2\Omega+1\Omega}=6A.$$



This circuit is in a steady state with the switch open and the capacitor discharged.

- (a) Find the currents I_1 and I_2 while the switch is still open.
- (b) Find the currents I_1 and I_2 right after the switch has been closed.
- (c) Find the currents I_1 and I_2 a long time later.
- (d) Find the voltage V across the capacitor, also a long time later.

(a)
$$I_1 = 0$$
, $I_2 = \frac{24V}{1\Omega + 2\Omega + 1\Omega} = 6A$.



(b)
$$R_{eq}=1\Omega+\left(rac{1}{2\Omega}+rac{1}{1\Omega+1\Omega}
ight)^{-1}+1\Omega=3\Omega$$
 (capacitor discharged)
$$\Rightarrow I_1+I_2=rac{24{
m V}}{3\Omega}=8{
m A},\quad I_1=I_2=4{
m A}.$$

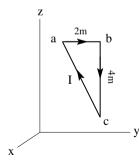
(c) capacitor fully charged:
$$I_1=0, \quad I_2=\frac{24 V}{1\Omega+2\Omega+1\Omega}=6 A.$$

(d) loop rule:
$$(2\Omega)(6A) - (1\Omega)(0A) - V - (1\Omega)(0A) = 0 \implies V = 12V$$
.



Consider a region with uniform magnetic field $\vec{B}=3T\hat{\bf j}+5T\hat{\bf k}$. A conducting loop positioned in the yz-plane has the shape of a right-angled triangle and carries a clockwise current I=2A.

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F}_{ab} (magnitude and direction) acting on side ab.
- (c) Find the force \vec{F}_{bc} (magnitude and direction) acting on side bc.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

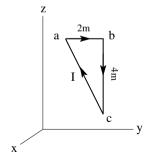




Consider a region with uniform magnetic field $\vec{B}=3T\hat{\bf j}+5T\hat{\bf k}$. A conducting loop positioned in the yz-plane has the shape of a right-angled triangle and carries a clockwise current I=2A.

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F}_{ab} (magnitude and direction) acting on side ab.
- (c) Find the force \vec{F}_{bc} (magnitude and direction) acting on side bc.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

(a)
$$\vec{\mu} = -(2A)(4m^2)\hat{i} = -8Am^2\hat{i}$$
.



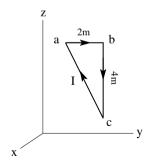


Consider a region with uniform magnetic field $\vec{B}=3T\hat{\bf j}+5T\hat{\bf k}$. A conducting loop positioned in the yz-plane has the shape of a right-angled triangle and carries a clockwise current I=2A.

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F}_{ab} (magnitude and direction) acting on side ab.
- (c) Find the force \vec{F}_{bc} (magnitude and direction) acting on side bc.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

(a)
$$\vec{\mu} = -(2A)(4m^2)\hat{\mathbf{i}} = -8Am^2\hat{\mathbf{i}}$$
.

(b)
$$\vec{F}_{ab} = (2A)(2m\hat{\mathbf{j}}) \times [3T\hat{\mathbf{j}} + 5T\hat{\mathbf{k}}] = 20N\hat{\mathbf{i}}$$
.





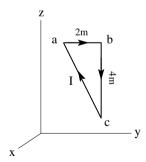
Consider a region with uniform magnetic field $\vec{B}=3T\hat{\bf j}+5T\hat{\bf k}$. A conducting loop positioned in the yz-plane has the shape of a right-angled triangle and carries a clockwise current I=2A.

- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F}_{ab} (magnitude and direction) acting on side ab.
- (c) Find the force \vec{F}_{bc} (magnitude and direction) acting on side bc.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

(a)
$$\vec{\mu} = -(2A)(4m^2)\hat{\mathbf{i}} = -8Am^2\hat{\mathbf{i}}$$
.

(b)
$$\vec{F}_{ab} = (2A)(2m\hat{\mathbf{j}}) \times [3T\hat{\mathbf{j}} + 5T\hat{\mathbf{k}}] = 20N\hat{\mathbf{i}}$$
.

(c)
$$\vec{F}_{bc} = (2A)(-4m\hat{\mathbf{k}}) \times [3T\hat{\mathbf{j}} + 5T\hat{\mathbf{k}}] = 24N\hat{\mathbf{i}}.$$





Consider a region with uniform magnetic field $\vec{B}=3T\hat{\bf j}+5T\hat{\bf k}$. A conducting loop positioned in the yz-plane has the shape of a right-angled triangle and carries a clockwise current I=2A.

