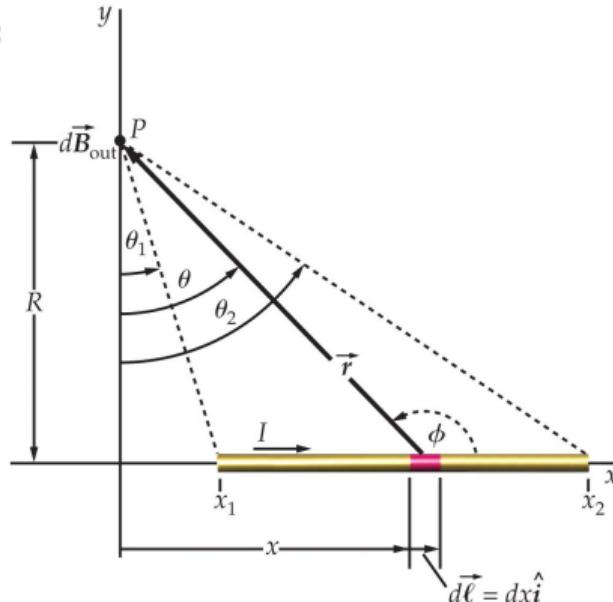


Magnetic Field Generated by Current in Straight Wire (1)



Consider a field point P that is a distance R from the axis.

- $dB = \frac{\mu_0}{4\pi} \frac{Idx}{r^2} \sin \phi = \frac{\mu_0}{4\pi} \frac{Idx}{r^2} \cos \theta$
- $x = R \tan \theta \Rightarrow \frac{dx}{d\theta} = \frac{R}{\cos^2 \theta} = \frac{R}{R^2/r^2} = \frac{r^2}{R}$
- $dB = \frac{\mu_0}{4\pi} \frac{I}{r^2} \frac{r^2 d\theta}{R} \cos \theta = \frac{\mu_0 I}{4\pi R} \cos \theta d\theta$
- $B = \frac{\mu_0 I}{4\pi R} \int_{\theta_1}^{\theta_2} \cos \theta d\theta$
 $= \frac{\mu_0 I}{4\pi R} (\sin \theta_2 - \sin \theta_1)$
- Length of wire: $L = R(\tan \theta_2 - \tan \theta_1)$



Wire of infinite length: $\theta_1 = -90^\circ, \theta_2 = 90^\circ \Rightarrow B = \frac{\mu_0 I}{2\pi R}$