## Classification of phase transitions [tln28]

Consider a 1-component fluid system with phases I and II.

The Gibbs free energy has a different functional dependence on its natural variables in the two phases:

$$G^{I}(T, p, n) = \mu^{I}(T, p)n, \quad G^{II}(T, p, n) = \mu^{II}(T, p)n.$$

For given values of T and p, the equilibrium state is the one with the lowest Gibbs free energy, i.e the state with the lower chemical potential.

At the transition:  $G^I = G^{II}$ , i.e.  $G^* = \mu^*(n^I + n^{II})$  with  $n^I + n^{II} = n$ .

## Discontinuous transition:

The volume and the entropy change discontinuously:

1. 
$$\left(\frac{\partial G}{\partial n}\right)_{T,p}^{I} = \left(\frac{\partial G}{\partial n}\right)_{T,p}^{II} \Rightarrow \mu^{I} = \mu^{II} = \mu^{*}.$$

2. 
$$\left(\frac{\partial G}{\partial p}\right)_{T,n}^{I} \neq \left(\frac{\partial G}{\partial p}\right)_{T,n}^{II} \Rightarrow V^{I} \neq V^{II}$$
.

3. 
$$\left(\frac{\partial G}{\partial T}\right)_{n,p}^{I} \neq \left(\frac{\partial G}{\partial T}\right)_{n,p}^{II} \Rightarrow S^{I} \neq S^{II}$$
.

Latent heat (change in enthalpy):  $\Delta E = \Delta (G + TS) = T\Delta S$ 

## Continuous transition:

The volume and the entropy change continuously. Discontinuities or divergences occur in higher-order derivatives.

1. 
$$\left(\frac{\partial G}{\partial n}\right)_{T,p}^{I} = \left(\frac{\partial G}{\partial n}\right)_{T,p}^{II} \Rightarrow \mu^{I} = \mu^{II} = \mu^{*}.$$

$$2. \left(\frac{\partial G}{\partial p}\right)_{T,n}^{I} = \left(\frac{\partial G}{\partial p}\right)_{T,n}^{II} \Rightarrow V^{I} = V^{II}.$$

3. 
$$\left(\frac{\partial G}{\partial T}\right)_{n,p}^{I} = \left(\frac{\partial G}{\partial T}\right)_{n,p}^{II} \implies S^{I} = S^{II}.$$