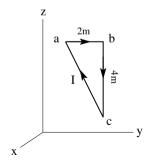
- (a) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the loop.
- (b) Find the force \vec{F}_{ab} (magnitude and direction) acting on side ab.
- (c) Find the force \vec{F}_{bc} (magnitude and direction) acting on side bc.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the loop.

(a)
$$\vec{\mu} = -(2A)(4m^2)\hat{\mathbf{i}} = -8Am^2\hat{\mathbf{i}}$$
.

(b)
$$\vec{F}_{ab} = (2A)(2m\hat{j}) \times [3T\hat{j} + 5T\hat{k}] = 20N\hat{i}$$
.

(c)
$$\vec{F}_{bc} = (2A)(-4m\hat{\mathbf{k}}) \times [3T\hat{\mathbf{j}} + 5T\hat{\mathbf{k}}] = 24N\hat{\mathbf{i}}.$$

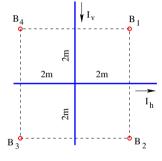
(d)
$$\vec{\tau} = (-8\text{Am}^2\hat{\mathbf{i}}) \times \left[3T\hat{\mathbf{j}} + 5T\hat{\mathbf{k}}\right] = -24\text{Nm}\hat{\mathbf{k}} + 40\text{Nm}\hat{\mathbf{j}}$$





Consider two infinitely long, straight wires with currents $I_v=3$ A, $I_h=3$ A in the directions shown.

Find direction (in/out) and magnitude of the magnetic fields B_1 , B_2 , B_3 , B_4 , at the points marked in the graph.

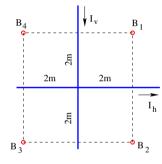




Consider two infinitely long, straight wires with currents $I_v=3$ A, $I_h=3$ A in the directions shown.

Find direction (in/out) and magnitude of the magnetic fields \mathbf{B}_1 , \mathbf{B}_2 , \mathbf{B}_3 , \mathbf{B}_4 , at the points marked in the graph.

•
$$B_1 = \frac{\mu_0}{2\pi} \left(\frac{I_v}{2m} + \frac{I_h}{2m} \right) = +6 \times 10^{-7} \text{T (out)}.$$



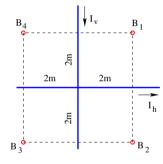


Consider two infinitely long, straight wires with currents $I_v = 3A$, $I_h = 3A$ in the directions shown.

Find direction (in/out) and magnitude of the magnetic fields B_1 , B_2 , B_3 , B_4 , at the points marked in the graph.

•
$$B_1 = \frac{\mu_0}{2\pi} \left(\frac{I_v}{2m} + \frac{I_h}{2m} \right) = +6 \times 10^{-7} \text{T (out)}.$$

•
$$B_2 = \frac{\mu_0}{2\pi} \left(\frac{I_v}{2\mathrm{m}} - \frac{I_h}{2\mathrm{m}} \right) = 0.$$





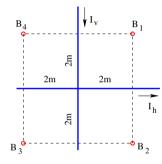
Consider two infinitely long, straight wires with currents $I_v = 3A$, $I_h = 3A$ in the directions shown.

Find direction (in/out) and magnitude of the magnetic fields B_1 , B_2 , B_3 , B_4 , at the points marked in the graph.

•
$$B_1 = \frac{\mu_0}{2\pi} \left(\frac{I_v}{2m} + \frac{I_h}{2m} \right) = +6 \times 10^{-7} \text{T (out)}.$$

•
$$B_2 = \frac{\mu_0}{2\pi} \left(\frac{I_v}{2\mathrm{m}} - \frac{I_h}{2\mathrm{m}} \right) = 0.$$

•
$$B_3 = \frac{\mu_0}{2\pi} \left(-\frac{I_v}{2m} - \frac{I_h}{2m} \right) = -6 \times 10^{-7} \text{T (in)}.$$





Consider two infinitely long, straight wires with currents $I_v=3$ A, $I_h=3$ A in the directions shown.

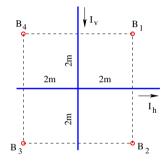
Find direction (in/out) and magnitude of the magnetic fields B_1 , B_2 , B_3 , B_4 , at the points marked in the graph.

•
$$B_1 = \frac{\mu_0}{2\pi} \left(\frac{I_v}{2m} + \frac{I_h}{2m} \right) = +6 \times 10^{-7} \text{T (out)}.$$

•
$$B_2 = \frac{\mu_0}{2\pi} \left(\frac{I_v}{2m} - \frac{I_h}{2m} \right) = 0.$$

•
$$B_3 = \frac{\mu_0}{2\pi} \left(-\frac{I_v}{2m} - \frac{I_h}{2m} \right) = -6 \times 10^{-7} \text{T (in)}.$$

$$\bullet \ B_4 = \frac{\mu_0}{2\pi} \left(-\frac{I_v}{2m} + \frac{I_h}{2m} \right) = 0.$$





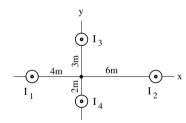
Consider long, straight currents,

(a)
$$I_1 = I_4 = 12A$$
, $I_2 = I_3 = 0$,

(b)
$$I_2 = I_3 = 12$$
A, $I_1 = I_4 = 0$,

perpendicular to the xy-plane and directed out of that plane. Find the magnetic field in the form $\mathbf{B} = B_x \hat{\mathbf{i}} + B_y \hat{\mathbf{j}}$ generated at the origin of the coordinate system.

Use the value $\mu_0/2\pi=2 imes 10^{-7} {
m Tm/A}$.





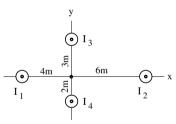
Consider long, straight currents,

(a)
$$I_1 = I_4 = 12A$$
, $I_2 = I_3 = 0$,

(b)
$$I_2 = I_3 = 12$$
A, $I_1 = I_4 = 0$,

perpendicular to the xy-plane and directed out of that plane. Find the magnetic field in the form $\mathbf{B} = B_x \hat{\mathbf{i}} + B_y \hat{\mathbf{j}}$ generated at the origin of the coordinate system.

Use the value $\mu_0/2\pi=2\times 10^{-7} {
m Tm/A}$.



(a)
$$B_x = -\frac{\mu_0(12A)}{2\pi(2m)} = -12 \times 10^{-7} \text{T}, \quad B_y = \frac{\mu_0(12A)}{2\pi(4m)} = 6 \times 10^{-7} \text{T}.$$



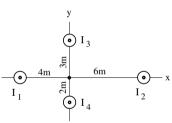
Consider long, straight currents,

(a)
$$I_1 = I_4 = 12A$$
, $I_2 = I_3 = 0$,

(b)
$$I_2 = I_3 = 12A$$
, $I_1 = I_4 = 0$,

perpendicular to the xy-plane and directed out of that plane. Find the magnetic field in the form $\mathbf{B} = B_x \hat{\mathbf{i}} + B_y \hat{\mathbf{j}}$ generated at the origin of the coordinate system.

Use the value $\mu_0/2\pi=2\times 10^{-7} {
m Tm/A}$.



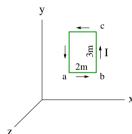
(a)
$$B_x = -\frac{\mu_0(12A)}{2\pi(2m)} = -12 \times 10^{-7} \text{T}, \quad B_y = \frac{\mu_0(12A)}{2\pi(4m)} = 6 \times 10^{-7} \text{T}.$$

(b)
$$B_x = \frac{\mu_0(12\text{A})}{2\pi(3\text{m})} = 8 \times 10^{-7}\text{T}, \quad B_y = -\frac{\mu_0(12\text{A})}{2\pi(6\text{m})} = -4 \times 10^{-7}\text{T}.$$



A counterclockwise current I=3A [I=2A] is flowing through the conducting rectangular frame positioned in the xy-plane. A uniform magnetic field $\mathbf{B}=2$ T $\hat{\mathbf{j}}$ [$\mathbf{B}=4$ T $\hat{\mathbf{i}}$] is present.

- (a) Find the force \mathbf{F}_{ab} (magnitude and direction) acting on side ab of the rectangle.
- (b) Find the force \mathbf{F}_{bc} (magnitude and direction) acting on side bc of the rectangle.
- (c) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the current loop.

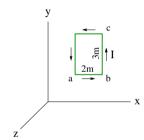




A counterclockwise current I=3A [I=2A] is flowing through the conducting rectangular frame positioned in the xy-plane. A uniform magnetic field $\mathbf{B}=2$ T $\hat{\mathbf{j}}$ $[\mathbf{B}=4$ T $\hat{\mathbf{i}}]$ is present.

- (a) Find the force \mathbf{F}_{ab} (magnitude and direction) acting on side ab of the rectangle.
- (b) Find the force \mathbf{F}_{bc} (magnitude and direction) acting on side bc of the rectangle.
- (c) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the current loop.

(a)
$$\mathbf{F}_{ab} = (3\mathrm{A})(2\mathrm{m}\mathbf{\hat{i}}) \times (2\mathrm{T}\mathbf{\hat{j}}) = 12\mathrm{N}\mathbf{\hat{k}}$$
 $[\mathbf{F}_{ab} = (2\mathrm{A})(2\mathrm{m}\mathbf{\hat{i}}) \times (4\mathrm{T}\mathbf{\hat{i}}) = \mathbf{0}].$



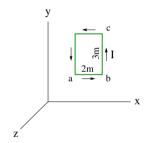


A counterclockwise current I = 3A [I = 2A] is flowing through the conducting rectangular frame positioned in the xy-plane. A uniform magnetic field $\mathbf{B} = 2\mathbf{T}_{\mathbf{i}}^2 [\mathbf{B} = 4\mathbf{T}_{\mathbf{i}}^2]$ is present.

- (a) Find the force \mathbf{F}_{ab} (magnitude and direction) acting on side ab of the rectangle.
- (b) Find the force \mathbf{F}_{bc} (magnitude and direction) acting on side bc of the rectangle.
- (c) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the current loop.

(a)
$$\mathbf{F}_{ab} = (3 \mathrm{A}) (2 \mathrm{m} \hat{\mathbf{i}}) \times (2 \mathrm{T} \hat{\mathbf{j}}) = 12 \mathrm{N} \hat{\mathbf{k}} \qquad [\mathbf{F}_{ab} = (2 \mathrm{A}) (2 \mathrm{m} \hat{\mathbf{i}}) \times (4 \mathrm{T} \hat{\mathbf{i}}) = \mathbf{0}].$$

(b)
$$\mathbf{F}_{bc} = (3A)(3m\hat{\mathbf{j}}) \times (2T\hat{\mathbf{j}}) = 0$$
 $[\mathbf{F}_{bc} = (2A)(3m\hat{\mathbf{j}}) \times (4T\hat{\mathbf{i}}) = -24N\hat{\mathbf{k}}].$





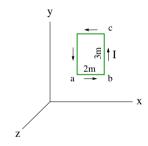
A counterclockwise current I=3A [I=2A] is flowing through the conducting rectangular frame positioned in the xy-plane. A uniform magnetic field $\mathbf{B}=2$ T $\hat{\mathbf{j}}$ $[\mathbf{B}=4$ T $\hat{\mathbf{i}}]$ is present.

- (a) Find the force \mathbf{F}_{ab} (magnitude and direction) acting on side ab of the rectangle.
- (b) Find the force \mathbf{F}_{bc} (magnitude and direction) acting on side bc of the rectangle.
- (c) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the current loop.

$$\mbox{(a)} \ \ F_{ab} = (3A)(2m\textbf{\^{i}}) \times (2T\textbf{\^{j}}) = 12N\textbf{\^{k}} \qquad [F_{ab} = (2A)(2m\textbf{\^{i}}) \times (4T\textbf{\^{i}}) = \textbf{0}].$$

(b)
$$\mathbf{F}_{bc} = (3A)(3m\hat{\mathbf{j}}) \times (2T\hat{\mathbf{j}}) = 0$$
 $[\mathbf{F}_{bc} = (2A)(3m\hat{\mathbf{j}}) \times (4T\hat{\mathbf{i}}) = -24N\hat{\mathbf{k}}].$

(c)
$$\vec{\mu} = [(2m)(3m)\hat{\mathbf{k}}](3A) = 18Am^2\hat{\mathbf{k}} \qquad [\vec{\mu} = [(2m)(3m)\hat{\mathbf{k}}](2A) = 12Am^2\hat{\mathbf{k}}].$$





A counterclockwise current I=3A [I=2A] is flowing through the conducting rectangular frame positioned in the xy-plane. A uniform magnetic field $\mathbf{B}=2$ T $\hat{\mathbf{j}}$ $[\mathbf{B}=4$ T $\hat{\mathbf{i}}]$ is present.

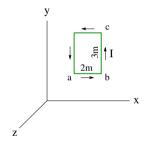
- (a) Find the force \mathbf{F}_{ab} (magnitude and direction) acting on side ab of the rectangle.
- (b) Find the force \mathbf{F}_{bc} (magnitude and direction) acting on side bc of the rectangle.
- (c) Find the magnetic moment $\vec{\mu}$ (magnitude and direction) of the current loop.
- (d) Find the torque $\vec{\tau}$ (magnitude and direction) acting on the current loop.

$$\mbox{(a)} \ \ F_{ab} = (3A)(2m\textbf{\^{i}}) \times (2T\textbf{\^{j}}) = 12N\textbf{\^{k}} \qquad [F_{ab} = (2A)(2m\textbf{\^{i}}) \times (4T\textbf{\^{i}}) = \textbf{0}].$$

$$\mbox{(b)} \ \ \mbox{${\bf F}_{bc} = (3A)(3m{\bf \hat{j}}) \times (2T{\bf \hat{j}}) = 0$} \qquad \mbox{$[{\bf F}_{bc} = (2A)(3m{\bf \hat{j}}) \times (4T{\bf \hat{i}}) = -24N{\bf \hat{k}}]$}.$$

(c)
$$\vec{\mu} = [(2m)(3m)\hat{\mathbf{k}}](3A) = 18Am^2\hat{\mathbf{k}} \qquad [\vec{\mu} = [(2m)(3m)\hat{\mathbf{k}}](2A) = 12Am^2\hat{\mathbf{k}}].$$

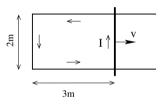
(d)
$$\vec{\tau} = (18 \text{Am}^2 \hat{\mathbf{k}}) \times (2 \text{T} \hat{\mathbf{j}}) = -36 \text{Nm} \hat{\mathbf{i}}$$
 $[\vec{\tau} = (12 \text{Am}^2 \hat{\mathbf{k}}) \times (4 \text{T} \hat{\mathbf{i}}) = 48 \text{Nm} \hat{\mathbf{j}}.$





A conducting frame with a moving conducting rod is located in a uniform magnetic field of magnitude B=5T [B=10T] directed perpendicular to the plane of the frame. The moving rod induces a counterclockwise current I=3A [I=2A] around the loop, which has resistance $R=2\Omega$ [$R=4\Omega$].

- (a) Find the magnetic flux $|\Phi_B|$ through the loop at the instant shown.
- (b) Find the induced emf \mathcal{E} .
- (c) Find the speed v of the rod.
- (d) Find the force F (magnitude) needed to keep the rod moving at speed v.
- (e) Find the direction (\odot, \otimes) of the magnetic field **B**.





A conducting frame with a moving conducting rod is located in a uniform magnetic field of magnitude B=5T [B=10T] directed perpendicular to the plane of the frame. The moving rod induces a counterclockwise current I=3A [I=2A] around the loop, which has resistance $R=2\Omega$ [$R=4\Omega$].

- (a) Find the magnetic flux $|\Phi_B|$ through the loop at the instant shown.
- (b) Find the induced emf \mathcal{E} .
- (c) Find the speed v of the rod.
- (d) Find the force F (magnitude) needed to keep the rod moving at speed v.
- (e) Find the direction (\odot, \otimes) of the magnetic field **B**.

(a)
$$|\Phi_B| = (2m)(3m)(5T) = 30Wb$$
 $[|\Phi_B| = (2m)(3m)(10T) = 60Wb$.



A conducting frame with a moving conducting rod is located in a uniform magnetic field of magnitude B=5T [B=10T] directed perpendicular to the plane of the frame. The moving rod induces a counterclockwise current I=3A [I=2A] around the loop, which has resistance $R=2\Omega$ [$R=4\Omega$].

- (a) Find the magnetic flux $|\Phi_B|$ through the loop at the instant shown.
- (b) Find the induced emf \mathcal{E} .
- (c) Find the speed v of the rod.
- (d) Find the force F (magnitude) needed to keep the rod moving at speed v.
- (e) Find the direction (\odot, \otimes) of the magnetic field **B**.

$\begin{bmatrix} \mathbf{E} \\ \mathbf{V} \\ \mathbf{I} \\ \mathbf{J} \\ \mathbf{J}$

$$\mbox{(a)} \ |\Phi_B| = (2m)(3m)(5T) = 30 \\ \mbox{Wb} \qquad [|\Phi_B| = (2m)(3m)(10T) = 60 \\ \mbox{Wb}.$$

$$\mbox{(b)} \ \mathcal{E}=(2\Omega)(3A)=6V \qquad [\mathcal{E}=(4\Omega)(2A)=8V]. \label{eq:energy}$$



A conducting frame with a moving conducting rod is located in a uniform magnetic field of magnitude B=5T [B=10T] directed perpendicular to the plane of the frame. The moving rod induces a counterclockwise current I=3A [I=2A] around the loop, which has resistance $R=2\Omega$ [$R=4\Omega$].

- (a) Find the magnetic flux $|\Phi_B|$ through the loop at the instant shown.
- (b) Find the induced emf \mathcal{E} .
- (c) Find the speed v of the rod.
- (d) Find the force F (magnitude) needed to keep the rod moving at speed v.
- (e) Find the direction (\odot, \otimes) of the magnetic field **B**.

(a)
$$|\Phi_B| = (2m)(3m)(5T) = 30$$
Wb $[|\Phi_B| = (2m)(3m)(10T) = 60$ Wb.

$$\mbox{(b)} \ \mathcal{E}=(2\Omega)(3A)=6V \qquad [\mathcal{E}=(4\Omega)(2A)=8V]. \label{eq:energy}$$

(c)
$$v = \frac{6V}{(5T)(2m)} = 0.6 \text{m/s}$$
 $\left[v = \frac{8V}{(10T)(2m)} = 0.4 \text{m/s}\right]$.



A conducting frame with a moving conducting rod is located in a uniform magnetic field of magnitude B=5T [B=10T] directed perpendicular to the plane of the frame. The moving rod induces a counterclockwise current I=3A [I=2A] around the loop, which has resistance $R=2\Omega$ [$R=4\Omega$].

- (a) Find the magnetic flux $|\Phi_B|$ through the loop at the instant shown.
- (b) Find the induced emf \mathcal{E} .
- (c) Find the speed v of the rod.
- (d) Find the force F (magnitude) needed to keep the rod moving at speed v.
- (e) Find the direction (\odot, \otimes) of the magnetic field **B**.

(a)
$$|\Phi_B| = (2m)(3m)(5T) = 30Wb$$
 $[|\Phi_B| = (2m)(3m)(10T) = 60Wb.$

(b)
$$\mathcal{E}=(2\Omega)(3A)=6V$$
 $[\mathcal{E}=(4\Omega)(2A)=8V].$

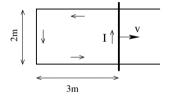
(c)
$$v = \frac{6\text{V}}{(5\text{T})(2\text{m})} = 0.6\text{m/s}$$
 $\left[v = \frac{8\text{V}}{(10\text{T})(2\text{m})} = 0.4\text{m/s}\right].$

(d)
$$F = (3A)(2m)(5T) = 30N$$
 $[F = (2A)(2m)(10T) = 40N].$



A conducting frame with a moving conducting rod is located in a uniform magnetic field of magnitude B=5T [B=10T] directed perpendicular to the plane of the frame. The moving rod induces a counterclockwise current I=3A [I=2A] around the loop, which has resistance $R=2\Omega$ [$R=4\Omega$].

- (a) Find the magnetic flux $|\Phi_B|$ through the loop at the instant shown.
- (b) Find the induced emf \mathcal{E} .
- (c) Find the speed v of the rod.
- (d) Find the force ${\it F}$ (magnitude) needed to keep the rod moving at speed ${\it v}.$
- (e) Find the direction (\odot, \otimes) of the magnetic field **B**.



(a)
$$|\Phi_B| = (2m)(3m)(5T) = 30Wb$$
 $[|\Phi_B| = (2m)(3m)(10T) = 60Wb.$

(b)
$$\mathcal{E}=(2\Omega)(3A)=6V$$
 $[\mathcal{E}=(4\Omega)(2A)=8V].$

(c)
$$v = \frac{6\text{V}}{(5\text{T})(2\text{m})} = 0.6\text{m/s}$$
 $\left[v = \frac{8\text{V}}{(10\text{T})(2\text{m})} = 0.4\text{m/s}\right].$

(d)
$$F = (3A)(2m)(5T) = 30N$$
 $[F = (2A)(2m)(10T) = 40N].$

(e)
$$\otimes$$
 $[\otimes]$.